

Computer algebra independent integration tests

4-Trig-functions/4.3-Tangent/4.3.10-c+d-x-^m-a+b-tan-^n

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Contents

1	Introduction	3
1.1	Listing of CAS systems tested	3
1.2	Results	3
1.3	Performance	7
1.4	list of integrals that has no closed form antiderivative	8
1.5	list of integrals solved by CAS but has no known antiderivative	8
1.6	list of integrals solved by CAS but failed verification	8
1.7	Timing	9
1.8	Verification	9
1.9	Important notes about some of the results	9
1.9.1	Important note about Maxima results	9
1.9.2	Important note about FriCAS and Giac/XCAS results	10
1.9.3	Important note about finding leaf size of antiderivative	10
1.9.4	Important note about Mupad results	11
1.10	Design of the test system	11
2	detailed summary tables of results	13
2.1	List of integrals sorted by grade for each CAS	13
2.1.1	Rubi	13
2.1.2	Mathematica	13
2.1.3	Maple	13
2.1.4	Maxima	13
2.1.5	FriCAS	14
2.1.6	Sympy	14
2.1.7	Giac	14
2.1.8	Mupad	14
2.2	Detailed conclusion table per each integral for all CAS systems	15
2.3	Detailed conclusion table specific for Rubi results	25
3	Listing of integrals	29
3.1	$\int x^3 \tan(a + bx) dx$	29
3.2	$\int x^2 \tan(a + bx) dx$	33
3.3	$\int x \tan(a + bx) dx$	36
3.4	$\int \frac{\tan(a+bx)}{x} dx$	39
3.5	$\int \frac{\tan(a+bx)}{x^2} dx$	41
3.6	$\int x^3 \tan^2(a + bx) dx$	43

3.7	$\int x^2 \tan^2(a + bx) dx$	47
3.8	$\int x \tan^2(a + bx) dx$	50
3.9	$\int \frac{\tan^2(a+bx)}{x} dx$	53
3.10	$\int \frac{\tan^2(a+bx)}{x^2} dx$	55
3.11	$\int x^3 \tan^3(a + bx) dx$	57
3.12	$\int x^2 \tan^3(a + bx) dx$	62
3.13	$\int x \tan^3(a + bx) dx$	66
3.14	$\int \frac{\tan^3(a+bx)}{x} dx$	69
3.15	$\int \frac{\tan^3(a+bx)}{x^2} dx$	71
3.16	$\int \left(\frac{x^2}{\tan^2(a+bx)} - \frac{4x}{b\sqrt{\tan(a+bx)}} + x^2 \sqrt{\tan(a+bx)} \right) dx$	73
3.17	$\int \left(\frac{x^2}{\sqrt{\tan(a+bx^2)}} + \frac{\sqrt{\tan(a+bx^2)}}{b} + x^2 \tan^{\frac{3}{2}}(a + bx^2) \right) dx$	76
3.18	$\int \frac{(c+dx)^3}{a+ia \tan(e+fx)} dx$	78
3.19	$\int \frac{(c+dx)^2}{a+ia \tan(e+fx)} dx$	82
3.20	$\int \frac{c+dx}{a+ia \tan(e+fx)} dx$	85
3.21	$\int \frac{1}{(c+dx)(a+ia \tan(e+fx))} dx$	88
3.22	$\int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))} dx$	91
3.23	$\int \frac{1}{(c+dx)^3(a+ia \tan(e+fx))} dx$	95
3.24	$\int \frac{(c+dx)^3}{(a+ia \tan(e+fx))^2} dx$	99
3.25	$\int \frac{(c+dx)^2}{(a+ia \tan(e+fx))^2} dx$	104
3.26	$\int \frac{c+dx}{(a+ia \tan(e+fx))^2} dx$	108
3.27	$\int \frac{1}{(c+dx)(a+ia \tan(e+fx))^2} dx$	111
3.28	$\int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))^2} dx$	115
3.29	$\int \frac{(c+dx)^3}{(a+ia \tan(e+fx))^3} dx$	119
3.30	$\int \frac{(c+dx)^2}{(a+ia \tan(e+fx))^3} dx$	125
3.31	$\int \frac{c+dx}{(a+ia \tan(e+fx))^3} dx$	129
3.32	$\int \frac{1}{(c+dx)(a+ia \tan(e+fx))^3} dx$	133
3.33	$\int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))^3} dx$	137
3.34	$\int (c + dx)^m (a + ia \tan(e + fx))^2 dx$	142
3.35	$\int (c + dx)^m (a + ia \tan(e + fx)) dx$	144
3.36	$\int \frac{(c+dx)^m}{a+ia \tan(e+fx)} dx$	146
3.37	$\int \frac{(c+dx)^m}{(a+ia \tan(e+fx))^2} dx$	149
3.38	$\int \frac{(c+dx)^m}{(a+ia \tan(e+fx))^3} dx$	152
3.39	$\int (c + dx)^3 (a + b \tan(e + fx)) dx$	155
3.40	$\int (c + dx)^2 (a + b \tan(e + fx)) dx$	159
3.41	$\int (c + dx) (a + b \tan(e + fx)) dx$	163
3.42	$\int \frac{a+b \tan(e+fx)}{c+dx} dx$	166
3.43	$\int \frac{a+b \tan(e+fx)}{(c+dx)^2} dx$	168
3.44	$\int (c + dx)^3 (a + b \tan(e + fx))^2 dx$	170
3.45	$\int (c + dx)^2 (a + b \tan(e + fx))^2 dx$	176

3.46	$\int (c + dx)(a + b \tan(e + fx))^2 dx$	181
3.47	$\int \frac{(a+b \tan(e+fx))^2}{c+dx} dx$	185
3.48	$\int \frac{(a+b \tan(e+fx))^2}{(c+dx)^2} dx$	187
3.49	$\int (c + dx)^3(a + b \tan(e + fx))^3 dx$	189
3.50	$\int (c + dx)^2(a + b \tan(e + fx))^3 dx$	198
3.51	$\int (c + dx)(a + b \tan(e + fx))^3 dx$	205
3.52	$\int \frac{(a+b \tan(e+fx))^3}{c+dx} dx$	209
3.53	$\int \frac{(a+b \tan(e+fx))^3}{(c+dx)^2} dx$	212
3.54	$\int \frac{(c+dx)^3}{a+b \tan(e+fx)} dx$	215
3.55	$\int \frac{(c+dx)^2}{a+b \tan(e+fx)} dx$	220
3.56	$\int \frac{c+dx}{a+b \tan(e+fx)} dx$	224
3.57	$\int \frac{1}{(c+dx)(a+b \tan(e+fx))} dx$	228
3.58	$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))} dx$	230
3.59	$\int \frac{(c+dx)^3}{(a+b \tan(e+fx))^2} dx$	232
3.60	$\int \frac{(c+dx)^2}{(a+b \tan(e+fx))^2} dx$	241
3.61	$\int \frac{c+dx}{(a+b \tan(e+fx))^2} dx$	248
3.62	$\int \frac{1}{(c+dx)(a+b \tan(e+fx))^2} dx$	253
3.63	$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))^2} dx$	255
4	Listing of Grading functions	257
4.0.1	Mathematica and Rubi grading function	257
4.0.2	Maple grading function	259
4.0.3	Sympy grading function	262
4.0.4	SageMath grading function	264

Chapter 1

Introduction

This report gives the result of running the computer algebra independent integration problems. The listing of the problems are maintained by and can be downloaded from <https://rulebasedintegration.org>

The number of integrals in this report is [63]. This is test number [99].

1.1 Listing of CAS systems tested

The following systems were tested at this time.

1. Mathematica 12.3 (64 bit) on windows 10.
2. Rubi 4.16.1 in Mathematica 12.1 on windows 10.
3. Maple 2021.1 (64 bit) on windows 10.
4. Maxima 5.44 on Linux. (via sagemath 9.3)
5. Fricas 1.3.7 on Linux (via sagemath 9.3)
6. Giac/Xcas 1.7 on Linux. (via sagemath 9.3)
7. Sympy 1.8 under Python 3.8.8 using Anaconda distribution on Ubuntu.
8. Mupad using Matlab 2021a with Symbolic Math Toolbox Version 8.7 under windows 10 (64 bit)

Maxima, Fricas and Giac/Xcas were called from inside SageMath. This was done using SageMath integrate command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly using Python.

1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or Hypergeometric₂F₁ functions. RootSum and RootOf are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	solved	Failed
Rubi	% 98.41 (62)	% 1.59 (1)
Mathematica	% 100.00 (63)	% 0.00 (0)
Maple	% 92.06 (58)	% 7.94 (5)
Maxima	% 71.43 (45)	% 28.57 (18)
Fricas	% 100.00 (63)	% 0.00 (0)
Sympy	% 44.44 (28)	% 55.56 (35)
Giac	% 49.21 (31)	% 50.79 (32)
Mupad	% 50.79 (32)	% 49.21 (31)

Table 1.1: Percentage solved for each CAS

The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> 1. antiderivative contains a hypergeometric function and the optimal antiderivative does not. 2. antiderivative contains a special function and the optimal antiderivative does not. 3. antiderivative contains the imaginary unit and the optimal antiderivative does not.
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

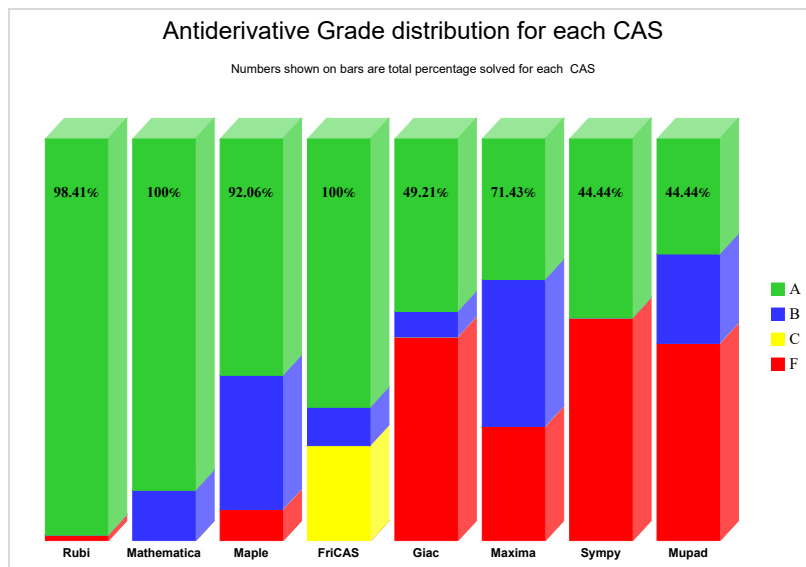
Table 1.2: Description of grading applied to integration result

Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

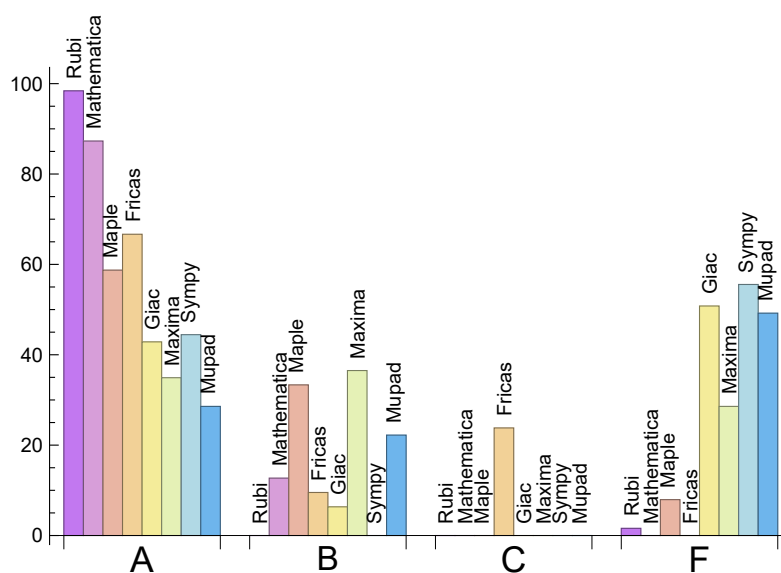
System	% A grade	% B grade	% C grade	% F grade
Rubi	98.41	0.00	0.00	1.59
Mathematica	87.30	12.70	0.00	0.00
Maple	58.73	33.33	0.00	7.94
Maxima	34.92	36.51	0.00	28.57
Fricas	66.67	9.52	23.81	0.00
Sympy	44.44	0.00	0.00	55.56
Giac	42.86	6.35	0.00	50.79
Mupad	28.57	22.22	0.00	49.21

Table 1.3: Antiderivative Grade distribution of each CAS

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



The following table shows the distribution of the different types of failure for each CAS. There are 3 types of reasons why it can fail. The first is when CAS returns back the input within the time limit, which means it could not solve it. This is the typical normal failure F.

The second is due to time out. CAS could not solve the integral within the 3 minutes time limit which is assigned F(-1).

The third is due to an exception generated. Assigned F(-2). This most likely indicates an interface problem between sagemath and the CAS (applicable only to FriCAS, Maxima and Giac) or it could be an indication of an internal error in CAS. This type of error requires more investigations to determine the cause.

System	Number failed	Percentage normal failure	Percentage time-out failure	Percentage exception failure
Rubi	1	100.00 %	0.00 %	0.00 %
Mathematica	0	0.00 %	0.00 %	0.00 %
Maple	5	100.00 %	0.00 %	0.00 %
Maxima	18	27.78 %	22.22 %	50.00 %
Fricas	0	0.00 %	0.00 %	0.00 %
Sympy	35	100.00 %	0.00 %	0.00 %
Giac	32	87.50 %	12.50 %	0.00 %
Mupad	31	100.00 %	0.00 %	0.00 %

Table 1.4: Time and leaf size performance for each CAS

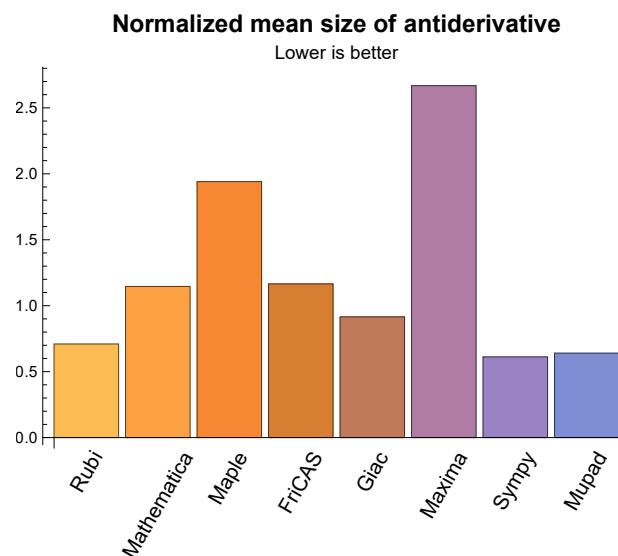
1.3 Performance

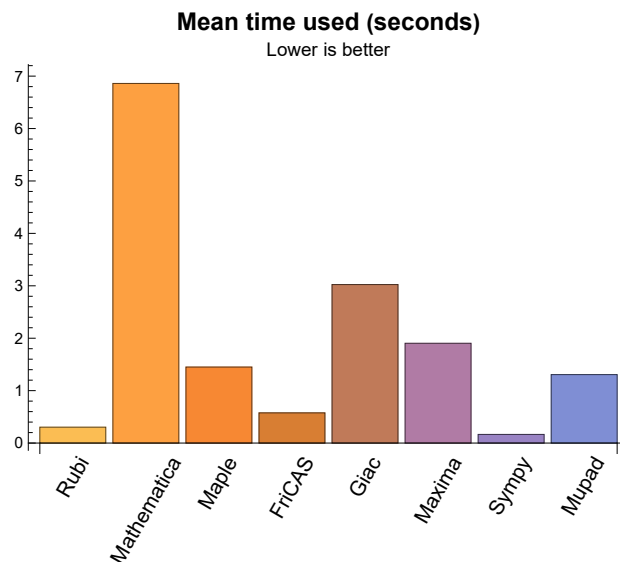
The table below summarizes the performance of each CAS system in terms of CPU time and leaf size of results.

System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.30	167.66	0.71	126.50	1.00
Mathematica	6.86	293.76	1.15	178.00	1.07
Maple	1.45	524.24	1.94	221.00	1.38
Maxima	1.90	728.58	2.67	214.00	1.70
Fricas	0.58	263.10	1.17	128.00	0.79
Sympy	0.16	133.68	0.61	0.00	0.00
Giac	3.02	173.68	0.92	0.00	0.00
Mupad	1.31	80.19	0.64	-1.00	-0.04

Table 1.5: Time and leaf size performance for each CAS

The following are bar charts for the normalized leafsize and time used columns from the above table.





1.4 list of integrals that has no closed form antiderivative

{4, 5, 9, 10, 14, 15, 34, 35, 42, 43, 47, 48, 52, 53, 57, 58, 62, 63}

1.5 list of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

Mupad {}

1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

Rubi {}

Mathematica {7, 11, 13, 21, 27, 28, 32, 33, 44, 45, 49, 50, 59, 61}

Maple Verification phase not implemented yet.

Maxima Verification phase not implemented yet.

Fricas Verification phase not implemented yet.

Sympy Verification phase not implemented yet.

Giac Verification phase not implemented yet.

Mupad Verification phase not implemented yet.

1.7 Timing

The command `AbsoluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of _int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call has completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out is not counted in the final statistics.

1.8 Verification

A verification phase was applied on the result of integration for Rubi and Mathematica. Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative produced was correct.

Verification phase has 3 minutes time out. An integral whose result was not verified could still be correct. Further investigation is needed on those integrals which failed verifications. Such integrals are marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

1.9 Important notes about some of the results

1.9.1 Important note about Maxima results

Since these integrals are run in a batch mode, using an automated script, and by using `sagemath` (SageMath uses Maxima), then any integral where Maxima needs an interactive response from the user to answer a question during evaluation of the integral in order to complete the integration, will fail and is counted as failed.

The exception raised is `ValueError`. Therefore Maxima result below is lower than what could result if Maxima was run directly and each question Maxima asks was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the Timofeev test file, there were about 14 such integrals out of total 705, or about 2 percent. This percentage can be higher or lower depending on the specific input test file.

Such integrals can be identified by looking at the output of the integration in each section for Maxima. The exception message will indicate if the error is due to the interactive question being asked or not.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
```

```
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath loading of Maxima `abs_integrate` was found to cause some problem. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

1.9.2 Important note about FriCAS and Giac/X-CAS results

There are Few integrals which failed due to SageMath not able to translate the result back to SageMath syntax and not because these CAS system were not able to do the integrations.

These will fail With error `Exception raised: NotImplementedError`

The number of such cases seems to be very small. About 1 or 2 percent of all integrals.

Hopefully the next version of SageMath will have complete translation of FriCAS and XCAS syntax and I will re-run all the tests again when this happens.

1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi and Maple, the buildin system function `LeafSize` is used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special buildin function for this purpose at this time. Therefore the leaf size for Fricas and Sympy and Giac antiderivatives is determined using the following function, thanks to user `slelievre` at https://ask.sagemath.org/question/57123/could-we-have-a-leaf_count-function-in-base-sagemath/

```
def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)
```

For Sympy, which is called directly from Python, the following code is used to obtain the leafsize of its result

```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount = 1
```

1.9.4 Important note about Mupad results

Matlab's symbolic toolbox does not have a leaf count function to measure the size of the antiderivative, Maple was used to determine the leaf size of Mupad output by post processing.

Currently no grading of the antiderivative for Mupad is implemented. If it can integrate the problem, it was assigned a B grade automatically as a placeholder. In the future, when grading function is implemented for Mupad, the tests will be rerun again.

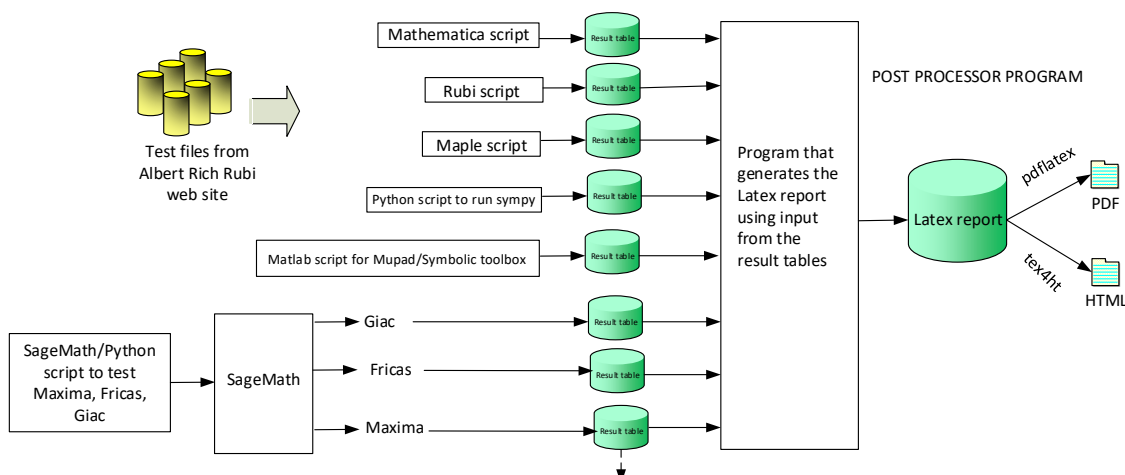
The following is an example of using Matlab's symbolic toolbox (Mupad) to solve an integral

```
integrand = evalin(symengine, 'cos(x)*sin(x)')
the_variable = evalin(symengine, 'x')
anti = int(integrand, the_variable)
```

Which gives $\sin(x)^2/2$

1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



One record (line) per one integral result. The line is CSV comma separated. This is description of each record

1. integer. the problem number.
2. integer. 0 for failed, 1 for passed, -1 for timeout, -2 for CAS specific exception. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntax.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"
- The following field present only in Rubi and Mathematica Tables*
13. integer. 1 if result was verified or 0 if not verified.
- The following fields present only in Rubi Tables*
14. integer. Number of rules used.
15. integer. Integrand leaf size.
16. real number. Ratio of field 14 over field 15
17. integer. 1 if result was verified or 0 if not verified.
18. String of form "{n,n,..}" which is list of the rules used by Rubi

High level overview of the CAS independent integration test build system

Chapter 2

detailed summary tables of results

2.1 List of integrals sorted by grade for each CAS

2.1.1 Rubi

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63 }

B grade: { }

C grade: { }

F grade: { 17 }

2.1.2 Mathematica

A grade: { 1, 2, 3, 4, 5, 6, 8, 9, 10, 11, 12, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 37, 38, 39, 40, 41, 42, 43, 46, 47, 48, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 62, 63 }

B grade: { 7, 13, 36, 44, 45, 49, 50, 61 }

C grade: { }

F grade: { }

2.1.3 Maple

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 21, 22, 23, 27, 28, 32, 33, 34, 35, 41, 42, 43, 46, 47, 48, 51, 52, 53, 57, 58, 62, 63 }

B grade: { 18, 19, 20, 24, 25, 26, 29, 30, 31, 39, 40, 44, 45, 49, 50, 54, 55, 56, 59, 60, 61 }

C grade: { }

F grade: { 16, 17, 36, 37, 38 }

2.1.4 Maxima

A grade: { 4, 5, 9, 10, 14, 15, 21, 22, 23, 27, 28, 32, 33, 34, 35, 41, 42, 43, 47, 48, 52, 53 }

B grade: { 1, 2, 3, 6, 7, 8, 11, 12, 13, 39, 40, 44, 45, 46, 49, 50, 51, 54, 55, 56, 59, 60, 61 }

C grade: { }

F grade: { 16, 17, 18, 19, 20, 24, 25, 26, 29, 30, 31, 36, 37, 38, 57, 58, 62, 63 }

2.1.5 FriCAS

A grade: { 4, 5, 8, 9, 10, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 42, 43, 46, 47, 48, 51, 52, 53, 57, 58, 62, 63 }

B grade: { 3, 7, 13, 41, 56, 61 }

C grade: { 1, 2, 6, 11, 12, 39, 40, 44, 45, 49, 50, 54, 55, 59, 60 }

F grade: { }

2.1.6 Sympy

A grade: { 4, 5, 8, 9, 10, 14, 15, 18, 19, 20, 24, 25, 26, 29, 30, 31, 34, 35, 42, 43, 47, 48, 52, 53, 57, 58, 62, 63 }

B grade: { }

C grade: { }

F grade: { 1, 2, 3, 6, 7, 11, 12, 13, 16, 17, 21, 22, 23, 27, 28, 32, 33, 36, 37, 38, 39, 40, 41, 44, 45, 46, 49, 50, 51, 54, 55, 56, 59, 60, 61 }

2.1.7 Giac

A grade: { 4, 5, 9, 10, 14, 15, 18, 19, 20, 21, 24, 25, 26, 27, 29, 30, 31, 34, 35, 42, 43, 47, 48, 52, 53, 57, 62 }

B grade: { 8, 22, 23, 32 }

C grade: { }

F grade: { 1, 2, 3, 6, 7, 11, 12, 13, 16, 17, 28, 33, 36, 37, 38, 39, 40, 41, 44, 45, 46, 49, 50, 51, 54, 55, 56, 58, 59, 60, 61, 63 }

2.1.8 Mupad

A grade: { 4, 5, 9, 10, 14, 15, 34, 35, 42, 43, 47, 48, 52, 53, 57, 58, 62, 63 }

B grade: { 3, 8, 16, 17, 18, 19, 20, 24, 25, 26, 29, 30, 31, 41 }

C grade: { }

F grade: { 1, 2, 6, 7, 11, 12, 13, 21, 22, 23, 27, 28, 32, 33, 36, 37, 38, 39, 40, 44, 45, 46, 49, 50, 51, 54, 55, 56, 59, 60, 61 }

2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table, the column **normalized size** is defined as $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$

Problem 1	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	106	106	106	125	241	286	0	0	-1
normalized size	1	1.00	1.00	1.18	2.27	2.70	0.00	0.00	-0.01
time (sec)	N/A	0.155	0.043	0.259	1.046	0.551	0.000	0.000	0.000
Problem 2	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	77	103	162	200	0	0	-1
normalized size	1	1.00	1.00	1.34	2.10	2.60	0.00	0.00	-0.01
time (sec)	N/A	0.134	0.010	0.250	1.189	0.568	0.000	0.000	0.000
Problem 3	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	54	78	92	122	0	0	129
normalized size	1	1.00	1.00	1.44	1.70	2.26	0.00	0.00	2.39
time (sec)	N/A	0.081	0.006	0.243	1.145	0.553	0.000	0.000	2.464
Problem 4	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.015	2.127	0.300	0.000	0.575	0.000	0.000	0.000
Problem 5	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.016	3.013	0.296	0.000	0.468	0.000	0.000	0.000

Problem 6	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	115	133	640	225	0	0	-1
normalized size	1	1.00	1.17	1.36	6.53	2.30	0.00	0.00	-0.01
time (sec)	N/A	0.167	0.789	0.361	2.988	0.641	0.000	0.000	0.000
Problem 7	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	73	73	189	108	256	144	0	0	-1
normalized size	1	1.00	2.59	1.48	3.51	1.97	0.00	0.00	-0.01
time (sec)	N/A	0.112	6.185	0.348	1.347	0.534	0.000	0.000	0.000
Problem 8	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	A	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	43	29	214	38	41	182	35
normalized size	1	1.00	1.43	0.97	7.13	1.27	1.37	6.07	1.17
time (sec)	N/A	0.023	0.182	0.258	0.931	0.572	0.179	1.263	0.113
Problem 9	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	15	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.07
time (sec)	N/A	0.028	2.762	0.365	0.000	0.454	0.000	0.000	0.000
Problem 10	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	15	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.07
time (sec)	N/A	0.030	2.978	0.363	0.000	0.581	0.000	0.000	0.000
Problem 11	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	C	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	205	205	359	251	1203	342	0	0	-1
normalized size	1	1.00	1.75	1.22	5.87	1.67	0.00	0.00	-0.00
time (sec)	N/A	0.292	6.672	0.319	2.581	0.570	0.000	0.000	0.000

Problem 12	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	128	128	172	180	740	240	0	0	-1
normalized size	1	1.00	1.34	1.41	5.78	1.88	0.00	0.00	-0.01
time (sec)	N/A	0.180	3.143	0.289	1.180	0.536	0.000	0.000	0.000
Problem 13	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	A	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	210	122	388	146	0	0	-1
normalized size	1	1.00	2.33	1.36	4.31	1.62	0.00	0.00	-0.01
time (sec)	N/A	0.103	6.149	0.217	3.041	0.495	0.000	0.000	0.000
Problem 14	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	15	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.07
time (sec)	N/A	0.027	5.121	1.208	0.000	0.464	0.000	0.000	0.000
Problem 15	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	15	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.07
time (sec)	N/A	0.028	3.422	1.361	0.000	0.573	0.000	0.000	0.000
Problem 16	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	0	0	16	0	0	50
normalized size	1	1.00	1.00	0.00	0.00	0.89	0.00	0.00	2.78
time (sec)	N/A	0.123	0.965	0.873	0.000	0.610	0.000	0.000	3.123
Problem 17	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	F	A	F	F	A	F	F	B
verified	N/A	N/A	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	17	0	17	0	0	15	0	0	45
normalized size	1	0.00	1.00	0.00	0.00	0.88	0.00	0.00	2.65
time (sec)	N/A	0.035	0.603	1.057	0.000	0.861	0.000	0.000	4.173

Problem 18	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	189	189	278	1061	0	162	262	193	423
normalized size	1	1.00	1.47	5.61	0.00	0.86	1.39	1.02	2.24
time (sec)	N/A	0.199	0.705	0.646	0.000	0.506	0.384	0.671	3.559
Problem 19	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	137	137	178	509	0	104	168	123	241
normalized size	1	1.00	1.30	3.72	0.00	0.76	1.23	0.90	1.76
time (sec)	N/A	0.123	0.403	0.618	0.000	0.563	0.308	0.793	3.078
Problem 20	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	96	187	0	55	97	65	105
normalized size	1	1.00	1.14	2.23	0.00	0.65	1.15	0.77	1.25
time (sec)	N/A	0.054	0.437	0.555	0.000	0.521	0.240	0.703	2.815
Problem 21	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	161	161	166	204	110	49	0	142	-1
normalized size	1	1.00	1.03	1.27	0.68	0.30	0.00	0.88	-0.01
time (sec)	N/A	0.277	0.355	0.513	0.795	0.575	0.000	0.776	0.000
Problem 22	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	168	168	224	285	117	84	0	1099	-1
normalized size	1	1.00	1.33	1.70	0.70	0.50	0.00	6.54	-0.01
time (sec)	N/A	0.240	0.853	0.474	0.858	0.581	0.000	74.992	0.000
Problem 23	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	227	227	285	358	156	128	0	542	-1
normalized size	1	1.00	1.26	1.58	0.69	0.56	0.00	2.39	-0.00
time (sec)	N/A	0.322	1.201	0.491	1.051	0.745	0.000	0.876	0.000

Problem 24	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	270	270	473	2070	0	262	666	383	289
normalized size	1	1.00	1.75	7.67	0.00	0.97	2.47	1.42	1.07
time (sec)	N/A	0.293	1.380	0.869	0.000	0.536	0.577	0.948	3.231
Problem 25	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	202	202	282	968	0	160	420	227	183
normalized size	1	1.00	1.40	4.79	0.00	0.79	2.08	1.12	0.91
time (sec)	N/A	0.208	0.888	0.751	0.000	0.638	0.447	1.054	2.987
Problem 26	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	151	151	130	350	0	78	228	107	103
normalized size	1	1.00	0.86	2.32	0.00	0.52	1.51	0.71	0.68
time (sec)	N/A	0.142	0.594	0.679	0.000	0.610	0.341	2.032	2.768
Problem 27	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	305	305	211	382	190	80	0	420	-1
normalized size	1	1.00	0.69	1.25	0.62	0.26	0.00	1.38	-0.00
time (sec)	N/A	0.772	0.523	0.572	0.839	0.557	0.000	1.136	0.000
Problem 28	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-1)	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	436	436	467	536	210	140	0	0	-1
normalized size	1	1.00	1.07	1.23	0.48	0.32	0.00	0.00	-0.00
time (sec)	N/A	0.739	1.610	0.568	1.077	0.438	0.000	0.000	0.000
Problem 29	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	396	396	667	3404	0	362	949	573	411
normalized size	1	1.00	1.68	8.60	0.00	0.91	2.40	1.45	1.04
time (sec)	N/A	0.404	2.739	0.930	0.000	0.611	0.916	2.326	3.851

Problem 30	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	294	294	405	1525	0	216	592	331	263
normalized size	1	1.00	1.38	5.19	0.00	0.73	2.01	1.13	0.89
time (sec)	N/A	0.265	1.805	0.892	0.000	0.524	0.702	2.564	3.375
Problem 31	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F(-2)	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	209	209	205	527	0	103	320	151	146
normalized size	1	1.00	0.98	2.52	0.00	0.49	1.53	0.72	0.70
time (sec)	N/A	0.264	0.912	0.849	0.000	0.704	0.516	2.129	3.030
Problem 32	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	B	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	449	449	336	560	270	111	0	846	-1
normalized size	1	1.00	0.75	1.25	0.60	0.25	0.00	1.88	-0.00
time (sec)	N/A	1.783	0.802	0.615	3.022	0.439	0.000	1.464	0.000
Problem 33	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F(-1)	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	712	712	833	787	294	192	0	0	-1
normalized size	1	1.00	1.17	1.11	0.41	0.27	0.00	0.00	-0.00
time (sec)	N/A	1.732	3.157	0.630	4.084	0.447	0.000	0.000	0.000
Problem 34	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	26	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.050	39.441	0.404	0.000	0.523	0.000	0.000	0.000
Problem 35	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	24	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.028	15.611	0.560	0.000	0.574	0.000	0.000	0.000

Problem 36	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	98	98	205	0	0	84	0	0	-1
normalized size	1	1.00	2.09	0.00	0.00	0.86	0.00	0.00	-0.01
time (sec)	N/A	0.123	1.367	0.831	0.000	0.458	0.000	0.000	0.000
Problem 37	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	171	171	192	0	0	140	0	0	-1
normalized size	1	1.00	1.12	0.00	0.00	0.82	0.00	0.00	-0.01
time (sec)	N/A	0.184	48.069	0.914	0.000	0.603	0.000	0.000	0.000
Problem 38	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	251	251	269	0	0	192	0	0	-1
normalized size	1	1.00	1.07	0.00	0.00	0.76	0.00	0.00	-0.00
time (sec)	N/A	0.242	68.698	1.030	0.000	0.619	0.000	0.000	0.000
Problem 39	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	152	152	255	481	665	498	0	0	-1
normalized size	1	1.00	1.68	3.16	4.38	3.28	0.00	0.00	-0.01
time (sec)	N/A	0.251	0.358	0.519	3.412	0.699	0.000	0.000	0.000
Problem 40	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	191	295	369	315	0	0	-1
normalized size	1	1.00	1.66	2.57	3.21	2.74	0.00	0.00	-0.01
time (sec)	N/A	0.208	0.132	0.434	1.233	0.559	0.000	0.000	0.000
Problem 41	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	87	143	130	160	0	0	161
normalized size	1	1.00	1.04	1.70	1.55	1.90	0.00	0.00	1.92
time (sec)	N/A	0.119	0.015	0.393	0.748	0.551	0.000	0.000	3.220

Problem 42	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	21	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.028	2.134	0.757	0.000	0.464	0.000	0.000	0.000
Problem 43	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	21	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.027	6.138	0.779	0.000	0.527	0.000	0.000	0.000
Problem 44	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	C	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	300	300	1326	919	2521	757	0	0	-1
normalized size	1	1.00	4.42	3.06	8.40	2.52	0.00	0.00	-0.00
time (sec)	N/A	0.522	8.039	0.818	2.787	0.655	0.000	0.000	0.000
Problem 45	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	C	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	229	229	649	542	1269	448	0	0	-1
normalized size	1	1.00	2.83	2.37	5.54	1.96	0.00	0.00	-0.00
time (sec)	N/A	0.412	7.185	0.678	1.287	0.505	0.000	0.000	0.000
Problem 46	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	136	136	200	238	529	219	0	0	-1
normalized size	1	1.00	1.47	1.75	3.89	1.61	0.00	0.00	-0.01
time (sec)	N/A	0.190	2.321	0.638	0.817	0.535	0.000	0.000	0.000
Problem 47	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.053	20.272	2.697	0.000	0.624	0.000	0.000	0.000

Problem 48	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.051	15.691	3.307	0.000	0.479	0.000	0.000	0.000
Problem 49	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	C	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	612	612	2572	1882	6819	1175	0	0	-1
normalized size	1	1.00	4.20	3.08	11.14	1.92	0.00	0.00	-0.00
time (sec)	N/A	0.982	8.476	1.007	23.828	0.541	0.000	0.000	0.000
Problem 50	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	C	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	436	436	1846	1090	3396	686	0	0	-1
normalized size	1	1.00	4.23	2.50	7.79	1.57	0.00	0.00	-0.00
time (sec)	N/A	0.720	7.848	0.842	3.978	0.535	0.000	0.000	0.000
Problem 51	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	B	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	277	277	277	493	1327	327	0	0	-1
normalized size	1	1.00	1.00	1.78	4.79	1.18	0.00	0.00	-0.00
time (sec)	N/A	0.338	3.686	0.769	1.677	0.631	0.000	0.000	0.000
Problem 52	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.053	14.572	4.502	0.000	0.948	0.000	0.000	0.000
Problem 53	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.050	20.110	6.923	0.000	0.516	0.000	0.000	0.000

Problem 54	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	243	243	297	1450	977	1183	0	0	-1
normalized size	1	1.00	1.22	5.97	4.02	4.87	0.00	0.00	-0.00
time (sec)	N/A	0.334	2.315	1.184	1.607	0.540	0.000	0.000	0.000
Problem 55	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	181	181	236	922	712	836	0	0	-1
normalized size	1	1.00	1.30	5.09	3.93	4.62	0.00	0.00	-0.01
time (sec)	N/A	0.272	1.861	1.099	1.218	1.222	0.000	0.000	0.000
Problem 56	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	125	125	177	462	399	533	0	0	-1
normalized size	1	1.00	1.42	3.70	3.19	4.26	0.00	0.00	-0.01
time (sec)	N/A	0.159	1.917	0.964	1.761	0.463	0.000	0.000	0.000
Problem 57	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	F(-1)	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.062	1.971	1.720	0.000	0.643	0.000	0.000	0.000
Problem 58	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	F(-1)	A	A	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.058	4.976	3.202	0.000	0.491	0.000	0.000	0.000
Problem 59	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	C	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	848	848	1673	3488	4668	2535	0	0	-1
normalized size	1	1.00	1.97	4.11	5.50	2.99	0.00	0.00	-0.00
time (sec)	N/A	2.004	10.850	1.346	8.203	0.688	0.000	0.000	0.000

Problem 60	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	B	C	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	654	654	714	2160	2558	1578	0	0	-1
normalized size	1	1.00	1.09	3.30	3.91	2.41	0.00	0.00	-0.00
time (sec)	N/A	1.537	9.597	1.228	4.428	0.599	0.000	0.000	0.000

Problem 61	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	B	B	B	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	214	214	745	999	1164	849	0	0	-1
normalized size	1	1.00	3.48	4.67	5.44	3.97	0.00	0.00	-0.00
time (sec)	N/A	0.275	7.075	1.146	1.494	0.588	0.000	0.000	0.000

Problem 62	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	F(-1)	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.061	19.524	10.733	0.000	0.447	0.000	0.000	0.000

Problem 63	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	F(-1)	A	A	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	23	0	0	0	0	0	0	0	-1
normalized size	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.04
time (sec)	N/A	0.059	19.415	18.371	0.000	0.457	0.000	0.000	0.000

2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio $\frac{\text{number of rules}}{\text{integrand size}}$ is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [11] had the largest ratio of [.8333]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	6	6	1.00	10	0.600
2	A	5	5	1.00	10	0.500
3	A	4	4	1.00	8	0.500
4	A	0	0	0.00	0	0.000
5	A	0	0	0.00	0	0.000
6	A	7	7	1.00	12	0.583
7	A	6	6	1.00	12	0.500
8	A	3	3	1.00	10	0.300
9	A	0	0	0.00	0	0.000
10	A	0	0	0.00	0	0.000
11	A	13	10	1.00	12	0.833
12	A	9	8	1.00	12	0.667
13	A	7	7	1.00	10	0.700
14	A	0	0	0.00	0	0.000
15	A	0	0	0.00	0	0.000
16	A	2	1	1.00	45	0.022
17	F	0	0	N/A	0	N/A
18	A	5	3	1.00	23	0.130
19	A	4	3	1.00	23	0.130
20	A	3	3	1.00	21	0.143
21	A	7	4	1.00	23	0.174
22	A	7	4	1.00	23	0.174
23	A	8	5	1.00	23	0.217
24	A	10	3	1.00	23	0.130
25	A	8	3	1.00	23	0.130
26	A	7	3	1.00	21	0.143
27	A	21	5	1.00	23	0.217
28	A	24	7	1.00	23	0.304
29	A	14	3	1.00	23	0.130
30	A	11	3	1.00	23	0.130
31	A	11	3	1.00	21	0.143
32	A	53	7	1.00	23	0.304
33	A	60	9	1.00	23	0.391
34	A	0	0	0.00	0	0.000
35	A	0	0	0.00	0	0.000

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
36	A	2	2	1.00	23	0.087
37	A	4	2	1.00	23	0.087
38	A	5	2	1.00	23	0.087
39	A	8	7	1.00	18	0.389
40	A	7	6	1.00	18	0.333
41	A	6	5	1.00	16	0.312
42	A	0	0	0.00	0	0.000
43	A	0	0	0.00	0	0.000
44	A	15	9	1.00	20	0.450
45	A	13	10	1.00	20	0.500
46	A	9	7	1.00	18	0.389
47	A	0	0	0.00	0	0.000
48	A	0	0	0.00	0	0.000
49	A	28	11	1.00	20	0.550
50	A	22	11	1.00	20	0.550
51	A	16	9	1.00	18	0.500
52	A	0	0	0.00	0	0.000
53	A	0	0	0.00	0	0.000
54	A	6	6	1.00	20	0.300
55	A	5	5	1.00	20	0.250
56	A	4	4	1.00	18	0.222
57	A	0	0	0.00	0	0.000
58	A	0	0	0.00	0	0.000
59	A	21	9	1.00	20	0.450
60	A	18	10	1.00	20	0.500
61	A	5	5	1.00	18	0.278
62	A	0	0	0.00	0	0.000
63	A	0	0	0.00	0	0.000

Chapter 3

Listing of integrals

3.1 $\int x^3 \tan(a + bx) dx$

Optimal. Leaf size=106

$$-\frac{3i\text{Li}_4(-e^{2i(a+bx)})}{4b^4} - \frac{3x\text{Li}_3(-e^{2i(a+bx)})}{2b^3} + \frac{3ix^2\text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^4}{4}$$

[Out] $1/4*I*x^4-x^3*\ln(1+\exp(2*I*(b*x+a)))/b+3/2*I*x^2*\text{polylog}(2,-\exp(2*I*(b*x+a)))/b^2-3/2*x*\text{polylog}(3,-\exp(2*I*(b*x+a)))/b^3-3/4*I*\text{polylog}(4,-\exp(2*I*(b*x+a)))/b^4$

Rubi [A] time = 0.16, antiderivative size = 106, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {3719, 2190, 2531, 6609, 2282, 6589}

$$\frac{3ix^2\text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{3x\text{Li}_3(-e^{2i(a+bx)})}{2b^3} - \frac{3i\text{Li}_4(-e^{2i(a+bx)})}{4b^4} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^4}{4}$$

Antiderivative was successfully verified.

[In] Int[x^3*Tan[a + b*x], x]

[Out] $(I/4)*x^4 - (x^3*\text{Log}[1 + E^((2*I)*(a + b*x))])/b + (((3*I)/2)*x^2*\text{PolyLog}[2, -E^((2*I)*(a + b*x))])/b^2 - (3*x*\text{PolyLog}[3, -E^((2*I)*(a + b*x))])/(2*b^3) - (((3*I)/4)*\text{PolyLog}[4, -E^((2*I)*(a + b*x))])/b^4$

Rule 2190

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^((n_)*((c_) + (d_)*(x_))^(m_)))/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^((n_))), x_Symbol] := Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2531

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^((n_)))*((f_) + (g_)*(x_))^(m_)], x_Symbol] := -Simp[(((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x))))]

)))^n]]/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n]], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 6589

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6609

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^(c_.)*((a_.) + (b_.)*(x_)))^(p_.)], x_Symbol] := Simp[(e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
 \int x^3 \tan(a + bx) dx &= \frac{ix^4}{4} - 2i \int \frac{e^{2i(a+bx)} x^3}{1 + e^{2i(a+bx)}} dx \\
 &= \frac{ix^4}{4} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{3 \int x^2 \log(1 + e^{2i(a+bx)}) dx}{b} \\
 &= \frac{ix^4}{4} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{3ix^2 \text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{(3i) \int x \text{Li}_2(-e^{2i(a+bx)}) dx}{b^2} \\
 &= \frac{ix^4}{4} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{3ix^2 \text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{3x \text{Li}_3(-e^{2i(a+bx)})}{2b^3} + \frac{3 \int \text{Li}_3(-e^{2i(a+bx)})}{2b^3} \\
 &= \frac{ix^4}{4} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{3ix^2 \text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{3x \text{Li}_3(-e^{2i(a+bx)})}{2b^3} - \frac{(3i) \text{Subst}\left(\int \frac{\text{Li}_3(-)}{x}\right)}{4b} \\
 &= \frac{ix^4}{4} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{3ix^2 \text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{3x \text{Li}_3(-e^{2i(a+bx)})}{2b^3} - \frac{3i \text{Li}_4(-e^{2i(a+bx)})}{4b^4}
 \end{aligned}$$

Mathematica [A] time = 0.04, size = 106, normalized size = 1.00

$$-\frac{3i \text{Li}_4(-e^{2i(a+bx)})}{4b^4} - \frac{3x \text{Li}_3(-e^{2i(a+bx)})}{2b^3} + \frac{3ix^2 \text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^4}{4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*Tan[a + b*x], x]

[Out] (I/4)*x^4 - (x^3*Log[1 + E^((2*I)*(a + b*x))])/b + (((3*I)/2)*x^2*PolyLog[2, -E^((2*I)*(a + b*x))])/b^2 - (3*x*PolyLog[3, -E^((2*I)*(a + b*x))])/(2*b^3) - (((3*I)/4)*PolyLog[4, -E^((2*I)*(a + b*x))])/b^4

fricas [C] time = 0.55, size = 286, normalized size = 2.70

$$4b^3x^3 \log\left(-\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 4b^3x^3 \log\left(-\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 6ib^2x^2 \operatorname{Li}_2\left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1\right) - 6ib^2x^2 \operatorname{Li}_2\left(\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a),x, algorithm="fricas")

[Out] $-1/8*(4*b^3*x^3*\log(-2*(I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)) + 4*b^3*x^3*\log(-2*(-I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)) + 6*I*b^2*x^2*\operatorname{dilog}(2*(I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1) + 1) - 6*I*b^2*x^2*\operatorname{dilog}(2*(-I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1) + 1) + 6*b*x*\operatorname{polylog}(3, (\tan(b*x + a)^2 + 2*I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)) + 6*b*x*\operatorname{polylog}(3, (\tan(b*x + a)^2 - 2*I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)) - 3*I*\operatorname{polylog}(4, (\tan(b*x + a)^2 + 2*I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)) + 3*I*\operatorname{polylog}(4, (\tan(b*x + a)^2 - 2*I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)))/b^4$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^3 \tan(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a),x, algorithm="giac")

[Out] integrate(x^3*tan(b*x + a), x)

maple [A] time = 0.26, size = 125, normalized size = 1.18

$$\frac{ix^4}{4} + \frac{2ia^3x}{b^3} + \frac{3ia^4}{2b^4} - \frac{x^3 \ln(e^{2i(bx+a)} + 1)}{b} + \frac{3ix^2 \operatorname{polylog}(2, -e^{2i(bx+a)})}{2b^2} - \frac{3x \operatorname{polylog}(3, -e^{2i(bx+a)})}{2b^3} - \frac{3i \operatorname{polylog}(4, -e^{2i(bx+a)})}{4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*tan(b*x+a),x)

[Out] $1/4*I*x^4+2*I/b^3*a^3*x+3/2*I/b^4*a^4-x^3*\ln(\exp(2*I*(b*x+a))+1)/b+3/2*I*x^2*\operatorname{polylog}(2, -\exp(2*I*(b*x+a)))/b^2-3/2*x*\operatorname{polylog}(3, -\exp(2*I*(b*x+a)))/b^3-3/4*I*\operatorname{polylog}(4, -\exp(2*I*(b*x+a)))/b^4-2/b^4*a^3*\ln(\exp(I*(b*x+a)))$

maxima [B] time = 1.05, size = 241, normalized size = 2.27

$$-3i(bx+a)^4 + 12i(bx+a)^3a - 18i(bx+a)^2a^2 + 12a^3 \log(\sec(bx+a)) + (16i(bx+a)^3 - 36i(bx+a)^2a + 36i(bx+a)a^2) \operatorname{arctan}(\sin(2bx+2a), \cos(2bx+2a)+1) + (-24i(bx+a)^2 + 36i(bx+a)a - 18ia^2) \operatorname{dilog}(-e^{(2Ibx+2Ia)}) + 2*(4*(bx+a)^3 - 9*(bx+a)^2a + 9*(bx+a)a^2) \log(\cos(2bx+2a)^2 + \sin(2bx+2a)^2 + 2\cos(2bx+2a)+1) + 6*(4bx+a) \operatorname{polylog}(3, -e^{(2Ibx+2Ia)}) + 12I \operatorname{polylog}(4, -e^{(2Ibx+2Ia)})/b^4$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a),x, algorithm="maxima")

[Out] $-1/12*(-3*I*(b*x + a)^4 + 12*I*(b*x + a)^3*a - 18*I*(b*x + a)^2*a^2 + 12*a^3*\log(\sec(b*x + a)) + (16*I*(b*x + a)^3 - 36*I*(b*x + a)^2*a + 36*I*(b*x + a)*a^2)*\operatorname{arctan}(\sin(2*b*x + 2*a), \cos(2*b*x + 2*a) + 1) + (-24*I*(b*x + a)^2 + 36*I*(b*x + a)*a - 18*I*a^2)*\operatorname{dilog}(-e^{(2*I*b*x + 2*I*a)}) + 2*(4*(b*x + a)^3 - 9*(b*x + a)^2*a + 9*(b*x + a)*a^2)*\log(\cos(2*b*x + 2*a)^2 + \sin(2*b*x + 2*a)^2 + 2*\cos(2*b*x + 2*a) + 1) + 6*(4*b*x + a)*\operatorname{polylog}(3, -e^{(2*I*b*x + 2*I*a)}) + 12*I*\operatorname{polylog}(4, -e^{(2*I*b*x + 2*I*a)})/b^4$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^3 \tan(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*tan(a + b*x), x)
```

```
[Out] int(x^3*tan(a + b*x), x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int x^3 \tan(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*tan(b*x+a), x)
```

```
[Out] Integral(x**3*tan(a + b*x), x)
```

3.2 $\int x^2 \tan(a + bx) dx$

Optimal. Leaf size=77

$$-\frac{\text{Li}_3(-e^{2i(a+bx)})}{2b^3} + \frac{ix\text{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^3}{3}$$

[Out] $1/3*I*x^3 - x^2*\ln(1+\exp(2*I*(b*x+a)))/b + I*x*\text{polylog}(2, -\exp(2*I*(b*x+a)))/b^2 - 1/2*\text{polylog}(3, -\exp(2*I*(b*x+a)))/b^3$

Rubi [A] time = 0.13, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3719, 2190, 2531, 2282, 6589}

$$\frac{ix\text{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{\text{Li}_3(-e^{2i(a+bx)})}{2b^3} - \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^3}{3}$$

Antiderivative was successfully verified.

[In] Int[x^2*Tan[a + b*x], x]

[Out] $(I/3)*x^3 - (x^2*\text{Log}[1 + E^{((2*I)*(a + b*x))}])/b + (I*x*\text{PolyLog}[2, -E^{((2*I)*(a + b*x))}])/b^2 - \text{PolyLog}[3, -E^{((2*I)*(a + b*x))}]/(2*b^3)$

Rule 2190

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] :> Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n]/a)]/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n]/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] :> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)^v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2531

Int[Log[1 + (e_)*((F_)^(c_)*((a_) + (b_)*(x_)))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] :> -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)]/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n]], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

Int[(((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] :> Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[(((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 6589

Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_))^(p_)]/((d_) + (e_)*(x_)), x_Symbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned}
\int x^2 \tan(a + bx) dx &= \frac{ix^3}{3} - 2i \int \frac{e^{2i(a+bx)} x^2}{1 + e^{2i(a+bx)}} dx \\
&= \frac{ix^3}{3} - \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} + \frac{2 \int x \log(1 + e^{2i(a+bx)}) dx}{b} \\
&= \frac{ix^3}{3} - \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{i \int \operatorname{Li}_2(-e^{2i(a+bx)}) dx}{b^2} \\
&= \frac{ix^3}{3} - \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{\operatorname{Subst}\left(\int \frac{\operatorname{Li}_2(-x)}{x} dx, x, e^{2i(a+bx)}\right)}{2b^3} \\
&= \frac{ix^3}{3} - \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{\operatorname{Li}_3(-e^{2i(a+bx)})}{2b^3}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 77, normalized size = 1.00

$$-\frac{\operatorname{Li}_3(-e^{2i(a+bx)})}{2b^3} + \frac{ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^3}{3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*Tan[a + b*x], x]

[Out] (I/3)*x^3 - (x^2*Log[1 + E^((2*I)*(a + b*x))])/b + (I*x*PolyLog[2, -E^((2*I)*(a + b*x))])/b^2 - PolyLog[3, -E^((2*I)*(a + b*x))]/(2*b^3)

fricas [C] time = 0.57, size = 200, normalized size = 2.60

$$\frac{2b^2x^2 \log\left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 2b^2x^2 \log\left(\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 2ibx \operatorname{Li}_2\left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1\right) - 2ibx \operatorname{Li}_2\left(\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1\right)}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a), x, algorithm="fricas")

[Out] -1/4*(2*b^2*x^2*log(-2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + 2*b^2*x^2*log(-2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + 2*I*b*x*dilog(2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) - 2*I*b*x*dilog(2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) + polylog(3, (tan(b*x + a)^2 + 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + polylog(3, (tan(b*x + a)^2 - 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)))/b^3

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a), x, algorithm="giac")

[Out] integrate(x^2*tan(b*x + a), x)

maple [A] time = 0.25, size = 103, normalized size = 1.34

$$\frac{ix^3}{3} - \frac{2ia^2x}{b^2} - \frac{4ia^3}{3b^3} - \frac{x^2 \ln(e^{2i(bx+a)} + 1)}{b} + \frac{ix \operatorname{polylog}(2, -e^{2i(bx+a)})}{b^2} - \frac{\operatorname{polylog}(3, -e^{2i(bx+a)})}{2b^3} + \frac{2a^2 \ln(e^{i(bx+a)})}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*tan(b*x+a),x)`

[Out] $\frac{1}{3}I*x^3 - \frac{2I}{b^2}a^2*x - \frac{4}{3}I/b^3*a^3 - x^2*\ln(\exp(2*I*(b*x+a))+1)/b + I*x*\text{polylog}(2, -\exp(2*I*(b*x+a)))/b^2 - \frac{1}{2}*\text{polylog}(3, -\exp(2*I*(b*x+a)))/b^3 + \frac{2}{b^3}a^2*\ln(\exp(I*(b*x+a)))$

maxima [B] time = 1.19, size = 162, normalized size = 2.10

$$\frac{-2i(bx+a)^3 + 6i(bx+a)^2a - 6ibx\text{Li}_2(-e^{(2ibx+2ia)}) - 6a^2\log(\sec(bx+a)) + (6i(bx+a)^2 - 12i(bx+a)a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*tan(b*x+a),x, algorithm="maxima")`

[Out] $-\frac{1}{6}*(-2I*(b*x+a)^3 + 6I*(b*x+a)^2*a - 6I*b*x*\text{dilog}(-e^{(2I*b*x+2I*a)}) - 6*a^2*\log(\sec(b*x+a)) + (6I*(b*x+a)^2 - 12I*(b*x+a)*a)*\arctan^2(\sin(2*b*x+2*a), \cos(2*b*x+2*a)+1) + 3*((b*x+a)^2 - 2*(b*x+a)*a)*\log(\cos(2*b*x+2*a)^2 + \sin(2*b*x+2*a)^2 + 2*\cos(2*b*x+2*a)+1) + 3*\text{polylog}(3, -e^{(2I*b*x+2I*a)}))/b^3$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^2 \tan(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*tan(a+b*x),x)`

[Out] `int(x^2*tan(a+b*x),x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*tan(b*x+a),x)`

[Out] `Integral(x**2*tan(a+b*x),x)`

3.3 $\int x \tan(a + bx) dx$

Optimal. Leaf size=54

$$\frac{i\text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{x \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^2}{2}$$

[Out] $1/2*I*x^2-x*\ln(1+\exp(2*I*(b*x+a)))/b+1/2*I*\text{polylog}(2,-\exp(2*I*(b*x+a)))/b^2$

Rubi [A] time = 0.08, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3719, 2190, 2279, 2391}

$$\frac{i\text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{x \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^2}{2}$$

Antiderivative was successfully verified.

[In] Int[x*Tan[a + b*x], x]

[Out] $(I/2)*x^2 - (x*\text{Log}[1 + E^((2*I)*(a + b*x))])/b + ((I/2)*\text{PolyLog}[2, -E^((2*I)*(a + b*x))])/b^2$

Rule 2190

```
Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/
((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] :> Simp
[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a]]/(b*f*g*n*Log[F]), x] - Di
st[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)
))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2279

```
Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_))))^(n_)], x_Symbol]
:> Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)
))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2391

```
Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] :> -Simp[PolyLog[2
, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 3719

```
Int[(((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] :> Simp[(
I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[(((c + d*x)^m*E^(2*I*(e
 + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rubi steps

$$\begin{aligned}
\int x \tan(a + bx) dx &= \frac{ix^2}{2} - 2i \int \frac{e^{2i(a+bx)} x}{1 + e^{2i(a+bx)}} dx \\
&= \frac{ix^2}{2} - \frac{x \log(1 + e^{2i(a+bx)})}{b} + \frac{\int \log(1 + e^{2i(a+bx)}) dx}{b} \\
&= \frac{ix^2}{2} - \frac{x \log(1 + e^{2i(a+bx)})}{b} - \frac{i \operatorname{Subst}\left(\int \frac{\log(1+x)}{x} dx, x, e^{2i(a+bx)}\right)}{2b^2} \\
&= \frac{ix^2}{2} - \frac{x \log(1 + e^{2i(a+bx)})}{b} + \frac{i \operatorname{Li}_2(-e^{2i(a+bx)})}{2b^2}
\end{aligned}$$

Mathematica [A] time = 0.01, size = 54, normalized size = 1.00

$$\frac{i \operatorname{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{x \log(1 + e^{2i(a+bx)})}{b} + \frac{ix^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[x*Tan[a + b*x], x]

[Out] (I/2)*x^2 - (x*Log[1 + E^((2*I)*(a + b*x))])/b + ((I/2)*PolyLog[2, -E^((2*I)*(a + b*x))])/b^2

fricas [B] time = 0.55, size = 122, normalized size = 2.26

$$\frac{2bx \log\left(-\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 2bx \log\left(-\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + i \operatorname{Li}_2\left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1\right) - i \operatorname{Li}_2\left(\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1\right)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a), x, algorithm="fricas")

[Out] -1/4*(2*b*x*log(-2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + 2*b*x*log(-2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + I*dilog(2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) - I*dilog(2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1))/b^2

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x \tan(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a), x, algorithm="giac")

[Out] integrate(x*tan(b*x + a), x)

maple [A] time = 0.24, size = 78, normalized size = 1.44

$$\frac{ix^2}{2} + \frac{2iax}{b} + \frac{ia^2}{b^2} - \frac{x \ln(e^{2i(bx+a)} + 1)}{b} + \frac{i \operatorname{polylog}(2, -e^{2i(bx+a)})}{2b^2} - \frac{2a \ln(e^{i(bx+a)})}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*tan(b*x+a), x)

[Out] 1/2*I*x^2+2*I/b*a*x+I/b^2*a^2-x*ln(exp(2*I*(b*x+a))+1)/b+1/2*I*polylog(2,-exp(2*I*(b*x+a)))/b^2-2/b^2*a*ln(exp(I*(b*x+a)))

maxima [B] time = 1.15, size = 92, normalized size = 1.70

$$\frac{-i b^2 x^2 + 2i b x \arctan(\sin(2 b x + 2 a), \cos(2 b x + 2 a) + 1) + b x \log(\cos(2 b x + 2 a)^2 + \sin(2 b x + 2 a)^2 + 2 \cos(2 b x + 2 a) + 1)}{2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a),x, algorithm="maxima")

[Out] -1/2*(-I*b^2*x^2 + 2*I*b*x*arctan2(sin(2*b*x + 2*a), cos(2*b*x + 2*a) + 1) + b*x*log(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1) - I*dilog(-e^(2*I*b*x + 2*I*a)))/b^2

mupad [B] time = 2.46, size = 129, normalized size = 2.39

$$\frac{\pi \ln(\cos(bx)) + \operatorname{polylog}\left(2, -e^{-a2i} e^{-bx2i}\right) 1i - \pi \ln\left(e^{-a2i} e^{-bx2i} + 1\right) + 2a \ln\left(e^{-a2i} e^{-bx2i} + 1\right) - \pi \ln\left(e^{bx2i} + 1\right)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*tan(a + b*x),x)

[Out] -(polylog(2, -exp(-a*2i)*exp(-b*x*2i))*1i - pi*log(exp(b*x*2i) + 1) - pi*log(exp(-a*2i)*exp(-b*x*2i) + 1) + 2*a*log(exp(-a*2i)*exp(-b*x*2i) + 1) + pi*log(cos(b*x)) + b^2*x^2*1i - log(cos(a + b*x))*(2*a - pi) + 2*b*x*log(exp(-a*2i)*exp(-b*x*2i) + 1) + a*b*x*2i)/(2*b^2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x \tan(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a),x)

[Out] Integral(x*tan(a + b*x), x)

$$3.4 \quad \int \frac{\tan(a+bx)}{x} dx$$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\tan(a+bx)}{x}, x\right)$$

[Out] Unintegrable(tan(b*x+a)/x,x)

Rubi [A] time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\tan(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[Tan[a + b*x]/x,x]

[Out] Defer[Int][Tan[a + b*x]/x, x]

Rubi steps

$$\int \frac{\tan(a+bx)}{x} dx = \int \frac{\tan(a+bx)}{x} dx$$

Mathematica [A] time = 2.13, size = 0, normalized size = 0.00

$$\int \frac{\tan(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[Tan[a + b*x]/x,x]

[Out] Integrate[Tan[a + b*x]/x, x]

fricas [A] time = 0.57, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\tan(bx+a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)/x,x, algorithm="fricas")

[Out] integral(tan(b*x + a)/x, x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)/x,x, algorithm="giac")

[Out] integrate(tan(b*x + a)/x, x)

maple [A] time = 0.30, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(tan(b*x+a)/x,x)`

[Out] `int(tan(b*x+a)/x,x)`

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(tan(b*x+a)/x,x, algorithm="maxima")`

[Out] `integrate(tan(b*x + a)/x, x)`

mupad [A] time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\tan(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(tan(a + b*x)/x,x)`

[Out] `int(tan(a + b*x)/x, x)`

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(tan(b*x+a)/x,x)`

[Out] `Integral(tan(a + b*x)/x, x)`

$$3.5 \quad \int \frac{\tan(a+bx)}{x^2} dx$$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\tan(a+bx)}{x^2}, x\right)$$

[Out] Unintegrable(tan(b*x+a)/x^2,x)

Rubi [A] time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\tan(a+bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[Tan[a + b*x]/x^2,x]

[Out] Defer[Int][Tan[a + b*x]/x^2, x]

Rubi steps

$$\int \frac{\tan(a+bx)}{x^2} dx = \int \frac{\tan(a+bx)}{x^2} dx$$

Mathematica [A] time = 3.01, size = 0, normalized size = 0.00

$$\int \frac{\tan(a+bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[Tan[a + b*x]/x^2,x]

[Out] Integrate[Tan[a + b*x]/x^2, x]

fricas [A] time = 0.47, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\tan(bx+a)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)/x^2,x, algorithm="fricas")

[Out] integral(tan(b*x + a)/x^2, x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)/x^2,x, algorithm="giac")

[Out] integrate(tan(b*x + a)/x^2, x)

maple [A] time = 0.30, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(tan(b*x+a)/x^2,x)`

[Out] `int(tan(b*x+a)/x^2,x)`

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx + a)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(tan(b*x+a)/x^2,x, algorithm="maxima")`

[Out] `integrate(tan(b*x + a)/x^2, x)`

mupad [A] time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\tan(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(tan(a + b*x)/x^2,x)`

[Out] `int(tan(a + b*x)/x^2, x)`

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(tan(b*x+a)/x**2,x)`

[Out] `Integral(tan(a + b*x)/x**2, x)`

3.6 $\int x^3 \tan^2(a + bx) dx$

Optimal. Leaf size=98

$$\frac{3\text{Li}_3(-e^{2i(a+bx)})}{2b^4} - \frac{3ix\text{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{3x^2 \log(1 + e^{2i(a+bx)})}{b^2} + \frac{x^3 \tan(a + bx)}{b} - \frac{ix^3}{b} - \frac{x^4}{4}$$

[Out] $-I*x^3/b-1/4*x^4+3*x^2*\ln(1+\exp(2*I*(b*x+a)))/b^2-3*I*x*\text{polylog}(2,-\exp(2*I*(b*x+a)))/b^3+3/2*\text{polylog}(3,-\exp(2*I*(b*x+a)))/b^4+x^3*\tan(b*x+a)/b$

Rubi [A] time = 0.17, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.583$, Rules used = {3720, 3719, 2190, 2531, 2282, 6589, 30}

$$-\frac{3ix\text{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{3\text{Li}_3(-e^{2i(a+bx)})}{2b^4} + \frac{3x^2 \log(1 + e^{2i(a+bx)})}{b^2} + \frac{x^3 \tan(a + bx)}{b} - \frac{ix^3}{b} - \frac{x^4}{4}$$

Antiderivative was successfully verified.

[In] Int[x^3*Tan[a + b*x]^2,x]

[Out] $((-I)*x^3)/b - x^4/4 + (3*x^2*\text{Log}[1 + E^((2*I)*(a + b*x))])/b^2 - ((3*I)*x*\text{PolyLog}[2, -E^((2*I)*(a + b*x))])/b^3 + (3*\text{PolyLog}[3, -E^((2*I)*(a + b*x))])/(2*b^4) + (x^3*\text{Tan}[a + b*x])/b$

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2190

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))* (F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2531

Int[Log[1 + (e_)*((F_)^(c_)*((a_) + (b_)*(x_)))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)])/ (b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

Int[((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

```
Int[((c_.) + (d_.)*(x_.))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_.)])^(n_), x_Symbol]
:= Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_.))^(p_.)]/((d_.) + (e_.)*(x_.)), x_Symbol]
:= Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int x^3 \tan^2(a + bx) dx &= \frac{x^3 \tan(a + bx)}{b} - \frac{3 \int x^2 \tan(a + bx) dx}{b} - \int x^3 dx \\ &= -\frac{ix^3}{b} - \frac{x^4}{4} + \frac{x^3 \tan(a + bx)}{b} + \frac{(6i) \int \frac{e^{2i(a+bx)} x^2}{1+e^{2i(a+bx)}} dx}{b} \\ &= -\frac{ix^3}{b} - \frac{x^4}{4} + \frac{3x^2 \log(1 + e^{2i(a+bx)})}{b^2} + \frac{x^3 \tan(a + bx)}{b} - \frac{6 \int x \log(1 + e^{2i(a+bx)}) dx}{b^2} \\ &= -\frac{ix^3}{b} - \frac{x^4}{4} + \frac{3x^2 \log(1 + e^{2i(a+bx)})}{b^2} - \frac{3ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{x^3 \tan(a + bx)}{b} + \frac{(3i) \int \operatorname{Li}_2(-e^{2i(a+bx)}) dx}{b^3} \\ &= -\frac{ix^3}{b} - \frac{x^4}{4} + \frac{3x^2 \log(1 + e^{2i(a+bx)})}{b^2} - \frac{3ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{x^3 \tan(a + bx)}{b} + \frac{3 \operatorname{Subst}\left(\int \frac{1}{1+e^{2i(a+bx)}} dx\right)}{b^3} \\ &= -\frac{ix^3}{b} - \frac{x^4}{4} + \frac{3x^2 \log(1 + e^{2i(a+bx)})}{b^2} - \frac{3ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{3 \operatorname{Li}_3(-e^{2i(a+bx)})}{2b^4} + \frac{x^3 \tan(a + bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.79, size = 115, normalized size = 1.17

$$\frac{2b^2 x^2 \left(\frac{2ibx}{1+e^{2ia}} + 3 \log(1 + e^{-2i(a+bx)}) \right) + 6ibx \operatorname{Li}_2(-e^{-2i(a+bx)}) + 3 \operatorname{Li}_3(-e^{-2i(a+bx)})}{2b^4} + \frac{x^3 \sec(a) \sin(bx) \sec(a + bx)}{b}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*Tan[a + b*x]^2,x]
```

```
[Out] -1/4*x^4 + (2*b^2*x^2*((2*I)*b*x)/(1 + E^((2*I)*a)) + 3*Log[1 + E^((-2*I)*(a + b*x))]) + (6*I)*b*x*PolyLog[2, -E^((-2*I)*(a + b*x))] + 3*PolyLog[3, -E^((-2*I)*(a + b*x))]/(2*b^4) + (x^3*Sec[a]*Sec[a + b*x]*Sin[b*x])/b
```

fricas [C] time = 0.64, size = 225, normalized size = 2.30

$$\frac{b^4 x^4 - 4b^3 x^3 \tan(bx + a) - 6b^2 x^2 \log\left(-\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) - 6b^2 x^2 \log\left(-\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) - 6i bx \operatorname{Li}_2\left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) - 6i bx \operatorname{Li}_2\left(\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right)}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*tan(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] -1/4*(b^4*x^4 - 4*b^3*x^3*tan(b*x + a) - 6*b^2*x^2*log(-2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) - 6*b^2*x^2*log(-2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) - 6*I*b*x*dilog(2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)))/b
```

1) + 6*I*b*x*dilog(2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) - 3*polylog(3, (tan(b*x + a)^2 + 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) - 3*polylog(3, (tan(b*x + a)^2 - 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)))/b^4

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^3 \tan(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a)^2,x, algorithm="giac")

[Out] integrate(x^3*tan(b*x + a)^2, x)

maple [A] time = 0.36, size = 133, normalized size = 1.36

$$-\frac{x^4}{4} + \frac{2ix^3}{b(e^{2i(bx+a)} + 1)} - \frac{2ix^3}{b} + \frac{6ia^2x}{b^3} + \frac{4ia^3}{b^4} + \frac{3x^2 \ln(e^{2i(bx+a)} + 1)}{b^2} - \frac{3ix \operatorname{polylog}(2, -e^{2i(bx+a)})}{b^3} + \frac{3 \operatorname{polylog}(3, -e^{2i(bx+a)})}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*tan(b*x+a)^2,x)

[Out] -1/4*x^4+2*I*x^3/b/(exp(2*I*(b*x+a))+1)-2*I/b*x^3+6*I/b^3*a^2*x+4*I/b^4*a^3+3*x^2*ln(exp(2*I*(b*x+a))+1)/b^2-3*I*x*polylog(2,-exp(2*I*(b*x+a)))/b^3+3/2*polylog(3,-exp(2*I*(b*x+a)))/b^4-6/b^4*a^2*ln(exp(I*(b*x+a)))

maxima [B] time = 2.99, size = 640, normalized size = 6.53

$$2(bx + a - \tan(bx + a))a^3 - \frac{3((bx+a)^2 \cos(2bx+2a)^2 + (bx+a)^2 \sin(2bx+2a)^2 + 2(bx+a)^2 \cos(2bx+2a) + (bx+a)^2 - (\cos(2bx+2a)^2 + \sin(2bx+2a)^2))}{\cos(2bx+2a)^2 + \sin(2bx+2a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a)^2,x, algorithm="maxima")

[Out] 1/2*(2*(b*x + a - tan(b*x + a))*a^3 - 3*((b*x + a)^2*cos(2*b*x + 2*a)^2 + (b*x + a)^2*sin(2*b*x + 2*a)^2 + 2*(b*x + a)^2*cos(2*b*x + 2*a) + (b*x + a)^2 - (cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1)*log(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1) - 4*(b*x + a)*sin(2*b*x + 2*a))*a^2/(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1) + 2*(I*(b*x + a)^4 - 4*I*(b*x + a)^3*a + (12*(b*x + a)^2 - 24*(b*x + a)*a + 12*((b*x + a)^2 - 2*(b*x + a)*a)*cos(2*b*x + 2*a) + (12*I*(b*x + a)^2 - 24*I*(b*x + a)*a)*sin(2*b*x + 2*a))*arctan2(sin(2*b*x + 2*a), cos(2*b*x + 2*a) + 1) + (I*(b*x + a)^4 - 4*(b*x + a)^3*(I*a + 2) + 24*(b*x + a)^2*a*cos(2*b*x + 2*a) - 12*(b*x*cos(2*b*x + 2*a) + I*b*x*sin(2*b*x + 2*a) + b*x)*dilog(-e^(2*I*b*x + 2*I*a)) + (-6*I*(b*x + a)^2 + 12*I*(b*x + a)*a + (-6*I*(b*x + a)^2 + 12*I*(b*x + a)*a)*cos(2*b*x + 2*a) + 6*((b*x + a)^2 - 2*(b*x + a)*a)*sin(2*b*x + 2*a))*log(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1) + (-6*I*cos(2*b*x + 2*a) + 6*sin(2*b*x + 2*a) - 6*I)*polylog(3, -e^(2*I*b*x + 2*I*a)) - ((b*x + a)^4 - (b*x + a)^3*(4*a - 8*I) - 24*I*(b*x + a)^2*a*sin(2*b*x + 2*a))/(-4*I*cos(2*b*x + 2*a) + 4*sin(2*b*x + 2*a) - 4*I))/b^4

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^3 \tan(a + bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*tan(a + b*x)^2,x)
```

```
[Out] int(x^3*tan(a + b*x)^2, x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int x^3 \tan^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*tan(b*x+a)**2,x)
```

```
[Out] Integral(x**3*tan(a + b*x)**2, x)
```


3.7 $\int x^2 \tan^2(a + bx) dx$

Optimal. Leaf size=73

$$-\frac{i\text{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{2x \log(1 + e^{2i(a+bx)})}{b^2} + \frac{x^2 \tan(a + bx)}{b} - \frac{ix^2}{b} - \frac{x^3}{3}$$

[Out] $-I*x^2/b-1/3*x^3+2*x*\ln(1+\exp(2*I*(b*x+a)))/b^2-I*\text{polylog}(2,-\exp(2*I*(b*x+a)))/b^3+x^2*\tan(b*x+a)/b$

Rubi [A] time = 0.11, antiderivative size = 73, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3720, 3719, 2190, 2279, 2391, 30}

$$-\frac{i\text{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{2x \log(1 + e^{2i(a+bx)})}{b^2} + \frac{x^2 \tan(a + bx)}{b} - \frac{ix^2}{b} - \frac{x^3}{3}$$

Antiderivative was successfully verified.

[In] Int[x^2*Tan[a + b*x]^2,x]

[Out] $((-I)*x^2)/b - x^3/3 + (2*x*\text{Log}[1 + E^((2*I)*(a + b*x))])/b^2 - (I*\text{PolyLog}[2, -E^((2*I)*(a + b*x))])/b^3 + (x^2*\text{Tan}[a + b*x])/b$

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2190

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_)*((F_)^(e_)*((c_) + (d_)*(x_)))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 3719

Int[((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1)/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

Int[((c_) + (d_)*(x_))^(m_)*((b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1)/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x],

x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x] /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

Rubi steps

$$\begin{aligned} \int x^2 \tan^2(a + bx) dx &= \frac{x^2 \tan(a + bx)}{b} - \frac{2 \int x \tan(a + bx) dx}{b} - \int x^2 dx \\ &= -\frac{ix^2}{b} - \frac{x^3}{3} + \frac{x^2 \tan(a + bx)}{b} + \frac{(4i) \int \frac{e^{2i(a+bx)} x}{1+e^{2i(a+bx)}} dx}{b} \\ &= -\frac{ix^2}{b} - \frac{x^3}{3} + \frac{2x \log(1 + e^{2i(a+bx)})}{b^2} + \frac{x^2 \tan(a + bx)}{b} - \frac{2 \int \log(1 + e^{2i(a+bx)}) dx}{b^2} \\ &= -\frac{ix^2}{b} - \frac{x^3}{3} + \frac{2x \log(1 + e^{2i(a+bx)})}{b^2} + \frac{x^2 \tan(a + bx)}{b} + \frac{i \text{Subst}\left(\int \frac{\log(1+x)}{x} dx, x, e^{2i(a+bx)}\right)}{b^3} \\ &= -\frac{ix^2}{b} - \frac{x^3}{3} + \frac{2x \log(1 + e^{2i(a+bx)})}{b^2} - \frac{i \text{Li}_2(-e^{2i(a+bx)})}{b^3} + \frac{x^2 \tan(a + bx)}{b} \end{aligned}$$

Mathematica [B] time = 6.19, size = 189, normalized size = 2.59

$$\text{csc}(a) \sec(a) \left(b^2 x^2 e^{-i \tan^{-1}(\cot(a))} - \frac{\cot(a) \left(i \text{Li}_2 \left(e^{2i(bx - \tan^{-1}(\cot(a)))} \right) + ibx(-2 \tan^{-1}(\cot(a)) - \pi) - 2(bx - \tan^{-1}(\cot(a))) \log \left(1 - e^{2i(bx - \tan^{-1}(\cot(a)))} \right) \right)}{\sqrt{\cot^2(a) + 1}} \right)$$

$$b^3 \sqrt{\csc^2(a) (\sin^2(a) + \cos^2(a))}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2*Tan[a + b*x]^2,x]

[Out] -1/3*x^3 + (Csc[a]*((b^2*x^2)/E^(I*ArcTan[Cot[a]])) - (Cot[a]*(I*b*x*(-Pi - 2*ArcTan[Cot[a]])) - Pi*Log[1 + E^((-2*I)*b*x)] - 2*(b*x - ArcTan[Cot[a]])*Log[1 - E^((2*I)*(b*x - ArcTan[Cot[a]])])]) + Pi*Log[Cos[b*x]] - 2*ArcTan[Cot[a]]*Log[Sin[b*x - ArcTan[Cot[a]]]) + I*PolyLog[2, E^((2*I)*(b*x - ArcTan[Cot[a]])])])]/Sqrt[1 + Cot[a]^2]*Sec[a]/(b^3*Sqrt[Csc[a]^2*(Cos[a]^2 + Sin[a]^2)]) + (x^2*Sec[a]*Sec[a + b*x]*Sin[b*x])/b

fricas [B] time = 0.53, size = 144, normalized size = 1.97

$$\frac{2b^3x^3 - 6b^2x^2 \tan(bx + a) - 6bx \log\left(-\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) - 6bx \log\left(-\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) - 3i \text{Li}_2\left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 3i \text{Li}_2\left(\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right)}{6b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a)^2,x, algorithm="fricas")

[Out] -1/6*(2*b^3*x^3 - 6*b^2*x^2*tan(b*x + a) - 6*b*x*log(-2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) - 6*b*x*log(-2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) - 3*I*dilog(2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) + 3*I*dilog(2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1))/b^3

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a)^2,x, algorithm="giac")

[Out] integrate(x^2*tan(b*x + a)^2, x)

maple [A] time = 0.35, size = 108, normalized size = 1.48

$$-\frac{x^3}{3} + \frac{2ix^2}{b(e^{2i(bx+a)} + 1)} - \frac{2ix^2}{b} - \frac{4iax}{b^2} - \frac{2ia^2}{b^3} + \frac{2x \ln(e^{2i(bx+a)} + 1)}{b^2} - \frac{i \operatorname{polylog}(2, -e^{2i(bx+a)})}{b^3} + \frac{4a \ln(e^{i(bx+a)})}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*tan(b*x+a)^2,x)

[Out] $-1/3*x^3+2*I*x^2/b/(\exp(2*I*(b*x+a))+1)-2*I/b*x^2-4*I/b^2*a*x-2*I/b^3*a^2+2*x*\ln(\exp(2*I*(b*x+a))+1)/b^2-I*\operatorname{polylog}(2,-\exp(2*I*(b*x+a)))/b^3+4/b^3*a*\ln(\exp(I*(b*x+a)))$

maxima [B] time = 1.35, size = 256, normalized size = 3.51

$$i b^3 x^3 + 6 (b x \cos (2 b x + 2 a) + i b x \sin (2 b x + 2 a) + b x) \arctan (\sin (2 b x + 2 a), \cos (2 b x + 2 a) + 1) + (i b^3 x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a)^2,x, algorithm="maxima")

[Out] $(I*b^3*x^3 + 6*(b*x*\cos(2*b*x + 2*a) + I*b*x*\sin(2*b*x + 2*a) + b*x)*\arctan(2(\sin(2*b*x + 2*a), \cos(2*b*x + 2*a) + 1) + (I*b^3*x^3 - 6*b^2*x^2)*\cos(2*b*x + 2*a) - 3*(\cos(2*b*x + 2*a) + I*\sin(2*b*x + 2*a) + 1)*\operatorname{dilog}(-e^{(2*I*b*x + 2*I*a)}) + (-3*I*b*x*\cos(2*b*x + 2*a) + 3*b*x*\sin(2*b*x + 2*a) - 3*I*b*x)*\log(\cos(2*b*x + 2*a)^2 + \sin(2*b*x + 2*a)^2 + 2*\cos(2*b*x + 2*a) + 1) - (b^3*x^3 + 6*I*b^2*x^2)*\sin(2*b*x + 2*a))/(-3*I*b^3*\cos(2*b*x + 2*a) + 3*b^3*\sin(2*b*x + 2*a) - 3*I*b^3)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^2 \tan(a + b x)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*tan(a + b*x)^2,x)

[Out] int(x^2*tan(a + b*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan^2(a + b x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*tan(b*x+a)**2,x)

[Out] Integral(x**2*tan(a + b*x)**2, x)

3.8 $\int x \tan^2(a + bx) dx$

Optimal. Leaf size=30

$$\frac{\log(\cos(a + bx))}{b^2} + \frac{x \tan(a + bx)}{b} - \frac{x^2}{2}$$

[Out] $-1/2*x^2+\ln(\cos(b*x+a))/b^2+x*\tan(b*x+a)/b$

Rubi [A] time = 0.02, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.300$, Rules used = {3720, 3475, 30}

$$\frac{\log(\cos(a + bx))}{b^2} + \frac{x \tan(a + bx)}{b} - \frac{x^2}{2}$$

Antiderivative was successfully verified.

[In] Int[x*Tan[a + b*x]^2,x]

[Out] $-x^2/2 + \text{Log}[\text{Cos}[a + b*x]]/b^2 + (x*\text{Tan}[a + b*x])/b$

Rule 30

Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 3475

Int[tan[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]

Rule 3720

Int[((c_.) + (d_.)*(x_))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

Rubi steps

$$\begin{aligned} \int x \tan^2(a + bx) dx &= \frac{x \tan(a + bx)}{b} - \frac{\int \tan(a + bx) dx}{b} - \int x dx \\ &= -\frac{x^2}{2} + \frac{\log(\cos(a + bx))}{b^2} + \frac{x \tan(a + bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.18, size = 43, normalized size = 1.43

$$\frac{\log(\cos(a + bx))}{b^2} + \frac{x \tan(a)}{b} + \frac{x \sec(a) \sin(bx) \sec(a + bx)}{b} - \frac{x^2}{2}$$

Antiderivative was successfully verified.

[In] Integrate[x*Tan[a + b*x]^2,x]

[Out] $-1/2*x^2 + \text{Log}[\text{Cos}[a + b*x]]/b^2 + (x*\text{Sec}[a]*\text{Sec}[a + b*x]*\text{Sin}[b*x])/b + (x*\text{Tan}[a])/b$

fricas [A] time = 0.57, size = 38, normalized size = 1.27

$$\frac{b^2 x^2 - 2 b x \tan(bx + a) - \log\left(\frac{1}{\tan(bx+a)^2+1}\right)}{2 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a)^2,x, algorithm="fricas")

[Out] -1/2*(b^2*x^2 - 2*b*x*tan(b*x + a) - log(1/(tan(b*x + a)^2 + 1)))/b^2

giac [B] time = 1.26, size = 182, normalized size = 6.07

$$\frac{b^2 x^2 \tan(bx) \tan(a) - b^2 x^2 + 2 b x \tan(bx) + 2 b x \tan(a) - \log\left(\frac{4(\tan(bx)^4 \tan(a)^2 - 2 \tan(bx)^3 \tan(a) + \tan(bx)^2 \tan(a)^2 + \tan(bx) \tan(a)^2 - 2 \tan(bx) \tan(a) + 1)}{\tan(a)^2 + 1}\right)}{2(b^2 \tan(bx) \tan(a) - b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a)^2,x, algorithm="giac")

[Out] -1/2*(b^2*x^2*tan(b*x)*tan(a) - b^2*x^2 + 2*b*x*tan(b*x) + 2*b*x*tan(a) - log(4*(tan(b*x)^4*tan(a)^2 - 2*tan(b*x)^3*tan(a) + tan(b*x)^2*tan(a)^2 + tan(b*x)*tan(a)^2 - 2*tan(b*x)*tan(a) + 1)/(tan(a)^2 + 1))*tan(b*x)*tan(a) + log(4*(tan(b*x)^4*tan(a)^2 - 2*tan(b*x)^3*tan(a) + tan(b*x)^2*tan(a)^2 + tan(b*x)*tan(a)^2 - 2*tan(b*x)*tan(a) + 1)/(tan(a)^2 + 1)))/(b^2*tan(b*x)*tan(a) - b^2)

maple [A] time = 0.26, size = 29, normalized size = 0.97

$$-\frac{x^2}{2} + \frac{\ln(\cos(bx + a))}{b^2} + \frac{x \tan(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*tan(b*x+a)^2,x)

[Out] -1/2*x^2+ln(cos(b*x+a))/b^2+x*tan(b*x+a)/b

maxima [B] time = 0.93, size = 214, normalized size = 7.13

$$2(bx + a - \tan(bx + a))a - \frac{(bx+a)^2 \cos(2bx+2a)^2 + (bx+a)^2 \sin(2bx+2a)^2 + 2(bx+a)^2 \cos(2bx+2a) + (bx+a)^2 - (\cos(2bx+2a)^2 + \sin(2bx+2a)^2)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a)^2,x, algorithm="maxima")

[Out] 1/2*(2*(b*x + a - tan(b*x + a))*a - ((b*x + a)^2*cos(2*b*x + 2*a)^2 + (b*x + a)^2*sin(2*b*x + 2*a)^2 + 2*(b*x + a)^2*cos(2*b*x + 2*a) + (b*x + a)^2 - (cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1)*log(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1) - 4*(b*x + a)*sin(2*b*x + 2*a))/(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1))/b^2

mupad [B] time = 0.11, size = 35, normalized size = 1.17

$$\frac{\frac{\ln(\tan(a+bx)^2+1)}{2} - bx \tan(a + bx)}{b^2} - \frac{x^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*tan(a + b*x)^2,x)
```

```
[Out] - (log(tan(a + b*x)^2 + 1)/2 - b*x*tan(a + b*x))/b^2 - x^2/2
```

sympy [A] time = 0.18, size = 41, normalized size = 1.37

$$\begin{cases} -\frac{x^2}{2} + \frac{x \tan(a+bx)}{b} - \frac{\log(\tan^2(a+bx)+1)}{2b^2} & \text{for } b \neq 0 \\ \frac{x^2 \tan^2(a)}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*tan(b*x+a)**2,x)
```

```
[Out] Piecewise((-x**2/2 + x*tan(a + b*x)/b - log(tan(a + b*x)**2 + 1)/(2*b**2),  
Ne(b, 0)), (x**2*tan(a)**2/2, True))
```

$$3.9 \quad \int \frac{\tan^2(a+bx)}{x} dx$$

Optimal. Leaf size=15

$$\text{Int}\left(\frac{\tan^2(a+bx)}{x}, x\right)$$

[Out] Unintegrable(tan(b*x+a)^2/x, x)

Rubi [A] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\tan^2(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[Tan[a + b*x]^2/x, x]

[Out] Defer[Int][Tan[a + b*x]^2/x, x]

Rubi steps

$$\int \frac{\tan^2(a+bx)}{x} dx = \int \frac{\tan^2(a+bx)}{x} dx$$

Mathematica [A] time = 2.76, size = 0, normalized size = 0.00

$$\int \frac{\tan^2(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[Tan[a + b*x]^2/x, x]

[Out] Integrate[Tan[a + b*x]^2/x, x]

fricas [A] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\tan(bx+a)^2}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^2/x, x, algorithm="fricas")

[Out] integral(tan(b*x + a)^2/x, x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^2/x, x, algorithm="giac")

[Out] integrate(tan(b*x + a)^2/x, x)

maple [A] time = 0.36, size = 0, normalized size = 0.00

$$\int \frac{\tan^2(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(b*x+a)^2/x,x)

[Out] int(tan(b*x+a)^2/x,x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\frac{bx \cos(2bx + 2a)^2 \log(x) + bx \log(x) \sin(2bx + 2a)^2 + 2bx \cos(2bx + 2a) \log(x) + bx \log(x) - \frac{2(b^2x \cos(2bx + 2a)^2)}{bx \cos(2bx + 2a)^2 + bx \sin(2bx + 2a)^2}}{bx \cos(2bx + 2a)^2 + bx \sin(2bx + 2a)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^2/x,x, algorithm="maxima")

[Out] $-(b*x*\cos(2*b*x + 2*a)^2*\log(x) + b*x*\log(x)*\sin(2*b*x + 2*a)^2 + 2*b*x*\cos(2*b*x + 2*a)*\log(x) + b*x*\log(x) - 2*(b^2*x*\cos(2*b*x + 2*a)^2 + b^2*x*\sin(2*b*x + 2*a)^2 + 2*b^2*x*\cos(2*b*x + 2*a) + b^2*x)*\integrate(\sin(2*b*x + 2*a)/(b^2*x^2*\cos(2*b*x + 2*a)^2 + b^2*x^2*\sin(2*b*x + 2*a)^2 + 2*b^2*x^2*\cos(2*b*x + 2*a) + b^2*x^2), x) - 2*\sin(2*b*x + 2*a))/(b*x*\cos(2*b*x + 2*a)^2 + b*x*\sin(2*b*x + 2*a)^2 + 2*b*x*\cos(2*b*x + 2*a) + b*x)$

mupad [A] time = 0.00, size = -1, normalized size = -0.07

$$\int \frac{\tan^2(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(a + b*x)^2/x,x)

[Out] int(tan(a + b*x)^2/x, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan^2(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)**2/x,x)

[Out] Integral(tan(a + b*x)**2/x, x)

3.10 $\int \frac{\tan^2(a+bx)}{x^2} dx$

Optimal. Leaf size=15

$$\text{Int}\left(\frac{\tan^2(a+bx)}{x^2}, x\right)$$

[Out] Unintegrable(tan(b*x+a)^2/x^2, x)

Rubi [A] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\tan^2(a+bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[Tan[a + b*x]^2/x^2, x]

[Out] Defer[Int][Tan[a + b*x]^2/x^2, x]

Rubi steps

$$\int \frac{\tan^2(a+bx)}{x^2} dx = \int \frac{\tan^2(a+bx)}{x^2} dx$$

Mathematica [A] time = 2.98, size = 0, normalized size = 0.00

$$\int \frac{\tan^2(a+bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[Tan[a + b*x]^2/x^2, x]

[Out] Integrate[Tan[a + b*x]^2/x^2, x]

fricas [A] time = 0.58, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\tan(bx+a)^2}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^2/x^2, x, algorithm="fricas")

[Out] integral(tan(b*x + a)^2/x^2, x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^2/x^2, x, algorithm="giac")

[Out] integrate(tan(b*x + a)^2/x^2, x)

maple [A] time = 0.36, size = 0, normalized size = 0.00

$$\int \frac{\tan^2(bx + a)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(b*x+a)^2/x^2,x)

[Out] int(tan(b*x+a)^2/x^2,x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$bx \cos(2bx + 2a)^2 + bx \sin(2bx + 2a)^2 + 2bx \cos(2bx + 2a) + bx + \frac{4(b^2x^2 \cos(2bx + 2a)^2 + b^2x^2 \sin(2bx + 2a)^2 + 2b^2x^2 \cos(2bx + 2a) \sin(2bx + 2a))}{bx^2 \cos(2bx + 2a)^2 + bx^2 \sin(2bx + 2a)^2 + 2bx^2 \cos(2bx + 2a) \sin(2bx + 2a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^2/x^2,x, algorithm="maxima")

[Out] (b*x*cos(2*b*x + 2*a)^2 + b*x*sin(2*b*x + 2*a)^2 + 2*b*x*cos(2*b*x + 2*a) + b*x + 4*(b^2*x^2*cos(2*b*x + 2*a)^2 + b^2*x^2*sin(2*b*x + 2*a)^2 + 2*b^2*x^2*cos(2*b*x + 2*a)*sin(2*b*x + 2*a))/(b^2*x^3*cos(2*b*x + 2*a)^2 + b^2*x^3*sin(2*b*x + 2*a)^2 + 2*b^2*x^3*cos(2*b*x + 2*a)*sin(2*b*x + 2*a) + b^2*x^3), x) + 2*sin(2*b*x + 2*a)/(b*x^2*cos(2*b*x + 2*a)^2 + b*x^2*sin(2*b*x + 2*a)^2 + 2*b*x^2*cos(2*b*x + 2*a)*sin(2*b*x + 2*a) + b*x^2)

mupad [A] time = 0.00, size = -1, normalized size = -0.07

$$\int \frac{\tan^2(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(a + b*x)^2/x^2,x)

[Out] int(tan(a + b*x)^2/x^2, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan^2(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)**2/x**2,x)

[Out] Integral(tan(a + b*x)**2/x**2, x)

3.11 $\int x^3 \tan^3(a + bx) dx$

Optimal. Leaf size=205

$$\frac{3i\text{Li}_2(-e^{2i(a+bx)})}{2b^4} + \frac{3i\text{Li}_4(-e^{2i(a+bx)})}{4b^4} + \frac{3x\text{Li}_3(-e^{2i(a+bx)})}{2b^3} - \frac{3x \log(1 + e^{2i(a+bx)})}{b^3} - \frac{3ix^2\text{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{3x^2 \tan(a + bx)}{2b^2}$$

[Out] $3/2*I*x^2/b^2+1/2*x^3/b-1/4*I*x^4-3*x*\ln(1+\exp(2*I*(b*x+a)))/b^3+x^3*\ln(1+\exp(2*I*(b*x+a)))/b+3/2*I*\text{polylog}(2,-\exp(2*I*(b*x+a)))/b^4-3/2*I*x^2*\text{polylog}(2,-\exp(2*I*(b*x+a)))/b^2+3/2*x*\text{polylog}(3,-\exp(2*I*(b*x+a)))/b^3+3/4*I*\text{polylog}(4,-\exp(2*I*(b*x+a)))/b^4-3/2*x^2*\tan(b*x+a)/b^2+1/2*x^3*\tan(b*x+a)^2/b$

Rubi [A] time = 0.29, antiderivative size = 205, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 10, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.833$, Rules used = {3720, 3719, 2190, 2279, 2391, 30, 2531, 6609, 2282, 6589}

$$-\frac{3ix^2\text{Li}_2(-e^{2i(a+bx)})}{2b^2} + \frac{3x\text{Li}_3(-e^{2i(a+bx)})}{2b^3} + \frac{3i\text{Li}_2(-e^{2i(a+bx)})}{2b^4} + \frac{3i\text{Li}_4(-e^{2i(a+bx)})}{4b^4} - \frac{3x^2 \tan(a + bx)}{2b^2} - \frac{3x \log(1 + e^{2i(a+bx)})}{b^3}$$

Antiderivative was successfully verified.

[In] Int[x^3*Tan[a + b*x]^3,x]

[Out] $((3I/2)*x^2)/b^2 + x^3/(2*b) - (I/4)*x^4 - (3*x*\text{Log}[1 + E^{((2I)*(a + b*x))}])/b^3 + (x^3*\text{Log}[1 + E^{((2I)*(a + b*x))}])/b + ((3I/2)*\text{PolyLog}[2, -E^{((2I)*(a + b*x))}])/b^4 - (((3I/2)*x^2*\text{PolyLog}[2, -E^{((2I)*(a + b*x))}])/b^2 + (3*x*\text{PolyLog}[3, -E^{((2I)*(a + b*x))}])/(2*b^3) + (((3I/4)*\text{PolyLog}[4, -E^{((2I)*(a + b*x))}])/b^4 - (3*x^2*\text{Tan}[a + b*x])/(2*b^2) + (x^3*\text{Tan}[a + b*x]^2)/(2*b)$

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2190

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_)*((F_)^(e_)*((c_) + (d_)*(x_)))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^{(c_)*((a_)+(b_)*x)}*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2391

```
Int[Log[(c_.)*(d_) + (e_.)*(x_)^(n_.)]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^((c_.)*(a_.) + (b_.)*(x_)))^(n_.)]*((f_.) + (g_.)*(x_)^(m_.), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x))))^n]]/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x))))^n]], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]
```

Rule 3719

```
Int[((c_.) + (d_.)*(x_)^(m_.))*tan[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 3720

```
Int[((c_.) + (d_.)*(x_)^(m_.))*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_)^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6609

```
Int[((e_.) + (f_.)*(x_)^(m_.))*PolyLog[n_, (d_.)*((F_)^((c_.)*(a_.) + (b_.)*(x_)))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]]/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned}
\int x^3 \tan^3(a + bx) dx &= \frac{x^3 \tan^2(a + bx)}{2b} - \frac{3 \int x^2 \tan^2(a + bx) dx}{2b} - \int x^3 \tan(a + bx) dx \\
&= -\frac{ix^4}{4} - \frac{3x^2 \tan(a + bx)}{2b^2} + \frac{x^3 \tan^2(a + bx)}{2b} + 2i \int \frac{e^{2i(a+bx)} x^3}{1 + e^{2i(a+bx)}} dx + \frac{3 \int x \tan(a + bx)}{b^2} \\
&= \frac{3ix^2}{2b^2} + \frac{x^3}{2b} - \frac{ix^4}{4} + \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} - \frac{3x^2 \tan(a + bx)}{2b^2} + \frac{x^3 \tan^2(a + bx)}{2b} - \frac{(6i) \int}{b^2} \\
&= \frac{3ix^2}{2b^2} + \frac{x^3}{2b} - \frac{ix^4}{4} - \frac{3x \log(1 + e^{2i(a+bx)})}{b^3} + \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} - \frac{3ix^2 \text{Li}_2(-e^{2i(a+bx)})}{2b^2} \\
&= \frac{3ix^2}{2b^2} + \frac{x^3}{2b} - \frac{ix^4}{4} - \frac{3x \log(1 + e^{2i(a+bx)})}{b^3} + \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} - \frac{3ix^2 \text{Li}_2(-e^{2i(a+bx)})}{2b^2} \\
&= \frac{3ix^2}{2b^2} + \frac{x^3}{2b} - \frac{ix^4}{4} - \frac{3x \log(1 + e^{2i(a+bx)})}{b^3} + \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{3i \text{Li}_2(-e^{2i(a+bx)})}{2b^4} - \\
&= \frac{3ix^2}{2b^2} + \frac{x^3}{2b} - \frac{ix^4}{4} - \frac{3x \log(1 + e^{2i(a+bx)})}{b^3} + \frac{x^3 \log(1 + e^{2i(a+bx)})}{b} + \frac{3i \text{Li}_2(-e^{2i(a+bx)})}{2b^4} -
\end{aligned}$$

Mathematica [A] time = 6.67, size = 359, normalized size = 1.75

$$\frac{3x^2 \sec(a) \sin(bx) \sec(a + bx)}{2b^2} - \frac{3 \csc(a) \sec(a) \left(b^2 x^2 e^{-i \tan^{-1}(\cot(a))} - \frac{\cot(a) \left(i \text{Li}_2 \left(e^{2i(bx - \tan^{-1}(\cot(a)))} \right) + ibx(-2 \tan^{-1}(\cot(a))) \right)}{2b^4} \right)}{2b^4}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3*Tan[a + b*x]^3,x]

[Out] (I/8)*E^(I*a)*((2*x^4)/E^((2*I)*a) - ((4*I)*(1 + E^((-2*I)*a))*x^3*Log[1 + E^((-2*I)*(a + b*x))])/b + (3*(1 + E^((2*I)*a))*(2*b^2*x^2*PolyLog[2, -E^((-2*I)*(a + b*x))] - (2*I)*b*x*PolyLog[3, -E^((-2*I)*(a + b*x))] - PolyLog[4, -E^((-2*I)*(a + b*x))]))/(b^4*E^((2*I)*a))*Sec[a] + (x^3*Sec[a + b*x]^2)/(2*b) - (3*Csc[a]*((b^2*x^2)/E^(I*ArcTan[Cot[a]]) - (Cot[a]*(I*b*x*(-Pi - 2*ArcTan[Cot[a]]) - Pi*Log[1 + E^((-2*I)*b*x]) - 2*(b*x - ArcTan[Cot[a]])*Log[1 - E^((2*I)*(b*x - ArcTan[Cot[a]])]) + Pi*Log[Cos[b*x]] - 2*ArcTan[Cot[a]]*Log[Sin[b*x - ArcTan[Cot[a]]]]) + I*PolyLog[2, E^((2*I)*(b*x - ArcTan[Cot[a]])])))/Sqrt[1 + Cot[a]^2])*Sec[a]/(2*b^4*Sqrt[Csc[a]^2*(Cos[a]^2 + Sin[a]^2)) - (3*x^2*Sec[a]*Sec[a + b*x]*Sin[b*x])/(2*b^2) - (x^4*Tan[a])/4

fricas [C] time = 0.57, size = 342, normalized size = 1.67

$$\frac{4b^3x^3 \tan(bx + a)^2 + 4b^3x^3 - 12b^2x^2 \tan(bx + a) + 6bx \text{polylog}\left(3, \frac{\tan(bx+a)^2 + 2i \tan(bx+a) - 1}{\tan(bx+a)^2 + 1}\right) + 6bx \text{polylog}\left(3, \frac{\tan(bx+a)^2 - 2i \tan(bx+a) - 1}{\tan(bx+a)^2 + 1}\right)}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a)^3,x, algorithm="fricas")

[Out] 1/8*(4*b^3*x^3*tan(b*x + a)^2 + 4*b^3*x^3 - 12*b^2*x^2*tan(b*x + a) + 6*b*x*polylog(3, (tan(b*x + a)^2 + 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + 6*b*x*polylog(3, (tan(b*x + a)^2 - 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + (6*I*b^2*x^2 - 6*I)*dilog(2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) + (-6*I*b^2*x^2 + 6*I)*dilog(2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) + 4*(b^3*x^3 - 3*b*x)*log(-2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1))

$2 + 1)) + 4*(b^3*x^3 - 3*b*x)*\log(-2*(-I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)) - 3*I*\text{polylog}(4, (\tan(b*x + a)^2 + 2*I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)) + 3*I*\text{polylog}(4, (\tan(b*x + a)^2 - 2*I*\tan(b*x + a) - 1)/(\tan(b*x + a)^2 + 1)))/b^4$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^3 \tan(bx + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a)^3,x, algorithm="giac")

[Out] integrate(x^3*tan(b*x + a)^3, x)

maple [A] time = 0.32, size = 251, normalized size = 1.22

$$-\frac{2ia^3x}{b^3} + \frac{x^2(2bx e^{2i(bx+a)} - 3ie^{2i(bx+a)} - 3i)}{b^2(e^{2i(bx+a)} + 1)^2} + \frac{3i \text{polylog}(2, -e^{2i(bx+a)})}{2b^4} + \frac{3i \text{polylog}(4, -e^{2i(bx+a)})}{4b^4} + \frac{3ix^2}{b^2} - \frac{3ia^4}{2b^4} - \frac{3i}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*tan(b*x+a)^3,x)

[Out] $-2*I/b^3*a^3*x + x^2*(2*b*x*\exp(2*I*(b*x+a)) - 3*I*\exp(2*I*(b*x+a)) - 3*I)/b^2/(e^{\exp(2*I*(b*x+a))} + 1)^2 + 3/2*I*\text{polylog}(2, -\exp(2*I*(b*x+a)))/b^4 + 3/4*I*\text{polylog}(4, -\exp(2*I*(b*x+a)))/b^4 + 3*I/b^2*x^2 - 3/2*I/b^4*a^4 - 3/2*I*x^2*\text{polylog}(2, -\exp(2*I*(b*x+a)))/b^2 - 1/4*I*x^4 + 3*I/b^4*a^2 + 6*I/b^3*a*x + x^3*\ln(\exp(2*I*(b*x+a)) + 1)/b + 3/2*x*\text{polylog}(3, -\exp(2*I*(b*x+a)))/b^3 - 3*x*\ln(\exp(2*I*(b*x+a)) + 1)/b^3 - 6/b^4*a*\ln(\exp(I*(b*x+a)))/b + 2/b^4*a^3*\ln(\exp(I*(b*x+a)))$

maxima [B] time = 2.58, size = 1203, normalized size = 5.87

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*tan(b*x+a)^3,x, algorithm="maxima")

[Out] $1/2*(a^3*(1/(\sin(b*x + a)^2 - 1) - \log(\sin(b*x + a)^2 - 1)) - 2*(3*(b*x + a)^4 - 12*(b*x + a)^3*a + 18*(b*x + a)^2*a^2 + 36*a^2 - (16*(b*x + a)^3 - 36*(b*x + a)^2*a + 36*(a^2 - 1)*(b*x + a) + 4*(4*(b*x + a)^3 - 9*(b*x + a)^2*a + 9*(a^2 - 1)*(b*x + a) + 9*a)*\cos(4*b*x + 4*a) + 8*(4*(b*x + a)^3 - 9*(b*x + a)^2*a + 9*(a^2 - 1)*(b*x + a) + 9*a)*\cos(2*b*x + 2*a) + (16*I*(b*x + a)^3 - 36*I*(b*x + a)^2*a + (36*I*a^2 - 36*I)*(b*x + a) + 36*I*a)*\sin(4*b*x + 4*a) + (32*I*(b*x + a)^3 - 72*I*(b*x + a)^2*a + (72*I*a^2 - 72*I)*(b*x + a) + 72*I*a)*\sin(2*b*x + 2*a) + 36*a)*\arctan2(\sin(2*b*x + 2*a), \cos(2*b*x + 2*a) + 1) + 3*((b*x + a)^4 - 4*(b*x + a)^3*a + 6*(a^2 - 2)*(b*x + a)^2 + 24*(b*x + a)*a)*\cos(4*b*x + 4*a) + (6*(b*x + a)^4 - (b*x + a)^3*(24*a - 24*I) + 36*(a^2 - 2*I*a - 1)*(b*x + a)^2 - (-72*I*a^2 - 72*a)*(b*x + a) + 36*a^2)*\cos(2*b*x + 2*a) + (24*(b*x + a)^2 - 36*(b*x + a)*a + 18*a^2 + 6*(4*(b*x + a)^2 - 6*(b*x + a)*a + 3*a^2 - 3)*\cos(4*b*x + 4*a) + 12*(4*(b*x + a)^2 - 6*(b*x + a)*a + 3*a^2 - 3)*\cos(2*b*x + 2*a) - (-24*I*(b*x + a)^2 + 36*I*(b*x + a)*a - 18*I*a^2 + 18*I)*\sin(4*b*x + 4*a) - (-48*I*(b*x + a)^2 + 72*I*(b*x + a)*a - 36*I*a^2 + 36*I)*\sin(2*b*x + 2*a) - 18)*\text{dilog}(-e^{(2*I*b*x + 2*I*a)}) - (-8*I*(b*x + a)^3 + 18*I*(b*x + a)^2*a + (-18*I*a^2 + 18*I)*(b*x + a) + (-8*I*(b*x + a)^3 + 18*I*(b*x + a)^2*a + (-18*I*a^2 + 18*I)*(b*x + a) - 18*I*a)*\cos(4*b*x + 4*a) + (-16*I*(b*x + a)^3 + 36*I*(b*x + a)^2*a + (-36*I*a^2 + 36*I)*(b*x + a) - 36*I*a)*\cos(2*b*x + 2*a) + 2*(4*(b*x + a)^3 - 9*(b*x + a)^2*a + 9*(a^2 - 1)*(b*x + a) + 9*a)*\sin(4*b*x + 4*a) + 4*(4*(b*x + a)^3 - 9*(b*x + a)^2*a + 9*(a^2 - 1)*(b*x + a) + 9*a)*\sin(2*b*x + 2*a) -$

```

18*I*a)*log(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) +
1) - (12*cos(4*b*x + 4*a) + 24*cos(2*b*x + 2*a) + 12*I*sin(4*b*x + 4*a) + 2
4*I*sin(2*b*x + 2*a) + 12)*polylog(4, -e^(2*I*b*x + 2*I*a)) - (-24*I*b*x +
(-24*I*b*x - 6*I*a)*cos(4*b*x + 4*a) + (-48*I*b*x - 12*I*a)*cos(2*b*x + 2*a
) + 6*(4*b*x + a)*sin(4*b*x + 4*a) + 12*(4*b*x + a)*sin(2*b*x + 2*a) - 6*I*
a)*polylog(3, -e^(2*I*b*x + 2*I*a)) - (-3*I*(b*x + a)^4 + 12*I*(b*x + a)^3*
a + (-18*I*a^2 + 36*I)*(b*x + a)^2 - 72*I*(b*x + a)*a)*sin(4*b*x + 4*a) - (
-6*I*(b*x + a)^4 - 24*(b*x + a)^3*(-I*a - 1) + (-36*I*a^2 - 72*a + 36*I)*(b
*x + a)^2 + 72*(a^2 - I*a)*(b*x + a) - 36*I*a^2)*sin(2*b*x + 2*a))/(-12*I*c
os(4*b*x + 4*a) - 24*I*cos(2*b*x + 2*a) + 12*sin(4*b*x + 4*a) + 24*sin(2*b*
x + 2*a) - 12*I))/b^4

```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int x^3 \tan(a + bx)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*tan(a + b*x)^3,x)
```

```
[Out] int(x^3*tan(a + b*x)^3, x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^3 \tan^3(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*tan(b*x+a)**3,x)
```

```
[Out] Integral(x**3*tan(a + b*x)**3, x)
```

3.12 $\int x^2 \tan^3(a + bx) dx$

Optimal. Leaf size=128

$$\frac{\text{Li}_3(-e^{2i(a+bx)})}{2b^3} - \frac{\log(\cos(a+bx))}{b^3} - \frac{ix\text{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{x \tan(a+bx)}{b^2} + \frac{x^2 \log(1+e^{2i(a+bx)})}{b} + \frac{x^2 \tan^2(a+bx)}{2b} + \frac{x^2}{2b}$$

[Out] 1/2*x^2/b-1/3*I*x^3+x^2*ln(1+exp(2*I*(b*x+a)))/b-ln(cos(b*x+a))/b^3-I*x*polylog(2,-exp(2*I*(b*x+a)))/b^2+1/2*polylog(3,-exp(2*I*(b*x+a)))/b^3-x*tan(b*x+a)/b^2+1/2*x^2*tan(b*x+a)^2/b

Rubi [A] time = 0.18, antiderivative size = 128, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {3720, 3475, 30, 3719, 2190, 2531, 2282, 6589}

$$-\frac{ix\text{Li}_2(-e^{2i(a+bx)})}{b^2} + \frac{\text{Li}_3(-e^{2i(a+bx)})}{2b^3} - \frac{x \tan(a+bx)}{b^2} - \frac{\log(\cos(a+bx))}{b^3} + \frac{x^2 \log(1+e^{2i(a+bx)})}{b} + \frac{x^2 \tan^2(a+bx)}{2b} + \frac{x^2}{2b}$$

Antiderivative was successfully verified.

[In] Int[x^2*Tan[a + b*x]^3,x]

[Out] x^2/(2*b) - (I/3)*x^3 + (x^2*Log[1 + E^((2*I)*(a + b*x))])/b - Log[Cos[a + b*x]]/b^3 - (I*x*PolyLog[2, -E^((2*I)*(a + b*x))])/b^2 + PolyLog[3, -E^((2*I)*(a + b*x))]/(2*b^3) - (x*Tan[a + b*x])/b^2 + (x^2*Tan[a + b*x]^2)/(2*b)

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 2190

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2531

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x))))^n])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x))))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3475

Int[tan[(c_) + (d_)*(x_)], x_Symbol] := -Simp[Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]

Rule 3719

```
Int[((c_.) + (d_.)*(x_.))^(m_.)*tan[(e_.) + (f_.)*(x_.)], x_Symbol] := Simp[(
I*(c + d*x)^(m + 1)/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e
+ f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 3720

```
Int[((c_.) + (d_.)*(x_.))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_.)])^(n_.), x_Symb
ol] := Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Di
st[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x],
x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[
{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_.))^(p_.)]/((d_.) + (e_.)*(x_.)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned}
\int x^2 \tan^3(a + bx) dx &= \frac{x^2 \tan^2(a + bx)}{2b} - \frac{\int x \tan^2(a + bx) dx}{b} - \int x^2 \tan(a + bx) dx \\
&= -\frac{ix^3}{3} - \frac{x \tan(a + bx)}{b^2} + \frac{x^2 \tan^2(a + bx)}{2b} + 2i \int \frac{e^{2i(a+bx)} x^2}{1 + e^{2i(a+bx)}} dx + \frac{\int \tan(a + bx) dx}{b^2} + \dots \\
&= \frac{x^2}{2b} - \frac{ix^3}{3} + \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} - \frac{\log(\cos(a + bx))}{b^3} - \frac{x \tan(a + bx)}{b^2} + \frac{x^2 \tan^2(a + bx)}{2b} \\
&= \frac{x^2}{2b} - \frac{ix^3}{3} + \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} - \frac{\log(\cos(a + bx))}{b^3} - \frac{ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{x \tan(a + bx)}{b^2} \\
&= \frac{x^2}{2b} - \frac{ix^3}{3} + \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} - \frac{\log(\cos(a + bx))}{b^3} - \frac{ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^2} - \frac{x \tan(a + bx)}{b^2} \\
&= \frac{x^2}{2b} - \frac{ix^3}{3} + \frac{x^2 \log(1 + e^{2i(a+bx)})}{b} - \frac{\log(\cos(a + bx))}{b^3} - \frac{ix \operatorname{Li}_2(-e^{2i(a+bx)})}{b^2} + \frac{\operatorname{Li}_3(-e^{2i(a+bx)})}{2b^3}
\end{aligned}$$

Mathematica [A] time = 3.14, size = 172, normalized size = 1.34

$$-4b^3 x^3 \tan(a) + e^{-ia} \sec(a) \left(2b^2 x^2 \left(3 \left(1 + e^{2ia} \right) \log \left(1 + e^{-2i(a+bx)} \right) + 2ibx \right) + 6i \left(1 + e^{2ia} \right) bx \operatorname{Li}_2 \left(-e^{-2i(a+bx)} \right) + 3 \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Tan[a + b*x]^3,x]
```

```
[Out] (((2*b^2*x^2*((2*I)*b*x + 3*(1 + E^((2*I)*a)))*Log[1 + E^((-2*I)*(a + b*x))]
) + (6*I)*b*(1 + E^((2*I)*a))*x*PolyLog[2, -E^((-2*I)*(a + b*x))] + 3*(1 +
E^((2*I)*a))*PolyLog[3, -E^((-2*I)*(a + b*x))])*Sec[a])/E^(I*a) + 6*b^2*x^2
*Sec[a + b*x]^2 - 12*b*x*Sec[a]*Sec[a + b*x]*Sin[b*x] - 4*b^3*x^3*Tan[a] -
12*(Log[Cos[a + b*x]] + b*x*Tan[a]))/(12*b^3)
```

fricas [C] time = 0.54, size = 240, normalized size = 1.88

$$2b^2 x^2 \tan(bx + a)^2 + 2b^2 x^2 + 2i bx \operatorname{Li}_2 \left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1 \right) - 2i bx \operatorname{Li}_2 \left(\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1 \right) - 4bx \tan(bx + a)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a)^3,x, algorithm="fricas")

[Out] 1/4*(2*b^2*x^2*tan(b*x + a)^2 + 2*b^2*x^2 + 2*I*b*x*dilog(2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) - 2*I*b*x*dilog(2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) - 4*b*x*tan(b*x + a) + 2*(b^2*x^2 - 1)*log(-2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + 2*(b^2*x^2 - 1)*log(-2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + polylog(3, (tan(b*x + a)^2 + 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + polylog(3, (tan(b*x + a)^2 - 2*I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)))/b^3

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan(bx + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a)^3,x, algorithm="giac")

[Out] integrate(x^2*tan(b*x + a)^3, x)

maple [A] time = 0.29, size = 180, normalized size = 1.41

$$-\frac{ix^3}{3} + \frac{2x \left(bx e^{2i(bx+a)} - ie^{2i(bx+a)} - i \right)}{b^2 \left(e^{2i(bx+a)} + 1 \right)^2} - \frac{2a^2 \ln \left(e^{i(bx+a)} \right)}{b^3} + \frac{4ia^3}{3b^3} + \frac{x^2 \ln \left(e^{2i(bx+a)} + 1 \right)}{b} - \frac{ix \operatorname{polylog} \left(2, -e^{2i(bx+a)} \right)}{b^2} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*tan(b*x+a)^3,x)

[Out] -1/3*I*x^3+2*x*(b*x*exp(2*I*(b*x+a))-I*exp(2*I*(b*x+a))-I)/b^2/(exp(2*I*(b*x+a))+1)^2-2/b^3*a^2*ln(exp(I*(b*x+a)))+4/3*I/b^3*a^3+x^2*ln(exp(2*I*(b*x+a))+1)/b-I*x*polylog(2,-exp(2*I*(b*x+a)))/b^2+1/2*polylog(3,-exp(2*I*(b*x+a)))/b^3-1/b^3*ln(exp(2*I*(b*x+a))+1)+2/b^3*ln(exp(I*(b*x+a)))+2*I/b^2*a^2*x

maxima [B] time = 1.18, size = 740, normalized size = 5.78

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*tan(b*x+a)^3,x, algorithm="maxima")

[Out] -1/2*(a^2*(1/(sin(b*x + a)^2 - 1) - log(sin(b*x + a)^2 - 1)) + 2*(2*(b*x + a)^3 - 6*(b*x + a)^2*a - (6*(b*x + a)^2 - 12*(b*x + a)*a + 6*((b*x + a)^2 - 2*(b*x + a)*a - 1))*cos(4*b*x + 4*a) + 12*((b*x + a)^2 - 2*(b*x + a)*a - 1)*cos(2*b*x + 2*a) + (6*I*(b*x + a)^2 - 12*I*(b*x + a)*a - 6*I)*sin(4*b*x + 4*a) + (12*I*(b*x + a)^2 - 24*I*(b*x + a)*a - 12*I)*sin(2*b*x + 2*a) - 6)*arctan2(sin(2*b*x + 2*a), cos(2*b*x + 2*a) + 1) + 2*((b*x + a)^3 - 3*(b*x + a)^2*a - 6*b*x - 6*a)*cos(4*b*x + 4*a) + (4*(b*x + a)^3 - (b*x + a)^2*(12*a - 12*I) + 12*(b*x + a)*(-2*I*a - 1) - 12*a)*cos(2*b*x + 2*a) + (6*b*x*cos(4*b*x + 4*a) + 12*b*x*cos(2*b*x + 2*a) + 6*I*b*x*sin(4*b*x + 4*a) + 12*I*b*x*sin(2*b*x + 2*a) + 6*b*x)*dilog(-e^(2*I*b*x + 2*I*a)) - (-3*I*(b*x + a)^2 + 6*I*(b*x + a)*a + (-3*I*(b*x + a)^2 + 6*I*(b*x + a)*a + 3*I)*cos(4*b*x + 4*a) + (-6*I*(b*x + a)^2 + 12*I*(b*x + a)*a + 6*I)*cos(2*b*x + 2*a) + 3*((b*x + a)^2 - 2*(b*x + a)*a - 1)*sin(4*b*x + 4*a) + 6*((b*x + a)^2 - 2*(b*x + a)*a - 1)*sin(2*b*x + 2*a) + 3*I*log(cos(2*b*x + 2*a)^2 + sin(2*b*x + 2*a)^2 + 2*cos(2*b*x + 2*a) + 1) - (-3*I*cos(4*b*x + 4*a) - 6*I*cos(2*b*x + 2*a) + 3*sin(4*b*x + 4*a) + 6*sin(2*b*x + 2*a) - 3*I)*polylog(3, -e^(2*I*b*x + 2*I*a)) - (-2*I*(b*x + a)^3 + 6*I*(b*x + a)^2*a + 12*I*b*x + 12*I*a)*sin

$(4bx + 4a) - (-4I(bx + a)^3 - 12(bx + a)^2(-Ia - 1) - (bx + a)(24a - 12I) + 12Ia)\sin(2bx + 2a) - 12a)/(-6I\cos(4bx + 4a) - 12I\cos(2bx + 2a) + 6\sin(4bx + 4a) + 12\sin(2bx + 2a) - 6I)/b^3$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x^2 \tan(a + bx)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*tan(a + b*x)^3,x)

[Out] int(x^2*tan(a + b*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan^3(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*tan(b*x+a)**3,x)

[Out] Integral(x**2*tan(a + b*x)**3, x)

3.13 $\int x \tan^3(a + bx) dx$

Optimal. Leaf size=90

$$-\frac{i\text{Li}_2\left(-e^{2i(a+bx)}\right)}{2b^2} - \frac{\tan(a+bx)}{2b^2} + \frac{x \log\left(1 + e^{2i(a+bx)}\right)}{b} + \frac{x \tan^2(a+bx)}{2b} + \frac{x}{2b} - \frac{ix^2}{2}$$

[Out] 1/2*x/b-1/2*I*x^2+x*ln(1+exp(2*I*(b*x+a)))/b-1/2*I*polylog(2,-exp(2*I*(b*x+a)))/b^2-1/2*tan(b*x+a)/b^2+1/2*x*tan(b*x+a)^2/b

Rubi [A] time = 0.10, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.700$, Rules used = {3720, 3473, 8, 3719, 2190, 2279, 2391}

$$-\frac{i\text{Li}_2\left(-e^{2i(a+bx)}\right)}{2b^2} - \frac{\tan(a+bx)}{2b^2} + \frac{x \log\left(1 + e^{2i(a+bx)}\right)}{b} + \frac{x \tan^2(a+bx)}{2b} + \frac{x}{2b} - \frac{ix^2}{2}$$

Antiderivative was successfully verified.

[In] Int[x*Tan[a + b*x]^3,x]

[Out] x/(2*b) - (I/2)*x^2 + (x*Log[1 + E^((2*I)*(a + b*x))])/b - ((I/2)*PolyLog[2, -E^((2*I)*(a + b*x))])/b^2 - Tan[a + b*x]/(2*b^2) + (x*Tan[a + b*x]^2)/(2*b)

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 2190

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_)))^(n_))], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 3473

Int[((b_)*tan[(c_) + (d_)*(x_)])^(n_), x_Symbol] := Simp[(b*(b*Tan[c + d*x])^(n - 1))/(d*(n - 1)), x] - Dist[b^2, Int[(b*Tan[c + d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1]

Rule 3719

Int[(((c_) + (d_)*(x_))^(m_))*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[(((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

```
Int[((c_.) + (d_.)*(x_.))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_.)])^(n_.), x_Symbol]
:> Simp[(b*(c + d*x)^(m*(b*Tan[e + f*x])^(n - 1)))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^(m*(b*Tan[e + f*x])^(n - 2)), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned} \int x \tan^3(a + bx) dx &= \frac{x \tan^2(a + bx)}{2b} - \frac{\int \tan^2(a + bx) dx}{2b} - \int x \tan(a + bx) dx \\ &= -\frac{ix^2}{2} - \frac{\tan(a + bx)}{2b^2} + \frac{x \tan^2(a + bx)}{2b} + 2i \int \frac{e^{2i(a+bx)} x}{1 + e^{2i(a+bx)}} dx + \frac{\int 1 dx}{2b} \\ &= \frac{x}{2b} - \frac{ix^2}{2} + \frac{x \log(1 + e^{2i(a+bx)})}{b} - \frac{\tan(a + bx)}{2b^2} + \frac{x \tan^2(a + bx)}{2b} - \frac{\int \log(1 + e^{2i(a+bx)})}{b} \\ &= \frac{x}{2b} - \frac{ix^2}{2} + \frac{x \log(1 + e^{2i(a+bx)})}{b} - \frac{\tan(a + bx)}{2b^2} + \frac{x \tan^2(a + bx)}{2b} + \frac{i \operatorname{Subst}\left(\int \frac{\log(1+x)}{x} dx\right)}{2b^2} \\ &= \frac{x}{2b} - \frac{ix^2}{2} + \frac{x \log(1 + e^{2i(a+bx)})}{b} - \frac{i \operatorname{Li}_2(-e^{2i(a+bx)})}{2b^2} - \frac{\tan(a + bx)}{2b^2} + \frac{x \tan^2(a + bx)}{2b} \end{aligned}$$

Mathematica [B] time = 6.15, size = 210, normalized size = 2.33

$$\frac{\csc(a) \sec(a) \left(b^2 x^2 e^{-i \tan^{-1}(\cot(a))} - \frac{\cot(a) \left(i \operatorname{Li}_2 \left(e^{2i(bx - \tan^{-1}(\cot(a)))} \right) + i b x (-2 \tan^{-1}(\cot(a)) - \pi) - 2(bx - \tan^{-1}(\cot(a))) \log \left(1 - e^{2i(bx - \tan^{-1}(\cot(a)))} \right) \right)}{\sqrt{\cot^2(a) + 1}} \right)}{2b^2 \sqrt{\csc^2(a) (\sin^2(a) + \cos^2(a))}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*Tan[a + b*x]^3,x]

[Out] (x*Sec[a + b*x]^2)/(2*b) + (Csc[a]*((b^2*x^2)/E^(I*ArcTan[Cot[a]])) - (Cot[a]*(I*b*x*(-Pi - 2*ArcTan[Cot[a]]) - Pi*Log[1 + E^((-2*I)*b*x)] - 2*(b*x - ArcTan[Cot[a]])*Log[1 - E^((2*I)*(b*x - ArcTan[Cot[a]])])]) + Pi*Log[Cos[b*x]] - 2*ArcTan[Cot[a]]*Log[Sin[b*x - ArcTan[Cot[a]]]]) + I*PolyLog[2, E^((2*I)*(b*x - ArcTan[Cot[a]])])])/Sqrt[1 + Cot[a]^2]*Sec[a]/(2*b^2*Sqrt[Csc[a]^2*(Cos[a]^2 + Sin[a]^2)]) - (Sec[a]*Sec[a + b*x]*Sin[b*x])/(2*b^2) - (x^2*Tan[a])/2

fricas [B] time = 0.50, size = 146, normalized size = 1.62

$$\frac{2bx \tan(bx + a)^2 + 2bx \log\left(-\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 2bx \log\left(-\frac{2(-i \tan(bx+a)-1)}{\tan(bx+a)^2+1}\right) + 2bx + i \operatorname{Li}_2\left(\frac{2(i \tan(bx+a)-1)}{\tan(bx+a)^2+1} + 1\right)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a)^3,x, algorithm="fricas")

[Out] 1/4*(2*b*x*tan(b*x + a)^2 + 2*b*x*log(-2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + 2*b*x*log(-2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1)) + 2*b*x + I*dilog(2*(I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) - I*dilog(2*(-I*tan(b*x + a) - 1)/(tan(b*x + a)^2 + 1) + 1) - 2*tan(b*x + a))/b^2

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x \tan(bx + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a)^3,x, algorithm="giac")

[Out] integrate(x*tan(b*x + a)^3, x)

maple [A] time = 0.22, size = 122, normalized size = 1.36

$$-\frac{ix^2}{2} + \frac{2bx e^{2i(bx+a)} - i e^{2i(bx+a)} - i}{b^2 (e^{2i(bx+a)} + 1)^2} - \frac{2iax}{b} - \frac{ia^2}{b^2} + \frac{x \ln(e^{2i(bx+a)} + 1)}{b} - \frac{i \operatorname{polylog}(2, -e^{2i(bx+a)})}{2b^2} + \frac{2a \ln(e^{i(bx+a)})}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*tan(b*x+a)^3,x)

[Out] $-1/2*I*x^2+(2*b*x*\exp(2*I*(b*x+a))-I*\exp(2*I*(b*x+a))-I)/b^2/(\exp(2*I*(b*x+a))+1)^2-2*I/b*a*x-I/b^2*a^2+x*\ln(\exp(2*I*(b*x+a))+1)/b-1/2*I*\operatorname{polylog}(2,-\exp(2*I*(b*x+a)))/b^2+2/b^2*a*\ln(\exp(I*(b*x+a)))$

maxima [B] time = 3.04, size = 388, normalized size = 4.31

$$\frac{b^2 x^2 \cos(4bx + 4a) + i b^2 x^2 \sin(4bx + 4a) + b^2 x^2 - (2bx \cos(4bx + 4a) + 4bx \cos(2bx + 2a) + 2ibx \sin(4bx + 4a))}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a)^3,x, algorithm="maxima")

[Out] $-(b^2 x^2 \cos(4bx + 4a) + I b^2 x^2 \sin(4bx + 4a) + b^2 x^2 - (2bx \cos(4bx + 4a) + 4bx \cos(2bx + 2a) + 2I b x \sin(4bx + 4a) + 4I b x \sin(2bx + 2a) + 2bx) \operatorname{arctan2}(\sin(2bx + 2a), \cos(2bx + 2a) + 1) + 2(b^2 x^2 + 2I b x + 1) \cos(2bx + 2a) + (\cos(4bx + 4a) + 2 \cos(2bx + 2a) + I \sin(4bx + 4a) + 2I \sin(2bx + 2a) + 1) \operatorname{dilog}(-e^{(2I b x + 2I a)}) - (-I b x \cos(4bx + 4a) - 2I b x \cos(2bx + 2a) + b x \sin(4bx + 4a) + 2b x \sin(2bx + 2a) - I b x) \log(\cos(2bx + 2a)^2 + \sin(2bx + 2a)^2 + 2 \cos(2bx + 2a) + 1) - (-2I b^2 x^2 + 4bx - 2I) \sin(2bx + 2a) + 2)/(-2I b^2 \cos(4bx + 4a) - 4I b^2 \cos(2bx + 2a) + 2b^2 \sin(4bx + 4a) + 4b^2 \sin(2bx + 2a) - 2I b^2)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int x \tan(a + bx)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*tan(a + b*x)^3,x)

[Out] int(x*tan(a + b*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x \tan^3(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*tan(b*x+a)**3,x)

[Out] Integral(x*tan(a + b*x)**3, x)

$$3.14 \quad \int \frac{\tan^3(a+bx)}{x} dx$$

Optimal. Leaf size=15

$$\text{Int}\left(\frac{\tan^3(a+bx)}{x}, x\right)$$

[Out] Unintegrable(tan(b*x+a)^3/x, x)

Rubi [A] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\tan^3(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[Tan[a + b*x]^3/x, x]

[Out] Defer[Int][Tan[a + b*x]^3/x, x]

Rubi steps

$$\int \frac{\tan^3(a+bx)}{x} dx = \int \frac{\tan^3(a+bx)}{x} dx$$

Mathematica [A] time = 5.12, size = 0, normalized size = 0.00

$$\int \frac{\tan^3(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[Tan[a + b*x]^3/x, x]

[Out] Integrate[Tan[a + b*x]^3/x, x]

fricas [A] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\tan(bx+a)^3}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^3/x, x, algorithm="fricas")

[Out] integral(tan(b*x + a)^3/x, x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)^3}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^3/x, x, algorithm="giac")

[Out] integrate(tan(b*x + a)^3/x, x)

maple [A] time = 1.21, size = 0, normalized size = 0.00

$$\int \frac{\tan^3(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(b*x+a)^3/x,x)

[Out] int(tan(b*x+a)^3/x,x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$4bx \cos(2bx + 2a)^2 + 4bx \sin(2bx + 2a)^2 + 2bx \cos(2bx + 2a) + (2bx \cos(2bx + 2a) - \sin(2bx + 2a)) \cos$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^3/x,x, algorithm="maxima")

[Out] (4*b*x*cos(2*b*x + 2*a)^2 + 4*b*x*sin(2*b*x + 2*a)^2 + 2*b*x*cos(2*b*x + 2*a) + (2*b*x*cos(2*b*x + 2*a) - sin(2*b*x + 2*a))*cos(4*b*x + 4*a) - (b^2*x^2*cos(4*b*x + 4*a)^2 + 4*b^2*x^2*cos(2*b*x + 2*a)^2 + b^2*x^2*sin(4*b*x + 4*a)^2 + 4*b^2*x^2*sin(4*b*x + 4*a)*sin(2*b*x + 2*a) + 4*b^2*x^2*sin(2*b*x + 2*a)^2 + 4*b^2*x^2*cos(2*b*x + 2*a) + b^2*x^2 + 2*(2*b^2*x^2*cos(2*b*x + 2*a) + b^2*x^2)*cos(4*b*x + 4*a))*integrate(2*(b^2*x^2 - 1)*sin(2*b*x + 2*a)/(b^2*x^3*cos(2*b*x + 2*a)^2 + b^2*x^3*sin(2*b*x + 2*a)^2 + 2*b^2*x^3*cos(2*b*x + 2*a) + b^2*x^3), x) + (2*b*x*sin(2*b*x + 2*a) + cos(2*b*x + 2*a) + 1)*sin(4*b*x + 4*a) + sin(2*b*x + 2*a))/(b^2*x^2*cos(4*b*x + 4*a)^2 + 4*b^2*x^2*cos(2*b*x + 2*a)^2 + b^2*x^2*sin(4*b*x + 4*a)^2 + 4*b^2*x^2*sin(4*b*x + 4*a)*sin(2*b*x + 2*a) + 4*b^2*x^2*sin(2*b*x + 2*a)^2 + 4*b^2*x^2*cos(2*b*x + 2*a) + b^2*x^2 + 2*(2*b^2*x^2*cos(2*b*x + 2*a) + b^2*x^2)*cos(4*b*x + 4*a))

mupad [A] time = 0.00, size = -1, normalized size = -0.07

$$\int \frac{\tan(a + bx)^3}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(a + b*x)^3/x,x)

[Out] int(tan(a + b*x)^3/x, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan^3(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)**3/x,x)

[Out] Integral(tan(a + b*x)**3/x, x)

$$3.15 \quad \int \frac{\tan^3(a+bx)}{x^2} dx$$

Optimal. Leaf size=15

$$\text{Int}\left(\frac{\tan^3(a+bx)}{x^2}, x\right)$$

[Out] Unintegrable(tan(b*x+a)^3/x^2, x)

Rubi [A] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\tan^3(a+bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[Tan[a + b*x]^3/x^2, x]

[Out] Defer[Int][Tan[a + b*x]^3/x^2, x]

Rubi steps

$$\int \frac{\tan^3(a+bx)}{x^2} dx = \int \frac{\tan^3(a+bx)}{x^2} dx$$

Mathematica [A] time = 3.42, size = 0, normalized size = 0.00

$$\int \frac{\tan^3(a+bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[Tan[a + b*x]^3/x^2, x]

[Out] Integrate[Tan[a + b*x]^3/x^2, x]

fricas [A] time = 0.57, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{\tan(bx+a)^3}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^3/x^2, x, algorithm="fricas")

[Out] integral(tan(b*x + a)^3/x^2, x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan(bx+a)^3}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^3/x^2, x, algorithm="giac")

[Out] integrate(tan(b*x + a)^3/x^2, x)

maple [A] time = 1.36, size = 0, normalized size = 0.00

$$\int \frac{\tan^3(bx + a)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(b*x+a)^3/x^2,x)

[Out] int(tan(b*x+a)^3/x^2,x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$4bx \cos(2bx + 2a)^2 + 4bx \sin(2bx + 2a)^2 + 2bx \cos(2bx + 2a) + 2(bx \cos(2bx + 2a) - \sin(2bx + 2a)) \cos$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)^3/x^2,x, algorithm="maxima")

[Out] (4*b*x*cos(2*b*x + 2*a)^2 + 4*b*x*sin(2*b*x + 2*a)^2 + 2*b*x*cos(2*b*x + 2*a) + 2*(b*x*cos(2*b*x + 2*a) - sin(2*b*x + 2*a))*cos(4*b*x + 4*a) - (b^2*x^3*cos(4*b*x + 4*a)^2 + 4*b^2*x^3*cos(2*b*x + 2*a)^2 + b^2*x^3*sin(4*b*x + 4*a)^2 + 4*b^2*x^3*sin(4*b*x + 4*a)*sin(2*b*x + 2*a) + 4*b^2*x^3*sin(2*b*x + 2*a)^2 + 4*b^2*x^3*cos(2*b*x + 2*a) + b^2*x^3 + 2*(2*b^2*x^3*cos(2*b*x + 2*a) + b^2*x^3)*cos(4*b*x + 4*a))*integrate(2*(b^2*x^2 - 3)*sin(2*b*x + 2*a)/(b^2*x^4*cos(2*b*x + 2*a)^2 + b^2*x^4*sin(2*b*x + 2*a)^2 + 2*b^2*x^4*cos(2*b*x + 2*a) + b^2*x^4), x) + 2*(b*x*sin(2*b*x + 2*a) + cos(2*b*x + 2*a) + 1)*sin(4*b*x + 4*a) + 2*sin(2*b*x + 2*a))/(b^2*x^3*cos(4*b*x + 4*a)^2 + 4*b^2*x^3*cos(2*b*x + 2*a)^2 + b^2*x^3*sin(4*b*x + 4*a)^2 + 4*b^2*x^3*sin(4*b*x + 4*a)*sin(2*b*x + 2*a) + 4*b^2*x^3*sin(2*b*x + 2*a)^2 + 4*b^2*x^3*cos(2*b*x + 2*a) + b^2*x^3 + 2*(2*b^2*x^3*cos(2*b*x + 2*a) + b^2*x^3)*cos(4*b*x + 4*a))

mupad [A] time = 0.00, size = -1, normalized size = -0.07

$$\int \frac{\tan(a + bx)^3}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(a + b*x)^3/x^2,x)

[Out] int(tan(a + b*x)^3/x^2, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\tan^3(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(tan(b*x+a)**3/x**2,x)

[Out] Integral(tan(a + b*x)**3/x**2, x)

$$3.16 \quad \int \left(\frac{x^2}{\tan^{\frac{3}{2}}(a+bx)} - \frac{4x}{b\sqrt{\tan(a+bx)}} + x^2\sqrt{\tan(a+bx)} \right) dx$$

Optimal. Leaf size=18

$$-\frac{2x^2}{b\sqrt{\tan(a+bx)}}$$

[Out] $-2*x^2/b/\tan(b*x+a)^{(1/2)}$

Rubi [A] time = 0.12, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 1, integrand size = 45, $\frac{\text{number of rules}}{\text{integrand size}} = 0.022$, Rules used = {3721}

$$-\frac{2x^2}{b\sqrt{\tan(a+bx)}}$$

Antiderivative was successfully verified.

[In] Int[x^2/Tan[a + b*x]^(3/2) - (4*x)/(b*Sqrt[Tan[a + b*x]]) + x^2*Sqrt[Tan[a + b*x]], x]

[Out] $(-2*x^2)/(b*Sqrt[Tan[a + b*x]])$

Rule 3721

Int[((c_.) + (d_.)*(x_.))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_.)])^(n_.), x_Symbol] :> Simp[((c + d*x)^m*(b*Tan[e + f*x])^(n + 1))/(b*f*(n + 1)), x] + (-Dist[(d*m)/(b*f*(n + 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n + 1), x], x] - Dist[1/b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n + 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && LtQ[n, -1] && GtQ[m, 0]

Rubi steps

$$\int \left(\frac{x^2}{\tan^{\frac{3}{2}}(a+bx)} - \frac{4x}{b\sqrt{\tan(a+bx)}} + x^2\sqrt{\tan(a+bx)} \right) dx = -\frac{4 \int \frac{x}{\sqrt{\tan(a+bx)}} dx}{b} + \int \frac{x^2}{\tan^{\frac{3}{2}}(a+bx)} dx + \int x^2 \sqrt{\tan(a+bx)} dx$$

$$= -\frac{2x^2}{b\sqrt{\tan(a+bx)}}$$

Mathematica [A] time = 0.96, size = 18, normalized size = 1.00

$$-\frac{2x^2}{b\sqrt{\tan(a+bx)}}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/Tan[a + b*x]^(3/2) - (4*x)/(b*Sqrt[Tan[a + b*x]]) + x^2*Sqrt[Tan[a + b*x]], x]

[Out] $(-2*x^2)/(b*Sqrt[Tan[a + b*x]])$

fricas [A] time = 0.61, size = 16, normalized size = 0.89

$$-\frac{2x^2}{b\sqrt{\tan(bx+a)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-4*x/b/tan(b*x+a)^(1/2)+x^2*tan(b*x+a)^(1/2)+x^2/tan(b*x+a)^(3/2), x, algorithm="fricas")

[Out] -2*x^2/(b*sqrt(tan(b*x + a)))

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \sqrt{\tan(bx + a)} + \frac{x^2}{\tan(bx + a)^{\frac{3}{2}}} - \frac{4x}{b\sqrt{\tan(bx + a)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-4*x/b/tan(b*x+a)^(1/2)+x^2*tan(b*x+a)^(1/2)+x^2/tan(b*x+a)^(3/2), x, algorithm="giac")

[Out] integrate(x^2*sqrt(tan(b*x + a)) + x^2/tan(b*x + a)^(3/2) - 4*x/(b*sqrt(tan(b*x + a))), x)

maple [F] time = 0.87, size = 0, normalized size = 0.00

$$\int -\frac{4x}{b\sqrt{\tan(bx + a)}} + x^2 (\sqrt{\tan(bx + a)}) + \frac{x^2}{\tan(bx + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(-4*x/b/tan(b*x+a)^(1/2)+x^2*tan(b*x+a)^(1/2)+x^2/tan(b*x+a)^(3/2), x)

[Out] int(-4*x/b/tan(b*x+a)^(1/2)+x^2*tan(b*x+a)^(1/2)+x^2/tan(b*x+a)^(3/2), x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \sqrt{\tan(bx + a)} + \frac{x^2}{\tan(bx + a)^{\frac{3}{2}}} - \frac{4x}{b\sqrt{\tan(bx + a)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(-4*x/b/tan(b*x+a)^(1/2)+x^2*tan(b*x+a)^(1/2)+x^2/tan(b*x+a)^(3/2), x, algorithm="maxima")

[Out] integrate(x^2*sqrt(tan(b*x + a)) + x^2/tan(b*x + a)^(3/2) - 4*x/(b*sqrt(tan(b*x + a))), x)

mupad [B] time = 3.12, size = 50, normalized size = 2.78

$$-\frac{x^2 \sin(2a + 2bx) \sqrt{\frac{\sin(2a + 2bx)}{\cos(2a + 2bx) + 1}}}{b \sin(a + bx)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*tan(a + b*x)^(1/2) + x^2/tan(a + b*x)^(3/2) - (4*x)/(b*tan(a + b*x)^(1/2)), x)

[Out] -(x^2*sin(2*a + 2*b*x)*(sin(2*a + 2*b*x)/(cos(2*a + 2*b*x) + 1))^(1/2))/(b*sin(a + b*x)^2)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \left(-\frac{4x}{\sqrt{\tan(a+bx)}} \right) dx + \int \frac{bx^2}{\tan^{\frac{3}{2}}(a+bx)} dx + \int bx^2 \sqrt{\tan(a+bx)} dx}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-4*x/b/tan(b*x+a)**(1/2)+x**2*tan(b*x+a)**(1/2)+x**2/tan(b*x+a)**(3/2),x)
```

```
[Out] (Integral(-4*x/sqrt(tan(a + b*x)), x) + Integral(b*x**2/tan(a + b*x)**(3/2), x) + Integral(b*x**2*sqrt(tan(a + b*x)), x))/b
```

$$3.17 \quad \int \left(\frac{x^2}{\sqrt{\tan(ax+bx^2)}} + \frac{\sqrt{\tan(ax+bx^2)}}{b} + x^2 \tan^{\frac{3}{2}}(ax+bx^2) \right) dx$$

Optimal. Leaf size=17

$$\frac{x\sqrt{\tan(ax+bx^2)}}{b}$$

[Out] x*tan(b*x^2+a)^(1/2)/b

Rubi [F] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \left(\frac{x^2}{\sqrt{\tan(ax+bx^2)}} + \frac{\sqrt{\tan(ax+bx^2)}}{b} + x^2 \tan^{\frac{3}{2}}(ax+bx^2) \right) dx$$

Verification is Not applicable to the result.

[In] Int[x^2/Sqrt[Tan[a + b*x^2]] + Sqrt[Tan[a + b*x^2]]/b + x^2*Tan[a + b*x^2]^(3/2), x]

[Out] Defer[Int][x^2/Sqrt[Tan[a + b*x^2]], x] + Defer[Int][Sqrt[Tan[a + b*x^2]], x]/b + Defer[Int][x^2*Tan[a + b*x^2]^(3/2), x]

Rubi steps

$$\int \left(\frac{x^2}{\sqrt{\tan(ax+bx^2)}} + \frac{\sqrt{\tan(ax+bx^2)}}{b} + x^2 \tan^{\frac{3}{2}}(ax+bx^2) \right) dx = \frac{\int \sqrt{\tan(ax+bx^2)} dx}{b} + \int \frac{x^2}{\sqrt{\tan(ax+bx^2)}} dx$$

Mathematica [A] time = 0.60, size = 17, normalized size = 1.00

$$\frac{x\sqrt{\tan(ax+bx^2)}}{b}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/Sqrt[Tan[a + b*x^2]] + Sqrt[Tan[a + b*x^2]]/b + x^2*Tan[a + b*x^2]^(3/2), x]

[Out] (x*Sqrt[Tan[a + b*x^2]])/b

fricas [A] time = 0.86, size = 15, normalized size = 0.88

$$\frac{x\sqrt{\tan(bx^2+a)}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/tan(b*x^2+a)^(1/2)+tan(b*x^2+a)^(1/2)/b+x^2*tan(b*x^2+a)^(3/2), x, algorithm="fricas")

[Out] x*sqrt(tan(b*x^2 + a))/b

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan(bx^2 + a)^{\frac{3}{2}} + \frac{x^2}{\sqrt{\tan(bx^2 + a)}} + \frac{\sqrt{\tan(bx^2 + a)}}{b} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/tan(b*x^2+a)^(1/2)+tan(b*x^2+a)^(1/2)/b+x^2*tan(b*x^2+a)^(3/2),x, algorithm="giac")

[Out] integrate(x^2*tan(b*x^2 + a)^(3/2) + x^2/sqrt(tan(b*x^2 + a)) + sqrt(tan(b*x^2 + a))/b, x)

maple [F] time = 1.06, size = 0, normalized size = 0.00

$$\int \frac{x^2}{\sqrt{\tan(bx^2 + a)}} + \frac{\sqrt{\tan(bx^2 + a)}}{b} + x^2 \left(\tan^{\frac{3}{2}}(bx^2 + a) \right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/tan(b*x^2+a)^(1/2)+tan(b*x^2+a)^(1/2)/b+x^2*tan(b*x^2+a)^(3/2),x)

[Out] int(x^2/tan(b*x^2+a)^(1/2)+tan(b*x^2+a)^(1/2)/b+x^2*tan(b*x^2+a)^(3/2),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \tan(bx^2 + a)^{\frac{3}{2}} + \frac{x^2}{\sqrt{\tan(bx^2 + a)}} + \frac{\sqrt{\tan(bx^2 + a)}}{b} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/tan(b*x^2+a)^(1/2)+tan(b*x^2+a)^(1/2)/b+x^2*tan(b*x^2+a)^(3/2),x, algorithm="maxima")

[Out] integrate(x^2*tan(b*x^2 + a)^(3/2) + x^2/sqrt(tan(b*x^2 + a)) + sqrt(tan(b*x^2 + a))/b, x)

mupad [B] time = 4.17, size = 45, normalized size = 2.65

$$\frac{x \sqrt{\frac{e^{2i b x^2 + a 2i} 1i - i}{e^{2i b x^2 + a 2i} + 1}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(tan(a + b*x^2)^(1/2)/b + x^2/tan(a + b*x^2)^(1/2) + x^2*tan(a + b*x^2)^(3/2),x)

[Out] (x*(-(exp(a*2i + b*x^2*2i)*1i - 1i)/(exp(a*2i + b*x^2*2i) + 1))^(1/2))/b

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{bx^2}{\sqrt{\tan(a+bx^2)}} dx + \int bx^2 \tan^{\frac{3}{2}}(a + bx^2) dx + \int \sqrt{\tan(a + bx^2)} dx}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/tan(b*x**2+a)**(1/2)+tan(b*x**2+a)**(1/2)/b+x**2*tan(b*x**2+a)**(3/2),x)

[Out] (Integral(b*x**2/sqrt(tan(a + b*x**2)), x) + Integral(b*x**2*tan(a + b*x**2)**(3/2), x) + Integral(sqrt(tan(a + b*x**2)), x))/b

$$3.18 \quad \int \frac{(c+dx)^3}{a+ia \tan(e+fx)} dx$$

Optimal. Leaf size=189

$$-\frac{3id^2(c+dx)}{4f^3(a+ia \tan(e+fx))} + \frac{3d(c+dx)^2}{4f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)^3}{2f(a+ia \tan(e+fx))} - \frac{3d(c+dx)^2}{8af^2} - \frac{i(c+dx)^3}{4af} + \frac{(c+dx)^4}{8ad}$$

[Out] $3/8*I*d^3*x/a/f^3-3/8*d*(d*x+c)^2/a/f^2-1/4*I*(d*x+c)^3/a/f+1/8*(d*x+c)^4/a/d-3/8*d^3/f^4/(a+I*a*\tan(f*x+e))-3/4*I*d^2*(d*x+c)/f^3/(a+I*a*\tan(f*x+e))+3/4*d*(d*x+c)^2/f^2/(a+I*a*\tan(f*x+e))+1/2*I*(d*x+c)^3/f/(a+I*a*\tan(f*x+e))$

Rubi [A] time = 0.20, antiderivative size = 189, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {3723, 3479, 8}

$$-\frac{3id^2(c+dx)}{4f^3(a+ia \tan(e+fx))} + \frac{3d(c+dx)^2}{4f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)^3}{2f(a+ia \tan(e+fx))} - \frac{3d(c+dx)^2}{8af^2} - \frac{i(c+dx)^3}{4af} + \frac{(c+dx)^4}{8ad}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + I*a*Tan[e + f*x]), x]

[Out] $((3*I)/8)*d^3*x/(a*f^3) - (3*d*(c + d*x)^2)/(8*a*f^2) - ((I/4)*(c + d*x)^3)/(a*f) + (c + d*x)^4/(8*a*d) - (3*d^3)/(8*f^4*(a + I*a*\tan[e + f*x])) - ((3*I)/4)*d^2*(c + d*x)/(f^3*(a + I*a*\tan[e + f*x])) + (3*d*(c + d*x)^2)/(4*f^2*(a + I*a*\tan[e + f*x])) + ((I/2)*(c + d*x)^3)/(f*(a + I*a*\tan[e + f*x]))$

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 3479

Int[((a_) + (b_.)*tan[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := Simp[(a*(a + b*Tan[c + d*x])^n)/(2*b*d*n), x] + Dist[1/(2*a), Int[(a + b*Tan[c + d*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[a^2 + b^2, 0] && LtQ[n, 0]

Rule 3723

Int[((c_.) + (d_.)*(x_))^(m_.)/((a_) + (b_.)*tan[(e_.) + (f_.)*(x_)]), x_Symbol] := Simp[(c + d*x)^(m + 1)/(2*a*d*(m + 1)), x] + (Dist[(a*d*m)/(2*b*f), Int[(c + d*x)^(m - 1)/(a + b*Tan[e + f*x]), x], x] - Simp[(a*(c + d*x)^m)/(2*b*f*(a + b*Tan[e + f*x])), x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^3}{a+ia \tan(e+fx)} dx &= \frac{(c+dx)^4}{8ad} + \frac{i(c+dx)^3}{2f(a+ia \tan(e+fx))} - \frac{(3id) \int \frac{(c+dx)^2}{a+ia \tan(e+fx)} dx}{2f} \\
&= -\frac{i(c+dx)^3}{4af} + \frac{(c+dx)^4}{8ad} + \frac{3d(c+dx)^2}{4f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)^3}{2f(a+ia \tan(e+fx))} - \frac{(3d^2)}{4f^3(a+ia \tan(e+fx))} \\
&= -\frac{3d(c+dx)^2}{8af^2} - \frac{i(c+dx)^3}{4af} + \frac{(c+dx)^4}{8ad} - \frac{3id^2(c+dx)}{4f^3(a+ia \tan(e+fx))} + \frac{3d(c+dx)}{4f^2(a+ia \tan(e+fx))} \\
&= -\frac{3d(c+dx)^2}{8af^2} - \frac{i(c+dx)^3}{4af} + \frac{(c+dx)^4}{8ad} - \frac{3d^3}{8f^4(a+ia \tan(e+fx))} - \frac{3id^2(c+dx)}{4f^3(a+ia \tan(e+fx))} \\
&= \frac{3id^3x}{8af^3} - \frac{3d(c+dx)^2}{8af^2} - \frac{i(c+dx)^3}{4af} + \frac{(c+dx)^4}{8ad} - \frac{3d^3}{8f^4(a+ia \tan(e+fx))} - \frac{3id^2(c+dx)}{4f^3(a+ia \tan(e+fx))}
\end{aligned}$$

Mathematica [A] time = 0.71, size = 278, normalized size = 1.47

$$\frac{\sec(e+fx)(\cos(fx) + i \sin(fx)) (2f^4x (4c^3 + 6c^2dx + 4cd^2x^2 + d^3x^3) (\cos(e) + i \sin(e)) + (\cos(e) - i \sin(e)) c)}{16af^4}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + I*a*Tan[e + f*x]),x]

[Out] (Sec[e + f*x]*(Cos[f*x] + I*Sin[f*x])*(((4*I)*c^3*f^3 + 6*c^2*d*f^2*(1 + (2*I)*f*x) + 6*c*d^2*f*(-I + 2*f*x + (2*I)*f^2*x^2) + d^3*(-3 - (6*I)*f*x + 6*f^2*x^2 + (4*I)*f^3*x^3))*Cos[2*f*x]*(Cos[e] - I*Sin[e]) + 2*f^4*x*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d^3*x^3)*(Cos[e] + I*Sin[e]) + (4*c^3*f^3 + 6*c^2*d*f^2*(-I + 2*f*x) + 6*c*d^2*f*(-1 - (2*I)*f*x + 2*f^2*x^2) + d^3*(3*I - 6*f*x - (6*I)*f^2*x^2 + 4*f^3*x^3))*(Cos[e] - I*Sin[e])*Sin[2*f*x]))/(16*f^4*(a + I*a*Tan[e + f*x]))

fricas [A] time = 0.51, size = 162, normalized size = 0.86

$$\frac{(4i d^3 f^3 x^3 + 4i c^3 f^3 + 6 c^2 d f^2 - 6i c d^2 f - 3 d^3 + (12i c d^2 f^3 + 6 d^3 f^2) x^2 + (12i c^2 d f^3 + 12 c d^2 f^2 - 6i d^3 f) x + 3 d^3)}{16 a f^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/16*(4*I*d^3*f^3*x^3 + 4*I*c^3*f^3 + 6*c^2*d*f^2 - 6*I*c*d^2*f - 3*d^3 + (12*I*c*d^2*f^3 + 6*d^3*f^2)*x^2 + (12*I*c^2*d*f^3 + 12*c*d^2*f^2 - 6*I*d^3*f)*x + 2*(d^3*f^4*x^4 + 4*c*d^2*f^4*x^3 + 6*c^2*d*f^4*x^2 + 4*c^3*f^4*x)*e^(2*I*f*x + 2*I*e))*e^(-2*I*f*x - 2*I*e)/(a*f^4)

giac [A] time = 0.67, size = 193, normalized size = 1.02

$$\frac{(2 d^3 f^4 x^4 e^{(2i f x + 2i e)} + 8 c d^2 f^4 x^3 e^{(2i f x + 2i e)} + 12 c^2 d f^4 x^2 e^{(2i f x + 2i e)} + 4i d^3 f^3 x^3 + 8 c^3 f^4 x e^{(2i f x + 2i e)} + 12i c d^2 f^3)}{16 a f^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] 1/16*(2*d^3*f^4*x^4*e^(2*I*f*x + 2*I*e) + 8*c*d^2*f^4*x^3*e^(2*I*f*x + 2*I*e) + 12*c^2*d*f^4*x^2*e^(2*I*f*x + 2*I*e) + 4*I*d^3*f^3*x^3 + 8*c^3*f^4*x*e

$$\begin{aligned} & \frac{(2I^2fx + 2I^2e) + 12I^2cd^2f^3x^2 + 12I^2c^2d^2f^3x + 6d^3f^2x^2 + 4I^2c^3f^3 + 12c^2d^2f^2x + 6c^2d^2f^2 - 6I^2d^3fx - 6I^2cd^2f - 3d^3}{e^{(-2I^2fx - 2I^2e)/(af^4)}} \end{aligned}$$

maple [B] time = 0.65, size = 1061, normalized size = 5.61

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(a+I*a*tan(f*x+e)),x)

[Out] $\frac{1}{af} \left(-\frac{3}{2} \frac{I}{f} c^2 d e \cos(fx+e)^2 + \frac{1}{2} I c^3 \cos(fx+e)^2 - 3 \frac{I}{f^3} d^3 e^2 \right. \\ \left. * \left(-\frac{1}{2} (fx+e) \cos(fx+e)^2 + \frac{1}{4} \sin(fx+e) \cos(fx+e) + \frac{1}{4} fx + \frac{1}{4} e \right) - \frac{1}{f^3} d^3 * \left(-\frac{1}{2} (fx+e)^3 \cos(fx+e)^2 + \frac{3}{2} (fx+e)^2 \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) + \frac{3}{4} (fx+e) \cos(fx+e)^2 - \frac{3}{8} \sin(fx+e) \cos(fx+e) - \frac{3}{8} fx - \frac{3}{8} e - \frac{1}{2} (fx+e)^3 \right) + \frac{3}{2} \frac{I}{f^2} c^2 d^2 e^2 \cos(fx+e)^2 - 3 \frac{I}{f} c^2 d * \left(-\frac{1}{2} (fx+e) \cos(fx+e)^2 + \frac{1}{4} \sin(fx+e) \cos(fx+e) + \frac{1}{4} fx + \frac{1}{4} e \right) + 3 \frac{I}{f^3} d^3 e * \left(-\frac{1}{2} (fx+e)^2 \cos(fx+e)^2 + (fx+e) \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) - \frac{1}{4} (fx+e)^2 - \frac{1}{4} \sin(fx+e)^2 \right) + 6 \frac{I}{f^2} c^2 d^2 e * \left(-\frac{1}{2} (fx+e) \cos(fx+e)^2 + \frac{1}{4} \sin(fx+e) \cos(fx+e) + \frac{1}{4} fx + \frac{1}{4} e \right) - \frac{1}{2} \frac{I}{f^3} d^3 e^3 \cos(fx+e)^2 - 3 \frac{I}{f^2} c^2 d^2 * \left(-\frac{1}{2} (fx+e)^2 \cos(fx+e)^2 + (fx+e) \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) - \frac{1}{4} (fx+e)^2 - \frac{1}{4} \sin(fx+e)^2 \right) + \frac{1}{f^3} d^3 * \left((fx+e)^3 \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) + \frac{3}{4} (fx+e)^2 \cos(fx+e)^2 - \frac{3}{2} (fx+e) * \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) + \frac{3}{8} (fx+e)^2 + \frac{3}{8} \sin(fx+e)^2 - \frac{3}{8} (fx+e)^4 \right) + \frac{3}{f^2} c^2 d^2 * \left((fx+e)^2 \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) + \frac{1}{2} (fx+e) \cos(fx+e)^2 - \frac{1}{4} \sin(fx+e) \cos(fx+e) - \frac{1}{4} fx - \frac{1}{4} e - \frac{1}{3} (fx+e)^3 \right) - \frac{3}{f^3} d^3 e * \left((fx+e)^2 \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) + \frac{1}{2} (fx+e) \cos(fx+e)^2 - \frac{1}{4} \sin(fx+e) \cos(fx+e) - \frac{1}{4} fx - \frac{1}{4} e - \frac{1}{3} (fx+e)^3 \right) + \frac{3}{f} c^2 d * \left((fx+e) \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) - \frac{1}{4} (fx+e)^2 - \frac{1}{4} \sin(fx+e)^2 \right) - \frac{6}{f^2} c^2 d^2 e * \left((fx+e) \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) - \frac{1}{4} (fx+e)^2 - \frac{1}{4} \sin(fx+e)^2 \right) + \frac{3}{f^3} d^3 e^2 * \left((fx+e) \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) - \frac{1}{4} (fx+e)^2 - \frac{1}{4} \sin(fx+e)^2 \right) + c^3 * \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) - \frac{3}{f} c^2 d^2 e * \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) + \frac{3}{f^2} c^2 d^2 e^2 * \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) - \frac{1}{f^3} d^3 e^3 * \left(\frac{1}{2} \sin(fx+e) \cos(fx+e) + \frac{1}{2} fx + \frac{1}{2} e \right) \right)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e)),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima: expt: undefined: 0 to a negative exponent.

mupad [B] time = 3.56, size = 423, normalized size = 2.24

$$\frac{8c^3 f^4 x - 3d^3 \cos(2e + 2fx) + 4c^3 f^3 \sin(2e + 2fx) + 2d^3 f^4 x^4 + 6c^2 d f^2 \cos(2e + 2fx) + 12c^2 d f^4 x^2}{}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + a*tan(e + f*x)*1i),x)

[Out] $(d^3 \sin(2e + 2fx) * 3i - 3d^3 \cos(2e + 2fx) + 8c^3 f^4 x + c^3 f^3 \cos(2e + 2fx) * 4i + 4c^3 f^3 \sin(2e + 2fx) + 2d^3 f^4 x^4 + 6c^2 d f^2 \cos(2e + 2fx) - c^2 d f^2 \sin(2e + 2fx) * 6i + 12c^2 d f^4 x^2 + 8c^2 d^2 f^4 x^3 + 6d^3 f^2 x^2 \cos(2e + 2fx) + d^3 f^3 x^3 \cos(2e + 2fx) * 4i - d^3 f^2 x^2 \sin(2e + 2fx) * 6i + 4d^3 f^3 x^3 \sin(2e + 2fx) -$

$$\frac{c^2 d^2 f \cos(2e + 2fx) 6i - 6 c^2 d^2 f \sin(2e + 2fx) - d^3 f^2 \cos(2e + 2fx) 6i - 6 d^3 f^2 \sin(2e + 2fx) + 12 c^2 d^2 f^2 x \cos(2e + 2fx) + c^2 d^2 f^3 x \cos(2e + 2fx) 12i - c^2 d^2 f^2 x \sin(2e + 2fx) 12i + 12 c^2 d^2 f^3 x \sin(2e + 2fx) + c^2 d^2 f^3 x^2 \cos(2e + 2fx) 12i + 12 c^2 d^2 f^3 x^2 \sin(2e + 2fx)}{(16 a f^4)}$$

sympy [A] time = 0.38, size = 262, normalized size = 1.39

$$\begin{cases} \frac{(-4ic^3f^3 - 12ic^2df^3x - 6c^2df^2 - 12icd^2f^3x^2 - 12cd^2f^2x + 6icd^2f - 4id^3f^3x^3 - 6d^3f^2x^2 + 6id^3fx + 3d^3)e^{-2ie}e^{-2ifx}}{16af^4} & \text{for } 16af^4e^{2ie} \neq 0 \\ \frac{c^3xe^{-2ie}}{2a} + \frac{3c^2dx^2e^{-2ie}}{4a} + \frac{cd^2x^3e^{-2ie}}{2a} + \frac{d^3x^4e^{-2ie}}{8a} & \text{otherwise} \end{cases} + \frac{c^3x}{2a} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(a+I*a*tan(f*x+e)),x)

[Out] Piecewise((-(-4*I*c**3*f**3 - 12*I*c**2*d*f**3*x - 6*c**2*d*f**2 - 12*I*c*d**2*f**3*x**2 - 12*c*d**2*f**2*x + 6*I*c*d**2*f - 4*I*d**3*f**3*x**3 - 6*d**3*f**2*x**2 + 6*I*d**3*f*x + 3*d**3)*exp(-2*I*e)*exp(-2*I*f*x)/(16*a*f**4), Ne(16*a*f**4*exp(2*I*e), 0)), (c**3*x*exp(-2*I*e)/(2*a) + 3*c**2*d*x**2*exp(-2*I*e)/(4*a) + c*d**2*x**3*exp(-2*I*e)/(2*a) + d**3*x**4*exp(-2*I*e)/(8*a), True)) + c**3*x/(2*a) + 3*c**2*d*x**2/(4*a) + c*d**2*x**3/(2*a) + d**3*x**4/(8*a)

$$3.19 \quad \int \frac{(c+dx)^2}{a+ia \tan(e+fx)} dx$$

Optimal. Leaf size=137

$$\frac{d(c+dx)}{2f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)^2}{2f(a+ia \tan(e+fx))} - \frac{i(c+dx)^2}{4af} + \frac{(c+dx)^3}{6ad} - \frac{id^2}{4f^3(a+ia \tan(e+fx))} - \frac{d^2x}{4af^2}$$

[Out] $-1/4*d^2*x/a/f^2-1/4*I*(d*x+c)^2/a/f+1/6*(d*x+c)^3/a/d-1/4*I*d^2/f^3/(a+I*a*\tan(f*x+e))+1/2*d*(d*x+c)/f^2/(a+I*a*\tan(f*x+e))+1/2*I*(d*x+c)^2/f/(a+I*a*\tan(f*x+e))$

Rubi [A] time = 0.12, antiderivative size = 137, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {3723, 3479, 8}

$$\frac{d(c+dx)}{2f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)^2}{2f(a+ia \tan(e+fx))} - \frac{i(c+dx)^2}{4af} + \frac{(c+dx)^3}{6ad} - \frac{id^2}{4f^3(a+ia \tan(e+fx))} - \frac{d^2x}{4af^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + I*a*Tan[e + f*x]), x]

[Out] $-(d^2*x)/(4*a*f^2) - ((I/4)*(c + d*x)^2)/(a*f) + (c + d*x)^3/(6*a*d) - ((I/4)*d^2)/(f^3*(a + I*a*Tan[e + f*x])) + (d*(c + d*x))/(2*f^2*(a + I*a*Tan[e + f*x])) + ((I/2)*(c + d*x)^2)/(f*(a + I*a*Tan[e + f*x]))$

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 3479

Int[((a_) + (b_)*tan[(c_) + (d_)*(x_)])^(n_), x_Symbol] := Simp[(a*(a + b*Tan[c + d*x])^n)/(2*b*d*n), x] + Dist[1/(2*a), Int[(a + b*Tan[c + d*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[a^2 + b^2, 0] && LtQ[n, 0]

Rule 3723

Int[((c_) + (d_)*(x_))^(m_)/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c + d*x)^(m + 1)/(2*a*d*(m + 1)), x] + (Dist[(a*d*m)/(2*b*f), Int[(c + d*x)^(m - 1)/(a + b*Tan[e + f*x]), x], x] - Simp[(a*(c + d*x)^m)/(2*b*f*(a + b*Tan[e + f*x])), x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && GtQ[m, 0]

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^2}{a+ia \tan(e+fx)} dx &= \frac{(c+dx)^3}{6ad} + \frac{i(c+dx)^2}{2f(a+ia \tan(e+fx))} - \frac{(id) \int \frac{c+dx}{a+ia \tan(e+fx)} dx}{f} \\ &= -\frac{i(c+dx)^2}{4af} + \frac{(c+dx)^3}{6ad} + \frac{d(c+dx)}{2f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)^2}{2f(a+ia \tan(e+fx))} - \frac{d^2 \int \frac{1}{a+ia \tan(e+fx)} dx}{2f(a+ia \tan(e+fx))} \\ &= -\frac{i(c+dx)^2}{4af} + \frac{(c+dx)^3}{6ad} - \frac{id^2}{4f^3(a+ia \tan(e+fx))} + \frac{d(c+dx)}{2f^2(a+ia \tan(e+fx))} + \frac{d^2 \int \frac{1}{a+ia \tan(e+fx)} dx}{2f(a+ia \tan(e+fx))} \\ &= -\frac{d^2x}{4af^2} - \frac{i(c+dx)^2}{4af} + \frac{(c+dx)^3}{6ad} - \frac{id^2}{4f^3(a+ia \tan(e+fx))} + \frac{d(c+dx)}{2f^2(a+ia \tan(e+fx))} \end{aligned}$$

Mathematica [A] time = 0.40, size = 178, normalized size = 1.30

$$\frac{\sec(e + fx)(\cos(fx) + i \sin(fx)) \left(\frac{4}{3} f^3 x (3c^2 + 3cdx + d^2 x^2) (\cos(e) + i \sin(e)) + (\cos(e) - i \sin(e)) \cos(2fx) \right)}{(1 + I)^2 c^2 f^2 + 6 c d f - 3 i d^2 + (12 i c d f^2 + 6 d^2 f) x + 4 (d^2 f^3 x^3 + 3 c d f^3 x^2 + 3 c^2 f^3 x) e^{(2i f x + 2i e)}}{24 a f^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + I*a*Tan[e + f*x]),x]

[Out] (Sec[e + f*x]*(Cos[f*x] + I*Sin[f*x])*((d + (1 + I)*c*f + (1 + I)*d*f*x)*((1 + I)*c*f + d*(-I + (1 + I)*f*x))*Cos[2*f*x]*(Cos[e] - I*Sin[e]) + (4*f^3*x*(3*c^2 + 3*c*d*x + d^2*x^2)*(Cos[e] + I*Sin[e]))/3 - I*(d + (1 + I)*c*f + (1 + I)*d*f*x)*((1 + I)*c*f + d*(-I + (1 + I)*f*x))*(Cos[e] - I*Sin[e])*Sin[2*f*x]))/(8*f^3*(a + I*a*Tan[e + f*x]))

fricas [A] time = 0.56, size = 104, normalized size = 0.76

$$\frac{(6i d^2 f^2 x^2 + 6i c^2 f^2 + 6 c d f - 3i d^2 + (12i c d f^2 + 6 d^2 f) x + 4 (d^2 f^3 x^3 + 3 c d f^3 x^2 + 3 c^2 f^3 x) e^{(2i f x + 2i e)}) e^{(-2i f x)}}{24 a f^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/24*(6*I*d^2*f^2*x^2 + 6*I*c^2*f^2 + 6*c*d*f - 3*I*d^2 + (12*I*c*d*f^2 + 6*d^2*f)*x + 4*(d^2*f^3*x^3 + 3*c*d*f^3*x^2 + 3*c^2*f^3*x)*e^(2*I*f*x + 2*I*e))*e^(-2*I*f*x - 2*I*e)/(a*f^3)

giac [A] time = 0.79, size = 123, normalized size = 0.90

$$\frac{(4 d^2 f^3 x^3 e^{(2i f x + 2i e)} + 12 c d f^3 x^2 e^{(2i f x + 2i e)} + 12 c^2 f^3 x e^{(2i f x + 2i e)} + 6i d^2 f^2 x^2 + 12i c d f^2 x + 6i c^2 f^2 + 6 d^2 f x + 6i d^2) e^{(-2i f x)}}{24 a f^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] 1/24*(4*d^2*f^3*x^3*e^(2*I*f*x + 2*I*e) + 12*c*d*f^3*x^2*e^(2*I*f*x + 2*I*e) + 12*c^2*f^3*x*e^(2*I*f*x + 2*I*e) + 6*I*d^2*f^2*x^2 + 12*I*c*d*f^2*x + 6*I*c^2*f^2 + 6*d^2*f*x + 6*c*d*f - 3*I*d^2)*e^(-2*I*f*x - 2*I*e)/(a*f^3)

maple [B] time = 0.62, size = 509, normalized size = 3.72

$$\frac{id^2 \left(-\frac{(fx+e)^2 (\cos^2(fx+e))}{2} + (fx+e) \left(\frac{\sin(fx+e) \cos(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2} \right) - \frac{(fx+e)^2 (\sin^2(fx+e))}{4} \right)}{f^2} - \frac{2icd \left(-\frac{(fx+e) (\cos^2(fx+e))}{2} + \frac{\sin(fx+e) \cos(fx+e)}{4} + \frac{fx}{4} + \frac{e}{4} \right)}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(a+I*a*tan(f*x+e)),x)

[Out] 1/a/f*(-I/f^2*d^2*(-1/2*(f*x+e)^2*cos(f*x+e)^2+(f*x+e)*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*sin(f*x+e)^2)-2*I/f*c*d*(-1/2*(f*x+e)*cos(f*x+e)^2+1/4*sin(f*x+e)*cos(f*x+e)+1/4*f*x+1/4*e)+2*I/f^2*d^2*e*(-1/2*(f*x+e)*cos(f*x+e)^2+1/4*sin(f*x+e)*cos(f*x+e)+1/4*f*x+1/4*e)+1/2*I*c^2*cos(f*x+e)^2-I/f*c*d*e*cos(f*x+e)^2+1/2*I/f^2*d^2*e^2*cos(f*x+e)^2+1/f^2*d^2*((f*x+e)^2*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*f*x+1/2*e)+1/2*(f*x+e)*cos(f*x+e)^2-1/4*sin(f*x+e)*cos(f*x+e)-1/4*f*x-1/4*e-1/3*(f*x+e)^3)+2/f*c*d*((f*x+e)*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*sin(f*x+e)^2)-

$$2/f^2*d^2*e*((f*x+e)*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*\sin(f*x+e)^2)+c^2*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)-2/f*c*d*e*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+1/f^2*d^2*e^2*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e))$$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e)),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima: expt: undefined: 0 to a negative exponent.

mpad [B] time = 3.08, size = 241, normalized size = 1.76

$$\frac{12c^2f^3x - 3d^2\sin(2e + 2fx) + 6c^2f^2\sin(2e + 2fx) + 4d^2f^3x^3 + 6cdf\cos(2e + 2fx) + 6d^2f^2x^2\sin(2e + 2fx)}{24af^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + a*tan(e + f*x)*1i),x)

[Out] $(12*c^2*f^3*x - 3*d^2*\sin(2*e + 2*f*x) - d^2*\cos(2*e + 2*f*x)*3i + c^2*f^2*\cos(2*e + 2*f*x)*6i + 6*c^2*f^2*\sin(2*e + 2*f*x) + 4*d^2*f^3*x^3 + 6*c*d*f*\cos(2*e + 2*f*x) - c*d*f*\sin(2*e + 2*f*x)*6i + d^2*f^2*x^2*\cos(2*e + 2*f*x)*6i + 6*d^2*f^2*x^2*\sin(2*e + 2*f*x) + 12*c*d*f^3*x^2 + 6*d^2*f*x*\cos(2*e + 2*f*x) - d^2*f*x*\sin(2*e + 2*f*x)*6i + c*d*f^2*x*\cos(2*e + 2*f*x)*12i + 12*c*d*f^2*x*\sin(2*e + 2*f*x))/(24*a*f^3)$

sympy [A] time = 0.31, size = 168, normalized size = 1.23

$$\begin{cases} \frac{(-2ic^2f^2 - 4icdf^2x - 2cdf - 2id^2f^2x^2 - 2d^2fx + id^2)e^{-2ie}e^{-2ifx}}{8af^3} & \text{for } 8af^3e^{2ie} \neq 0 \\ \frac{c^2xe^{-2ie}}{2a} + \frac{cdx^2e^{-2ie}}{2a} + \frac{d^2x^3e^{-2ie}}{6a} & \text{otherwise} \end{cases} + \frac{c^2x}{2a} + \frac{cdx^2}{2a} + \frac{d^2x^3}{6a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(a+I*a*tan(f*x+e)),x)

[Out] Piecewise((-(-2*I*c**2*f**2 - 4*I*c*d*f**2*x - 2*c*d*f - 2*I*d**2*f**2*x**2 - 2*d**2*f*x + I*d**2)*exp(-2*I*e)*exp(-2*I*f*x)/(8*a*f**3), Ne(8*a*f**3*exp(2*I*e), 0)), (c**2*x*exp(-2*I*e)/(2*a) + c*d*x**2*exp(-2*I*e)/(2*a) + d**2*x**3*exp(-2*I*e)/(6*a), True)) + c**2*x/(2*a) + c*d*x**2/(2*a) + d**2*x**3/(6*a)

$$3.20 \quad \int \frac{c+dx}{a+ia \tan(e+fx)} dx$$

Optimal. Leaf size=84

$$\frac{i(c+dx)}{2f(a+ia \tan(e+fx))} + \frac{(c+dx)^2}{4ad} + \frac{d}{4f^2(a+ia \tan(e+fx))} - \frac{id}{4af}$$

[Out] $-1/4*I*d*x/a/f+1/4*(d*x+c)^2/a/d+1/4*d/f^2/(a+I*a*\tan(f*x+e))+1/2*I*(d*x+c)/f/(a+I*a*\tan(f*x+e))$

Rubi [A] time = 0.05, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {3723, 3479, 8}

$$\frac{i(c+dx)}{2f(a+ia \tan(e+fx))} + \frac{(c+dx)^2}{4ad} + \frac{d}{4f^2(a+ia \tan(e+fx))} - \frac{id}{4af}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + I*a*Tan[e + f*x]), x]

[Out] $((-I/4)*d*x)/(a*f) + (c + d*x)^2/(4*a*d) + d/(4*f^2*(a + I*a*Tan[e + f*x])) + ((I/2)*(c + d*x))/(f*(a + I*a*Tan[e + f*x]))$

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rule 3479

Int[((a_) + (b_)*tan[(c_) + (d_)*(x_)])^(n_), x_Symbol] :> Simp[(a*(a + b*Tan[c + d*x])^n)/(2*b*d*n), x] + Dist[1/(2*a), Int[(a + b*Tan[c + d*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[a^2 + b^2, 0] && LtQ[n, 0]

Rule 3723

Int[((c_) + (d_)*(x_)^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] :> Simp[(c + d*x)^(m + 1)/(2*a*d*(m + 1)), x] + (Dist[(a*d*m)/(2*b*f), Int[(c + d*x)^(m - 1)/(a + b*Tan[e + f*x]), x], x] - Simp[(a*(c + d*x)^m)/(2*b*f*(a + b*Tan[e + f*x])), x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && GtQ[m, 0]

Rubi steps

$$\begin{aligned} \int \frac{c+dx}{a+ia \tan(e+fx)} dx &= \frac{(c+dx)^2}{4ad} + \frac{i(c+dx)}{2f(a+ia \tan(e+fx))} - \frac{(id) \int \frac{1}{a+ia \tan(e+fx)} dx}{2f} \\ &= \frac{(c+dx)^2}{4ad} + \frac{d}{4f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)}{2f(a+ia \tan(e+fx))} - \frac{(id) \int 1 dx}{4af} \\ &= -\frac{id}{4af} + \frac{(c+dx)^2}{4ad} + \frac{d}{4f^2(a+ia \tan(e+fx))} + \frac{i(c+dx)}{2f(a+ia \tan(e+fx))} \end{aligned}$$

Mathematica [A] time = 0.44, size = 96, normalized size = 1.14

$$\frac{(2cf(2fx - i) + d(2f^2x^2 - 2ifx - 1)) \tan(e + fx) - i(2cf(2fx + i) + d(2f^2x^2 + 2ifx + 1))}{8af^2(\tan(e + fx) - i)}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + I*a*Tan[e + f*x]),x]

[Out] ((-I)*(2*c*f*(I + 2*f*x) + d*(1 + (2*I)*f*x + 2*f^2*x^2)) + (2*c*f*(-I + 2*f*x) + d*(-1 - (2*I)*f*x + 2*f^2*x^2))*Tan[e + f*x])/(8*a*f^2*(-I + Tan[e + f*x]))

fricas [A] time = 0.52, size = 55, normalized size = 0.65

$$\frac{(2idfx + 2icf + 2(df^2x^2 + 2cf^2x)e^{2ifx+2ie} + d)e^{-2ifx-2ie}}{8af^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/8*(2*I*d*f*x + 2*I*c*f + 2*(d*f^2*x^2 + 2*c*f^2*x)*e^(2*I*f*x + 2*I*e) + d)*e^(-2*I*f*x - 2*I*e)/(a*f^2)

giac [A] time = 0.70, size = 65, normalized size = 0.77

$$\frac{(2df^2x^2e^{2ifx+2ie} + 4cf^2xe^{2ifx+2ie} + 2idfx + 2icf + d)e^{-2ifx-2ie}}{8af^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] 1/8*(2*d*f^2*x^2*e^(2*I*f*x + 2*I*e) + 4*c*f^2*x*e^(2*I*f*x + 2*I*e) + 2*I*d*f*x + 2*I*c*f + d)*e^(-2*I*f*x - 2*I*e)/(a*f^2)

maple [B] time = 0.56, size = 187, normalized size = 2.23

$$\frac{id\left(-\frac{(fx+e)\cos^2(fx+e)}{2} + \frac{\sin(fx+e)\cos(fx+e)}{4} + \frac{fx}{4} + \frac{e}{4}\right) + \frac{ic(\cos^2(fx+e))}{2} - \frac{ide(\cos^2(fx+e))}{2f} + \frac{d\left((fx+e)\left(\frac{\sin(fx+e)\cos(fx+e)}{2} + \frac{fx}{2} + \frac{e}{2}\right) - \frac{(fx+e)^2}{4} - \frac{\sin^2(fx+e)}{4}\right)}{af}}{af}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)/(a+I*a*tan(f*x+e)),x)

[Out] 1/a/f*(-I/f*d*(-1/2*(f*x+e)*cos(f*x+e)^2+1/4*sin(f*x+e)*cos(f*x+e)+1/4*f*x+1/4*e)+1/2*I*c*cos(f*x+e)^2-1/2*I/f*d*e*cos(f*x+e)^2+1/f*d*((f*x+e)*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*sin(f*x+e)^2)+c*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*f*x+1/2*e)-1/f*d*e*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*f*x+1/2*e))

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e)),x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima: expt: undefined: 0 to a negative exponent.

mupad [B] time = 2.81, size = 105, normalized size = 1.25

$$\frac{d \cos(2e + 2fx) + 2df^2x^2 + 2cf \sin(2e + 2fx) + 4cf^2x + 2dfx \sin(2e + 2fx) - d \sin(2e + 2fx)}{8af^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)/(a + a*tan(e + f*x)*1i), x)

[Out] (d*cos(2*e + 2*f*x) - d*sin(2*e + 2*f*x)*1i + 2*d*f^2*x^2 + c*f*cos(2*e + 2*f*x)*2i + 2*c*f*sin(2*e + 2*f*x) + 4*c*f^2*x + d*f*x*cos(2*e + 2*f*x)*2i + 2*d*f*x*sin(2*e + 2*f*x))/(8*a*f^2)

sympy [A] time = 0.24, size = 97, normalized size = 1.15

$$\begin{cases} -\frac{(-2icf-2idfx-d)e^{-2ie}e^{-2ifx}}{8af^2} & \text{for } 8af^2e^{2ie} \neq 0 \\ \frac{cx e^{-2ie}}{2a} + \frac{dx^2 e^{-2ie}}{4a} & \text{otherwise} \end{cases} + \frac{cx}{2a} + \frac{dx^2}{4a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e)), x)

[Out] Piecewise((-(-2*I*c*f - 2*I*d*f*x - d)*exp(-2*I*e)*exp(-2*I*f*x)/(8*a*f**2), Ne(8*a*f**2*exp(2*I*e), 0)), (c*x*exp(-2*I*e)/(2*a) + d*x**2*exp(-2*I*e)/(4*a), True)) + c*x/(2*a) + d*x**2/(4*a)

$$3.21 \quad \int \frac{1}{(c+dx)(a+ia \tan(e+fx))} dx$$

Optimal. Leaf size=161

$$\frac{i \operatorname{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{2ad} + \frac{\operatorname{Ci}\left(2xf + \frac{2cf}{d}\right) \cos\left(2e - \frac{2cf}{d}\right)}{2ad} - \frac{\sin\left(2e - \frac{2cf}{d}\right) \operatorname{Si}\left(2xf + \frac{2cf}{d}\right)}{2ad} - \frac{i \cos\left(2e - \frac{2cf}{d}\right) \operatorname{Si}\left(2xf + \frac{2cf}{d}\right)}{2ad}$$

[Out] $1/2 * \operatorname{Ci}(2 * c * f / d + 2 * f * x) * \cos(-2 * e + 2 * c * f / d) / a / d + 1/2 * \ln(d * x + c) / a / d - 1/2 * I * \cos(-2 * e + 2 * c * f / d) * \operatorname{Si}(2 * c * f / d + 2 * f * x) / a / d + 1/2 * I * \operatorname{Ci}(2 * c * f / d + 2 * f * x) * \sin(-2 * e + 2 * c * f / d) / a / d + 1/2 * \operatorname{Si}(2 * c * f / d + 2 * f * x) * \sin(-2 * e + 2 * c * f / d) / a / d$

Rubi [A] time = 0.28, antiderivative size = 161, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.174$, Rules used = {3726, 3303, 3299, 3302}

$$\frac{i \operatorname{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{2ad} + \frac{\operatorname{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right)}{2ad} - \frac{\sin\left(2e - \frac{2cf}{d}\right) \operatorname{Si}\left(2xf + \frac{2cf}{d}\right)}{2ad}$$

Antiderivative was successfully verified.

[In] `Int[1/((c + d*x)*(a + I*a*Tan[e + f*x])),x]`

[Out] $(\operatorname{Cos}[2 * e - (2 * c * f) / d] * \operatorname{CosIntegral}[(2 * c * f) / d + 2 * f * x]) / (2 * a * d) + \operatorname{Log}[c + d * x] / (2 * a * d) - ((I / 2) * \operatorname{CosIntegral}[(2 * c * f) / d + 2 * f * x] * \operatorname{Sin}[2 * e - (2 * c * f) / d]) / (a * d) - ((I / 2) * \operatorname{Cos}[2 * e - (2 * c * f) / d] * \operatorname{SinIntegral}[(2 * c * f) / d + 2 * f * x]) / (a * d) - (\operatorname{Sin}[2 * e - (2 * c * f) / d] * \operatorname{SinIntegral}[(2 * c * f) / d + 2 * f * x]) / (2 * a * d)$

Rule 3299

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]`

Rule 3302

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]`

Rule 3303

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]`

Rule 3726

`Int[1/(((c_.) + (d_.)*(x_))*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])), x_Symbol] := Simp[Log[c + d*x]/(2*a*d), x] + (Dist[1/(2*a), Int[Cos[2*e + 2*f*x]/(c + d*x), x], x] + Dist[1/(2*b), Int[Sin[2*e + 2*f*x]/(c + d*x), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0]`

Rubi steps

$$\begin{aligned} \int \frac{1}{(c+dx)(a+ia \tan(e+fx))} dx &= \frac{\log(c+dx)}{2ad} - \frac{i \int \frac{\sin(2e+2fx)}{c+dx} dx}{2a} + \frac{\int \frac{\cos(2e+2fx)}{c+dx} dx}{2a} \\ &= \frac{\log(c+dx)}{2ad} - \frac{\left(i \cos\left(2e - \frac{2cf}{d}\right)\right) \int \frac{\sin\left(\frac{2cf}{d} + 2fx\right)}{c+dx} dx}{2a} + \frac{\cos\left(2e - \frac{2cf}{d}\right) \int \frac{\cos\left(\frac{2cf}{d} + 2fx\right)}{c+dx} dx}{2a} \\ &= \frac{\cos\left(2e - \frac{2cf}{d}\right) \operatorname{Ci}\left(\frac{2cf}{d} + 2fx\right)}{2ad} + \frac{\log(c+dx)}{2ad} - \frac{i \operatorname{Ci}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{2ad} \end{aligned}$$

Mathematica [A] time = 0.35, size = 166, normalized size = 1.03

$$\frac{\sec(e+fx) \left(\sin\left(f\left(\frac{c}{d}+x\right)\right) - i \cos\left(f\left(\frac{c}{d}+x\right)\right) \right) \left(\operatorname{Ci}\left(\frac{2f(c+dx)}{d}\right) \left(\cos\left(e - \frac{cf}{d}\right) - i \sin\left(e - \frac{cf}{d}\right) \right) + \operatorname{Si}\left(\frac{2f(c+dx)}{d}\right) \right)}{2ad(\tan(e+fx) - i)}$$

Warning: Unable to verify antiderivative.

[In] Integrate[1/((c+d*x)*(a+I*a*Tan[e+f*x])),x]

[Out] (Sec[e+f*x]*((-I)*Cos[f*(c/d+x)]+Sin[f*(c/d+x)])*(CosIntegral[(2*f*(c+d*x))/d]*(Cos[e-(c*f)/d]-I*Sin[e-(c*f)/d])+Log[f*(c+d*x)]*(Cos[e-(c*f)/d]+I*Sin[e-(c*f)/d])+((-I)*Cos[e-(c*f)/d]-Sin[e-(c*f)/d])*SinIntegral[(2*f*(c+d*x))/d])/(2*a*d*(-I+Tan[e+f*x]))

fricas [A] time = 0.58, size = 49, normalized size = 0.30

$$\frac{\operatorname{Ei}\left(\frac{-2i d f x - 2i c f}{d}\right) e^{\left(\frac{-2i d e + 2i c f}{d}\right)} + \log\left(\frac{d x + c}{d}\right)}{2 a d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/2*(Ei((-2*I*d*f*x - 2*I*c*f)/d)*e^((-2*I*d*e + 2*I*c*f)/d) + log((d*x + c)/d))/(a*d)

giac [A] time = 0.78, size = 142, normalized size = 0.88

$$\frac{\cos\left(\frac{2cf}{d}\right) \operatorname{Ci}\left(-\frac{2(df x + cf)}{d}\right) + \cos(2e) \log(dx+c) + i \operatorname{Ci}\left(-\frac{2(df x + cf)}{d}\right) \sin\left(\frac{2cf}{d}\right) + i \log(dx+c) \sin(2e) - i \cos(2e) \operatorname{Si}\left(\frac{2f(c+dx)}{d}\right)}{2(ad \cos(2e) + i ad \sin(2e))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] 1/2*(cos(2*c*f/d)*cos_integral(-2*(d*f*x + c*f)/d) + cos(2*e)*log(d*x + c) + I*cos_integral(-2*(d*f*x + c*f)/d)*sin(2*c*f/d) + I*log(d*x + c)*sin(2*e) - I*cos(2*c*f/d)*sin_integral(2*(d*f*x + c*f)/d) + sin(2*c*f/d)*sin_integral(2*(d*f*x + c*f)/d))/(a*d*cos(2*e) + I*a*d*sin(2*e))

maple [A] time = 0.51, size = 204, normalized size = 1.27

$$\frac{i \operatorname{Si}\left(2fx + 2e + \frac{2cf - 2de}{d}\right) \cos\left(\frac{2cf - 2de}{d}\right)}{2ad} + \frac{i \operatorname{Ci}\left(2fx + 2e + \frac{2cf - 2de}{d}\right) \sin\left(\frac{2cf - 2de}{d}\right)}{2ad} + \frac{\operatorname{Si}\left(2fx + 2e + \frac{2cf - 2de}{d}\right) \sin\left(\frac{2cf - 2de}{d}\right)}{2ad}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)/(a+I*a*tan(f*x+e)),x)

[Out] $-1/2*I/a*Si(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d+1/2*I/a*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d+1/2/a*Si(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d+1/2/a*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d+1/2/a*ln((f*x+e)*d+c*f-d*e)/d$

maxima [A] time = 0.79, size = 110, normalized size = 0.68

$$\frac{f \cos\left(-\frac{2(de-cf)}{d}\right) E_1\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) + if E_1\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) \sin\left(-\frac{2(de-cf)}{d}\right) - f \log((fx+e)d - de + c)}{2adf}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e)),x, algorithm="maxima")

[Out] $-1/2*(f*cos(-2*(d*e - c*f)/d)*exp_integral_e(1, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d) + I*f*exp_integral_e(1, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d)*sin(-2*(d*e - c*f)/d) - f*log((f*x + e)*d - d*e + c*f))/(a*d*f)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + a \tan(e + f x) 1i) (c + d x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + a*tan(e + f*x)*1i)*(c + d*x)),x)

[Out] int(1/((a + a*tan(e + f*x)*1i)*(c + d*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{i \int \frac{1}{c \tan(e+fx)-ic+dx \tan(e+fx)-idx} dx}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e)),x)

[Out] $-I*Integral(1/(c*tan(e + f*x) - I*c + d*x*tan(e + f*x) - I*d*x), x)/a$

$$3.22 \quad \int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))} dx$$

Optimal. Leaf size=168

$$\frac{f \operatorname{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{ad^2} - \frac{if \operatorname{Ci}\left(2xf + \frac{2cf}{d}\right) \cos\left(2e - \frac{2cf}{d}\right)}{ad^2} + \frac{if \sin\left(2e - \frac{2cf}{d}\right) \operatorname{Si}\left(2xf + \frac{2cf}{d}\right)}{ad^2} - \frac{f \cos\left(2e - \frac{2cf}{d}\right)}{ad^2}$$

[Out] $-I*f*Ci(2*c*f/d+2*f*x)*cos(-2*e+2*c*f/d)/a/d^2-f*cos(-2*e+2*c*f/d)*Si(2*c*f/d+2*f*x)/a/d^2+f*Ci(2*c*f/d+2*f*x)*sin(-2*e+2*c*f/d)/a/d^2-I*f*Si(2*c*f/d+2*f*x)*sin(-2*e+2*c*f/d)/a/d^2-1/d/(d*x+c)/(a+I*a*tan(f*x+e))$

Rubi [A] time = 0.24, antiderivative size = 168, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.174$, Rules used = {3724, 3303, 3299, 3302}

$$\frac{f \operatorname{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{ad^2} - \frac{if \operatorname{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right)}{ad^2} + \frac{if \sin\left(2e - \frac{2cf}{d}\right) \operatorname{Si}\left(2xf + \frac{2cf}{d}\right)}{ad^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[1/((c + d*x)^2*(a + I*a*Tan[e + f*x])),x]$

[Out] $((-I)*f*\operatorname{Cos}[2*e - (2*c*f)/d]*\operatorname{CosIntegral}[(2*c*f)/d + 2*f*x])/(a*d^2) - (f*\operatorname{CosIntegral}[(2*c*f)/d + 2*f*x]*\operatorname{Sin}[2*e - (2*c*f)/d])/(a*d^2) - (f*\operatorname{Cos}[2*e - (2*c*f)/d]*\operatorname{SinIntegral}[(2*c*f)/d + 2*f*x])/(a*d^2) + (I*f*\operatorname{Sin}[2*e - (2*c*f)/d]*\operatorname{SinIntegral}[(2*c*f)/d + 2*f*x])/(a*d^2) - 1/(d*(c + d*x)*(a + I*a*Tan[e + f*x]))$

Rule 3299

$\operatorname{Int}[\sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{SinIntegral}[e + f*x]/d, x] /; \operatorname{FreeQ}\{c, d, e, f\}, x \ \&\& \operatorname{EqQ}[d*e - c*f, 0]$

Rule 3302

$\operatorname{Int}[\sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{CosIntegral}[e - \operatorname{Pi}/2 + f*x]/d, x] /; \operatorname{FreeQ}\{c, d, e, f\}, x \ \&\& \operatorname{EqQ}[d*(e - \operatorname{Pi}/2) - c*f, 0]$

Rule 3303

$\operatorname{Int}[\sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \rightarrow \operatorname{Dist}[\operatorname{Cos}[(d*e - c*f)/d], \operatorname{Int}[\operatorname{Sin}[(c*f)/d + f*x]/(c + d*x), x], x] + \operatorname{Dist}[\operatorname{Sin}[(d*e - c*f)/d], \operatorname{Int}[\operatorname{Cos}[(c*f)/d + f*x]/(c + d*x), x], x] /; \operatorname{FreeQ}\{c, d, e, f\}, x \ \&\& \operatorname{NeQ}[d*e - c*f, 0]$

Rule 3724

$\operatorname{Int}[1/(((c_.) + (d_.)*(x_.))^2*((a_.) + (b_.)*\tan[(e_.) + (f_.)*(x_.)])), x_Symbol] \rightarrow -\operatorname{Simp}[(d*(c + d*x)*(a + b*\tan[e + f*x]))^{-1}, x] + (-\operatorname{Dist}[f/(a*d), \operatorname{Int}[\operatorname{Sin}[2*e + 2*f*x]/(c + d*x), x], x] + \operatorname{Dist}[f/(b*d), \operatorname{Int}[\operatorname{Cos}[2*e + 2*f*x]/(c + d*x), x], x]) /; \operatorname{FreeQ}\{a, b, c, d, e, f\}, x \ \&\& \operatorname{EqQ}[a^2 + b^2, 0]$

Rubi steps

$$\begin{aligned} \int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))} dx &= -\frac{1}{d(c+dx)(a+ia \tan(e+fx))} - \frac{(if) \int \frac{\cos(2e+2fx)}{c+dx} dx}{ad} - \frac{f \int \frac{\sin(2e+2fx)}{c+dx} dx}{ad} \\ &= -\frac{1}{d(c+dx)(a+ia \tan(e+fx))} - \frac{\left(if \cos\left(2e - \frac{2cf}{d}\right) \right) \int \frac{\cos\left(\frac{2cf}{d} + 2fx\right)}{c+dx} dx}{ad} - \frac{\left(f \cos\left(2e - \frac{2cf}{d}\right) \right) \int \frac{\sin\left(\frac{2cf}{d} + 2fx\right)}{c+dx} dx}{ad} \\ &= -\frac{if \cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{ad^2} - \frac{f \text{Ci}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{ad^2} - \frac{f \cos\left(2e - \frac{2cf}{d}\right) \text{Si}\left(\frac{2cf}{d} + 2fx\right)}{ad^2} \end{aligned}$$

Mathematica [A] time = 0.85, size = 224, normalized size = 1.33

$$\frac{\sec(e+fx) \left(\cos\left(\frac{cf}{d}\right) + i \sin\left(\frac{cf}{d}\right) \right) \left(-2f(c+dx) \text{Ci}\left(\frac{2f(c+dx)}{d}\right) \left(\cos\left(e - \frac{f(c+dx)}{d}\right) - i \sin\left(e - \frac{f(c+dx)}{d}\right) \right) + 2f(c+dx) \right)}{ad^2}$$

Antiderivative was successfully verified.

[In] Integrate[1/((c + d*x)^2*(a + I*a*Tan[e + f*x])),x]

[Out] (Sec[e + f*x]*(Cos[(c*f)/d] + I*Sin[(c*f)/d])*(d*(I*Cos[e + f*(-(c/d) + x)] + I*Cos[e + f*(c/d + x)] - Sin[e + f*(-(c/d) + x)] + Sin[e + f*(c/d + x)]) - 2*f*(c + d*x)*CosIntegral[(2*f*(c + d*x))/d]*(Cos[e - (f*(c + d*x))/d] - I*Sin[e - (f*(c + d*x))/d]) + 2*f*(c + d*x)*(I*Cos[e - (f*(c + d*x))/d] + Sin[e - (f*(c + d*x))/d])*SinIntegral[(2*f*(c + d*x))/d])/(2*a*d^2*(c + d*x)*(-I + Tan[e + f*x]))

fricas [A] time = 0.58, size = 84, normalized size = 0.50

$$\frac{\left(\left((-2i d f x - 2i c f) \text{Ei}\left(\frac{-2i d f x - 2i c f}{d}\right) e^{\left(\frac{-2i d e + 2i c f}{d}\right)} - d \right) e^{(2i f x + 2i e)} - d \right) e^{(-2i f x - 2i e)}}{2(ad^3x + acd^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/2*(((-2*I*d*f*x - 2*I*c*f)*Ei((-2*I*d*f*x - 2*I*c*f)/d)*e^((-2*I*d*e + 2*I*c*f)/d) - d)*e^(2*I*f*x + 2*I*e) - d)*e^(-2*I*f*x - 2*I*e)/(a*d^3*x + a*c*d^2)

giac [B] time = 74.99, size = 1099, normalized size = 6.54

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] -1/2*(2*I*(d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c))*f^2*cos(2*(c*f - d*e)/d)*cos_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) - 2*I*c*f^3*cos(2*(c*f - d*e)/d)*cos_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) + 2*I*d*f^2*cos(2*(c*f - d*e)/d)*cos_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d)*e - 2*(d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c))*f^2*cos_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d)*sin(2*(c*f - d*e)/d) + 2*c*f^3*cos_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d)*sin(2*(c*f - d*e)/d) - 2*d*f^2*cos_integral(-2

*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d)*e*sin(2*(c*f - d*e)/d) + 2*(d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c))*f^2*cos(2*(c*f - d*e)/d)*sin_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) - 2*c*f^3*cos(2*(c*f - d*e)/d)*sin_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) + 2*d*f^2*cos(2*(c*f - d*e)/d)*e*sin_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) + 2*I*(d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c))*f^2*sin(2*(c*f - d*e)/d)*sin_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) - 2*I*c*f^3*sin(2*(c*f - d*e)/d)*sin_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) + 2*I*d*f^2*e*sin(2*(c*f - d*e)/d)*sin_integral(-2*((d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)) - c*f + d*e)/d) - d*f^2*cos(2*(d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)))/d) - I*d*f^2*sin(2*(d*x + c)*(c*f/(d*x + c) - f - d*e/(d*x + c)))/d) - d*f^2*d^2/(((d*x + c)*a*d^4*(c*f/(d*x + c) - f - d*e/(d*x + c)) - a*c*d^4*f + a*d^5*e)*f)

maple [A] time = 0.47, size = 285, normalized size = 1.70

$$\frac{if^2 \left(\frac{2 \sin(2fx+2e)}{((fx+e)d+cf-de)d} + \frac{4 \operatorname{Si}\left(2fx+2e+\frac{2cf-2de}{d}\right) \sin\left(\frac{2cf-2de}{d}\right)}{d} + \frac{4 \operatorname{Ci}\left(2fx+2e+\frac{2cf-2de}{d}\right) \cos\left(\frac{2cf-2de}{d}\right)}{d} \right)}{4} + \frac{f^2 \left(\frac{2 \cos(2fx+2e)}{((fx+e)d+cf-de)d} - \frac{2 \operatorname{Si}\left(2fx+2e+\frac{2cf-2de}{d}\right) \cos\left(\frac{2cf-2de}{d}\right)}{d} \right)}{af}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^2/(a+I*a*tan(f*x+e)), x)

[Out] 1/a/f*(-1/4*I*f^2*(-2*sin(2*f*x+2*e)/((f*x+e)*d+c*f-d*e)/d+2*(2*Si(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d+2*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d)/d+1/4*f^2*(-2*cos(2*f*x+2*e)/((f*x+e)*d+c*f-d*e)/d-2*(2*Si(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d-2*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d)/d-1/2*f^2/((f*x+e)*d+c*f-d*e)/d)

maxima [A] time = 0.86, size = 117, normalized size = 0.70

$$\frac{f^2 \cos\left(-\frac{2(de-cf)}{d}\right) E_2\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) + if^2 E_2\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) \sin\left(-\frac{2(de-cf)}{d}\right) + f^2}{2((fx+e)ad^2 - ad^2e + acdf)f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e)), x, algorithm="maxima")

[Out] -1/2*(f^2*cos(-2*(d*e - c*f)/d)*exp_integral_e(2, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d) + I*f^2*exp_integral_e(2, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d)*sin(-2*(d*e - c*f)/d) + f^2)/(((f*x + e)*a*d^2 - a*d^2*e + a*c*d*f)*f)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{1}{(a + a \tan(e + fx) 1i) (c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + a*tan(e + f*x)*1i)*(c + d*x)^2), x)

[Out] int(1/((a + a*tan(e + f*x)*1i)*(c + d*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{i \int \frac{1}{c^2 \tan(e+fx) - ic^2 + 2cdx \tan(e+fx) - 2icdx + d^2x^2 \tan(e+fx) - id^2x^2} dx}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**2/(a+I*a*tan(f*x+e)),x)

[Out] -I*Integral(1/(c**2*tan(e + f*x) - I*c**2 + 2*c*d*x*tan(e + f*x) - 2*I*c*d*x + d**2*x**2*tan(e + f*x) - I*d**2*x**2), x)/a

$$3.23 \quad \int \frac{1}{(c+dx)^3(a+ia \tan(e+fx))} dx$$

Optimal. Leaf size=227

$$\frac{if^2 \text{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{ad^3} - \frac{f^2 \text{Ci}\left(2xf + \frac{2cf}{d}\right) \cos\left(2e - \frac{2cf}{d}\right)}{ad^3} + \frac{f^2 \sin\left(2e - \frac{2cf}{d}\right) \text{Si}\left(2xf + \frac{2cf}{d}\right)}{ad^3} + \frac{if^2 \cos\left(2e - \frac{2cf}{d}\right)}{ad^3}$$

[Out] $-1/2*I*f/a/d^2/(d*x+c)-f^2*Ci(2*c*f/d+2*f*x)*\cos(-2*e+2*c*f/d)/a/d^3+I*f^2*\cos(-2*e+2*c*f/d)*Si(2*c*f/d+2*f*x)/a/d^3-I*f^2*Ci(2*c*f/d+2*f*x)*\sin(-2*e+2*c*f/d)/a/d^3-f^2*Si(2*c*f/d+2*f*x)*\sin(-2*e+2*c*f/d)/a/d^3-1/2/d/(d*x+c)^2/(a+I*a*\tan(f*x+e))+I*f/d^2/(d*x+c)/(a+I*a*\tan(f*x+e))$

Rubi [A] time = 0.32, antiderivative size = 227, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {3725, 3724, 3303, 3299, 3302}

$$\frac{if^2 \text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{ad^3} - \frac{f^2 \text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right)}{ad^3} + \frac{f^2 \sin\left(2e - \frac{2cf}{d}\right) \text{Si}\left(\frac{2cf}{d} + 2fx\right)}{ad^3}$$

Antiderivative was successfully verified.

[In] Int[1/((c + d*x)^3*(a + I*a*Tan[e + f*x])),x]

[Out] $((-I/2)*f)/(a*d^2*(c + d*x)) - (f^2*\text{Cos}[2*e - (2*c*f)/d]*\text{CosIntegral}[(2*c*f)/d + 2*f*x])/(a*d^3) + (I*f^2*\text{CosIntegral}[(2*c*f)/d + 2*f*x]*\text{Sin}[2*e - (2*c*f)/d])/(a*d^3) + (I*f^2*\text{Cos}[2*e - (2*c*f)/d]*\text{SinIntegral}[(2*c*f)/d + 2*f*x])/(a*d^3) + (f^2*\text{Sin}[2*e - (2*c*f)/d]*\text{SinIntegral}[(2*c*f)/d + 2*f*x])/(a*d^3) - 1/(2*d*(c + d*x)^2*(a + I*a*Tan[e + f*x])) + (I*f)/(d^2*(c + d*x)*(a + I*a*Tan[e + f*x]))$

Rule 3299

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3724

Int[1/(((c_.) + (d_.)*(x_.))^2*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_.)])), x_Symbol] := -Simp[(d*(c + d*x)*(a + b*Tan[e + f*x]))^(-1), x] + (-Dist[f/(a*d), Int[Sin[2*e + 2*f*x]/(c + d*x), x], x] + Dist[f/(b*d), Int[Cos[2*e + 2*f*x]/(c + d*x), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0]

Rule 3725

Int[((c_.) + (d_.)*(x_.))^(m_.)/((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_.)]), x_Symbol] := Simp[(f*(c + d*x)^(m + 2))/(b*d^2*(m + 1)*(m + 2)), x] + (Dist[(2*b

$\ast f)/(a \ast d \ast (m + 1))$, $\text{Int}[(c + d \ast x)^{(m + 1)}/(a + b \ast \text{Tan}[e + f \ast x]), x]$, $x] + \text{Simp}[(c + d \ast x)^{(m + 1)}/(d \ast (m + 1) \ast (a + b \ast \text{Tan}[e + f \ast x])), x] /;$ $\text{FreeQ}\{a, b, c, d, e, f, x\}$ && $\text{EqQ}[a^2 + b^2, 0]$ && $\text{LtQ}[m, -1]$ && $\text{NeQ}[m, -2]$

Rubi steps

$$\begin{aligned} \int \frac{1}{(c + dx)^3(a + ia \tan(e + fx))} dx &= -\frac{if}{2ad^2(c + dx)} - \frac{1}{2d(c + dx)^2(a + ia \tan(e + fx))} - \frac{(if) \int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))} dx}{d} \\ &= -\frac{if}{2ad^2(c + dx)} - \frac{1}{2d(c + dx)^2(a + ia \tan(e + fx))} + \frac{if}{d^2(c + dx)(a + ia \tan(e + fx))} \\ &= -\frac{if}{2ad^2(c + dx)} - \frac{1}{2d(c + dx)^2(a + ia \tan(e + fx))} + \frac{if}{d^2(c + dx)(a + ia \tan(e + fx))} \\ &= -\frac{if}{2ad^2(c + dx)} - \frac{f^2 \cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{ad^3} + \frac{if^2 \text{Ci}\left(\frac{2cf}{d} + 2fx\right) \sin\left(\frac{2cf}{d} + 2fx\right)}{ad^3} \end{aligned}$$

Mathematica [A] time = 1.20, size = 285, normalized size = 1.26

$$\frac{\sec(e + fx) \left(\cos\left(\frac{cf}{d}\right) + i \sin\left(\frac{cf}{d}\right) \right) \left(4f^2(c + dx)^2 \text{Ci}\left(\frac{2f(c+dx)}{d}\right) \left(\sin\left(e - \frac{f(c+dx)}{d}\right) + i \cos\left(e - \frac{f(c+dx)}{d}\right) \right) + 4f^2(c + dx) \right)}{ad^3}$$

Antiderivative was successfully verified.

[In] Integrate[1/((c + d*x)^3*(a + I*a*Tan[e + f*x])),x]

[Out] (Sec[e + f*x]*(Cos[(c*f)/d] + I*Sin[(c*f)/d])*(d*(I*d*Cos[e + f*(-(c/d) + x)] + (I*d + 2*c*f + 2*d*f*x)*Cos[e + f*(c/d + x)] - d*Sin[e + f*(-(c/d) + x)] + d*Sin[e + f*(c/d + x)] - (2*I)*c*f*Sin[e + f*(c/d + x)] - (2*I)*d*f*x*Sin[e + f*(c/d + x)]) + 4*f^2*(c + d*x)^2*CosIntegral[(2*f*(c + d*x))/d]*(I*Cos[e - (f*(c + d*x))/d] + Sin[e - (f*(c + d*x))/d]) + 4*f^2*(c + d*x)^2*(Cos[e - (f*(c + d*x))/d] - I*Sin[e - (f*(c + d*x))/d])*SinIntegral[(2*f*(c + d*x))/d]))/(4*a*d^3*(c + d*x)^2*(-I + Tan[e + f*x]))

fricas [A] time = 0.74, size = 128, normalized size = 0.56

$$\frac{\left(2i d^2 f x + 2i c d f - d^2 - \left(4 \left(d^2 f^2 x^2 + 2 c d f^2 x + c^2 f^2 \right) \text{Ei}\left(\frac{-2i d f x - 2i c f}{d}\right) e^{\left(\frac{-2i d e + 2i c f}{d}\right)} + d^2 \right) e^{(2i f x + 2i e)} \right) e^{(-2i f x - 2i e)}}{4 \left(a d^5 x^2 + 2 a c d^4 x + a c^2 d^3 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^3/(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/4*(2*I*d^2*f*x + 2*I*c*d*f - d^2 - (4*(d^2*f^2*x^2 + 2*c*d*f^2*x + c^2*f^2)*Ei((-2*I*d*f*x - 2*I*c*f)/d)*e^((-2*I*d*e + 2*I*c*f)/d) + d^2)*e^(2*I*f*x + 2*I*e))*e^(-2*I*f*x - 2*I*e)/(a*d^5*x^2 + 2*a*c*d^4*x + a*c^2*d^3)

giac [B] time = 0.88, size = 542, normalized size = 2.39

$$\frac{4 d^2 f^2 x^2 \cos\left(\frac{2cf}{d}\right) \text{Ci}\left(-\frac{2(dfx+cf)}{d}\right) + 4i d^2 f^2 x^2 \text{Ci}\left(-\frac{2(dfx+cf)}{d}\right) \sin\left(\frac{2cf}{d}\right) - 4i d^2 f^2 x^2 \cos\left(\frac{2cf}{d}\right) \text{Si}\left(\frac{2(dfx+cf)}{d}\right) + \dots}{ad^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^3/(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] $-(4*d^2*f^2*x^2*\cos(2*c*f/d)*\cos_integral(-2*(d*f*x + c*f)/d) + 4*I*d^2*f^2*x^2*\cos_integral(-2*(d*f*x + c*f)/d)*\sin(2*c*f/d) - 4*I*d^2*f^2*x^2*\cos(2*c*f/d)*\sin_integral(2*(d*f*x + c*f)/d) + 4*d^2*f^2*x^2*\sin(2*c*f/d)*\sin_integral(2*(d*f*x + c*f)/d) + 8*c*d*f^2*x*\cos(2*c*f/d)*\cos_integral(-2*(d*f*x + c*f)/d) + 8*I*c*d*f^2*x*\cos_integral(-2*(d*f*x + c*f)/d)*\sin(2*c*f/d) - 8*I*c*d*f^2*x*\cos(2*c*f/d)*\sin_integral(2*(d*f*x + c*f)/d) + 8*c*d*f^2*x*\sin(2*c*f/d)*\sin_integral(2*(d*f*x + c*f)/d) + 4*c^2*f^2*\cos(2*c*f/d)*\cos_integral(-2*(d*f*x + c*f)/d) + 4*I*c^2*f^2*\cos_integral(-2*(d*f*x + c*f)/d)*\sin(2*c*f/d) - 4*I*c^2*f^2*\cos(2*c*f/d)*\sin_integral(2*(d*f*x + c*f)/d) + 4*c^2*f^2*\sin(2*c*f/d)*\sin_integral(2*(d*f*x + c*f)/d) - 2*I*d^2*f*x*\cos(2*f*x) - 2*d^2*f*x*\sin(2*f*x) - 2*I*c*d*f*\cos(2*f*x) - 2*c*d*f*\sin(2*f*x) + d^2*\cos(2*f*x) + d^2*\cos(2*e) - I*d^2*\sin(2*f*x) + I*d^2*\sin(2*e))/(4*a*d^5*x^2*\cos(2*e) + 4*I*a*d^5*x^2*\sin(2*e) + 8*a*c*d^4*x*\cos(2*e) + 8*I*a*c*d^4*x*\sin(2*e) + 4*a*c^2*d^3*\cos(2*e) + 4*I*a*c^2*d^3*\sin(2*e))$

maple [A] time = 0.49, size = 358, normalized size = 1.58

$$\frac{if^3 \left(\frac{\sin(2fx+2e)}{((fx+e)d+cf-de)^2} + \frac{2\cos(2fx+2e)}{((fx+e)d+cf-de)d} - \frac{2 \left(\frac{2\text{Si}\left(2fx+2e+\frac{2cf-2de}{d}\right)\cos\left(\frac{2cf-2de}{d}\right) - 2\text{Ci}\left(2fx+2e+\frac{2cf-2de}{d}\right)\sin\left(\frac{2cf-2de}{d}\right)}{d} \right)}{d} \right)}{4} + \frac{f^3 \frac{\cos(2fx+2e)}{((fx+e)d+cf-de)^2}}{af}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^3/(a+I*a*tan(f*x+e)),x)

[Out] $1/a/f*(-1/4*I*f^3*(-\sin(2*f*x+2*e))/((f*x+e)*d+c*f-d*e)^2/d+(-2*\cos(2*f*x+2*e))/((f*x+e)*d+c*f-d*e)/d-2*(2*\text{Si}(2*f*x+2*e+2*(c*f-d*e)/d)*\cos(2*(c*f-d*e)/d)/d-2*\text{Ci}(2*f*x+2*e+2*(c*f-d*e)/d)*\sin(2*(c*f-d*e)/d)/d)/d)+1/4*f^3*(-\cos(2*f*x+2*e))/((f*x+e)*d+c*f-d*e)^2/d-(-2*\sin(2*f*x+2*e))/((f*x+e)*d+c*f-d*e)/d+2*(2*\text{Si}(2*f*x+2*e+2*(c*f-d*e)/d)*\sin(2*(c*f-d*e)/d)/d+2*\text{Ci}(2*f*x+2*e+2*(c*f-d*e)/d)*\cos(2*(c*f-d*e)/d)/d)/d)-1/4*f^3/((f*x+e)*d+c*f-d*e)^2/d)$

maxima [A] time = 1.05, size = 156, normalized size = 0.69

$$\frac{2f^3 \cos\left(-\frac{2(de-cf)}{d}\right) E_3\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) + 2if^3 E_3\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) \sin\left(-\frac{2(de-cf)}{d}\right) + f^3}{4\left((fx+e)^2 ad^3 + ad^3 e^2 - 2acd^2 ef + ac^2 d f^2 - 2(ad^3 e - acd^2 f)(fx+e)\right) f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^3/(a+I*a*tan(f*x+e)),x, algorithm="maxima")

[Out] $-1/4*(2*f^3*\cos(-2*(d*e - c*f)/d)*\exp_integral_e(3, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d) + 2*I*f^3*\exp_integral_e(3, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d)*\sin(-2*(d*e - c*f)/d) + f^3)/(((f*x + e)^2*a*d^3 + a*d^3*e^2 - 2*a*c*d^2*e*f + a*c^2*d*f^2 - 2*(a*d^3*e - a*c*d^2*f)*(f*x + e))*f)$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + a \tan(e + f x) i) (c + d x)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + a*tan(e + f*x)*1i)*(c + d*x)^3), x)`

[Out] `int(1/((a + a*tan(e + f*x)*1i)*(c + d*x)^3), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{i \int \frac{1}{c^3 \tan(e+fx) - ic^3 + 3c^2 dx \tan(e+fx) - 3ic^2 dx + 3cd^2 x^2 \tan(e+fx) - 3icd^2 x^2 + d^3 x^3 \tan(e+fx) - id^3 x^3} dx}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x+c)**3/(a+I*a*tan(f*x+e)), x)`

[Out] `-I*Integral(1/(c**3*tan(e + f*x) - I*c**3 + 3*c**2*d*x*tan(e + f*x) - 3*I*c**2*d*x + 3*c*d**2*x**2*tan(e + f*x) - 3*I*c*d**2*x**2 + d**3*x**3*tan(e + f*x) - I*d**3*x**3), x)/a`

$$3.24 \quad \int \frac{(c+dx)^3}{(a+ia \tan(e+fx))^2} dx$$

Optimal. Leaf size=270

$$\frac{3id^2(c+dx)e^{-2ie-2ifx}}{8a^2f^3} - \frac{3id^2(c+dx)e^{-4ie-4ifx}}{128a^2f^3} + \frac{3d(c+dx)^2e^{-2ie-2ifx}}{8a^2f^2} + \frac{3d(c+dx)^2e^{-4ie-4ifx}}{64a^2f^2} + \frac{i(c+dx)^3e^{-2ie-2ifx}}{4a^2f}$$

[Out] $-3/16*d^3*\exp(-2*I*e-2*I*f*x)/a^2/f^4-3/512*d^3*\exp(-4*I*e-4*I*f*x)/a^2/f^4-3/8*I*d^2*\exp(-2*I*e-2*I*f*x)*(d*x+c)/a^2/f^3-3/128*I*d^2*\exp(-4*I*e-4*I*f*x)*(d*x+c)/a^2/f^3+3/8*d*\exp(-2*I*e-2*I*f*x)*(d*x+c)^2/a^2/f^2+3/64*d*\exp(-4*I*e-4*I*f*x)*(d*x+c)^2/a^2/f^2+1/4*I*\exp(-2*I*e-2*I*f*x)*(d*x+c)^3/a^2/f+1/16*I*\exp(-4*I*e-4*I*f*x)*(d*x+c)^3/a^2/f+1/16*(d*x+c)^4/a^2/d$

Rubi [A] time = 0.29, antiderivative size = 270, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {3729, 2176, 2194}

$$\frac{3id^2(c+dx)e^{-2ie-2ifx}}{8a^2f^3} - \frac{3id^2(c+dx)e^{-4ie-4ifx}}{128a^2f^3} + \frac{3d(c+dx)^2e^{-2ie-2ifx}}{8a^2f^2} + \frac{3d(c+dx)^2e^{-4ie-4ifx}}{64a^2f^2} + \frac{i(c+dx)^3e^{-2ie-2ifx}}{4a^2f}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + I*a*Tan[e + f*x])^2, x]

[Out] $(-3*d^3*E^{((-2*I)*e - (2*I)*f*x))/(16*a^2*f^4) - (3*d^3*E^{((-4*I)*e - (4*I)*f*x))/(512*a^2*f^4) - (((3*I)/8)*d^2*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)})/(a^2*f^3) - (((3*I)/128)*d^2*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)})/(a^2*f^3) + (3*d*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)^2})/(8*a^2*f^2) + (3*d*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)^2})/(64*a^2*f^2) + ((I/4)*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)^3})/(a^2*f) + ((I/16)*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)^3})/(a^2*f) + (c + d*x)^4/(16*a^2*d)$

Rule 2176

Int[((b_.)*(F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] := Simp[((c + d*x)^m*(b*F^(g*(e + f*x)))^n)/(f*g*n*Log[F]), x] - Dist[(d*m)/(f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*(b*F^(g*(e + f*x)))^n, x], x] /; FreeQ[{F, b, c, d, e, f, g, n}, x] && GtQ[m, 0] && IntegerQ[2*m] && !\$UseGamma == True

Rule 2194

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 3729

Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + E^((2*a*(e + f*x))/b)/(2*a))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[a^2 + b^2, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^3}{(a+ia \tan(e+fx))^2} dx &= \int \left(\frac{(c+dx)^3}{4a^2} + \frac{e^{-2ie-2ifx}(c+dx)^3}{2a^2} + \frac{e^{-4ie-4ifx}(c+dx)^3}{4a^2} \right) dx \\
&= \frac{(c+dx)^4}{16a^2d} + \frac{\int e^{-4ie-4ifx}(c+dx)^3 dx}{4a^2} + \frac{\int e^{-2ie-2ifx}(c+dx)^3 dx}{2a^2} \\
&= \frac{ie^{-2ie-2ifx}(c+dx)^3}{4a^2f} + \frac{ie^{-4ie-4ifx}(c+dx)^3}{16a^2f} + \frac{(c+dx)^4}{16a^2d} - \frac{(3id) \int e^{-4ie-4ifx}(c+dx)^2 dx}{16a^2f} \\
&= \frac{3de^{-2ie-2ifx}(c+dx)^2}{8a^2f^2} + \frac{3de^{-4ie-4ifx}(c+dx)^2}{64a^2f^2} + \frac{ie^{-2ie-2ifx}(c+dx)^3}{4a^2f} + \frac{ie^{-4ie-4ifx}(c+dx)^3}{16a^2f} \\
&= -\frac{3id^2e^{-2ie-2ifx}(c+dx)}{8a^2f^3} - \frac{3id^2e^{-4ie-4ifx}(c+dx)}{128a^2f^3} + \frac{3de^{-2ie-2ifx}(c+dx)^2}{8a^2f^2} + \frac{3de^{-4ie-4ifx}(c+dx)^2}{64a^2f^2} \\
&= -\frac{3d^3e^{-2ie-2ifx}}{16a^2f^4} - \frac{3d^3e^{-4ie-4ifx}}{512a^2f^4} - \frac{3id^2e^{-2ie-2ifx}(c+dx)}{8a^2f^3} - \frac{3id^2e^{-4ie-4ifx}(c+dx)}{128a^2f^3} + \frac{3d^3e^{-2ie-2ifx}}{16a^2f^4}
\end{aligned}$$

Mathematica [A] time = 1.38, size = 473, normalized size = 1.75

$$\sec^2(e+fx)(\cos(fx)+i\sin(fx))^2 \left(f^4x(4c^3+6c^2dx+4cd^2x^2+d^3x^3)(\cos(2e)+i\sin(2e)) + \frac{1}{32}(\cos(2e)-i\sin(2e)) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + I*a*Tan[e + f*x])^2,x]

[Out] (Sec[e + f*x]^2*(Cos[f*x] + I*Sin[f*x])^2*(((4*I)*c^3*f^3 + 6*c^2*d*f^2*(1 + (2*I)*f*x) + 6*c*d^2*f*(-I + 2*f*x + (2*I)*f^2*x^2) + d^3*(-3 - (6*I)*f*x + 6*f^2*x^2 + (4*I)*f^3*x^3))*Cos[2*f*x] + (((32*I)*c^3*f^3 + 24*c^2*d*f^2*(1 + (4*I)*f*x) + 12*c*d^2*f*(-I + 4*f*x + (8*I)*f^2*x^2) + d^3*(-3 - (12*I)*f*x + 24*f^2*x^2 + (32*I)*f^3*x^3))*Cos[4*f*x]*(Cos[2*e] - I*Sin[2*e]))/32 + f^4*x*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d^3*x^3)*(Cos[2*e] + I*Sin[2*e])) + (4*c^3*f^3 + 6*c^2*d*f^2*(-I + 2*f*x) + 6*c*d^2*f*(-1 - (2*I)*f*x + 2*f^2*x^2) + d^3*(3*I - 6*f*x - (6*I)*f^2*x^2 + 4*f^3*x^3))*Sin[2*f*x] + ((32*c^3*f^3 + 24*c^2*d*f^2*(-I + 4*f*x) + 12*c*d^2*f*(-1 - (4*I)*f*x + 8*f^2*x^2) + d^3*(3*I - 12*f*x - (24*I)*f^2*x^2 + 32*f^3*x^3))*(Cos[2*e] - I*Sin[2*e])*Sin[4*f*x])/32)/(16*f^4*(a + I*a*Tan[e + f*x])^2)

fricas [A] time = 0.54, size = 262, normalized size = 0.97

$$\left(32i d^3 f^3 x^3 + 32i c^3 f^3 + 24 c^2 d f^2 - 12i c d^2 f - 3 d^3 + (96i c d^2 f^3 + 24 d^3 f^2) x^2 + (96i c^2 d f^3 + 48 c d^2 f^2 - 12i d^3 f) x + 32i d^3 f^3 \right) / (16 f^4 (a + I a \tan(e + f x))^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e))^2,x, algorithm="fricas")

[Out] 1/512*(32*I*d^3*f^3*x^3 + 32*I*c^3*f^3 + 24*c^2*d*f^2 - 12*I*c*d^2*f - 3*d^3 + (96*I*c*d^2*f^3 + 24*d^3*f^2)*x^2 + (96*I*c^2*d*f^3 + 48*c*d^2*f^2 - 12*I*d^3*f)*x + 32*(d^3*f^4*x^4 + 4*c*d^2*f^4*x^3 + 6*c^2*d*f^4*x^2 + 4*c^3*f^4*x)*e^(4*I*f*x + 4*I*e) + (128*I*d^3*f^3*x^3 + 128*I*c^3*f^3 + 192*c^2*d*f^2 - 192*I*c*d^2*f - 96*d^3 + (384*I*c*d^2*f^3 + 192*d^3*f^2)*x^2 + (384*I*c^2*d*f^3 + 384*c*d^2*f^2 - 192*I*d^3*f)*x)*e^(2*I*f*x + 2*I*e))*e^(-4*I*f*x - 4*I*e)/(a^2*f^4)

giac [A] time = 0.95, size = 383, normalized size = 1.42

$$\left(32 d^3 f^4 x^4 e^{(4i f x + 4i e)} + 128 c d^2 f^4 x^3 e^{(4i f x + 4i e)} + 192 c^2 d f^4 x^2 e^{(4i f x + 4i e)} + 128 i d^3 f^3 x^3 e^{(2i f x + 2i e)} + 32 i d^3 f^3 x^3 + 128 i d^3 f^3 x^3 \right) / (16 f^4 (a + I a \tan(e + f x))^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e))^2,x, algorithm="giac")

[Out] $\frac{1}{512}*(32*d^3*f^4*x^4*e^{(4*I*f*x + 4*I*e)} + 128*c*d^2*f^4*x^3*e^{(4*I*f*x + 4*I*e)} + 192*c^2*d*f^4*x^2*e^{(4*I*f*x + 4*I*e)} + 128*I*d^3*f^3*x^3*e^{(2*I*f*x + 2*I*e)} + 32*I*d^3*f^3*x^3 + 128*c^3*f^4*x*e^{(4*I*f*x + 4*I*e)} + 384*I*c*d^2*f^3*x^2*e^{(2*I*f*x + 2*I*e)} + 96*I*c*d^2*f^3*x^2 + 384*I*c^2*d*f^3*x*e^{(2*I*f*x + 2*I*e)} + 192*d^3*f^2*x^2*e^{(2*I*f*x + 2*I*e)} + 96*I*c^2*d*f^3*x + 24*d^3*f^2*x^2 + 128*I*c^3*f^3*e^{(2*I*f*x + 2*I*e)} + 384*c*d^2*f^2*x*e^{(2*I*f*x + 2*I*e)} + 32*I*c^3*f^3 + 48*c*d^2*f^2*x + 192*c^2*d*f^2*e^{(2*I*f*x + 2*I*e)} - 192*I*d^3*f*x*e^{(2*I*f*x + 2*I*e)} + 24*c^2*d*f^2 - 12*I*d^3*f*x - 192*I*c*d^2*f*e^{(2*I*f*x + 2*I*e)} - 12*I*c*d^2*f - 96*d^3*e^{(2*I*f*x + 2*I*e)} - 3*d^3)*e^{(-4*I*f*x - 4*I*e)}/(a^2*f^4)$

maple [B] time = 0.87, size = 2070, normalized size = 7.67

Expression too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(a+I*a*tan(f*x+e))^2,x)

[Out] $\frac{1}{a^2/f}*(-3/f^2*c*d^2*((f*x+e)^2*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+1/2*(f*x+e)*\cos(f*x+e)^2-1/4*\sin(f*x+e)*\cos(f*x+e)-1/4*f*x-1/4*e-1/3*(f*x+e)^3)+3/f^3*d^3*e*((f*x+e)^2*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+1/2*(f*x+e)*\cos(f*x+e)^2-1/4*\sin(f*x+e)*\cos(f*x+e)-1/4*f*x-1/4*e-1/3*(f*x+e)^3)-3/f*c^2*d*((f*x+e)*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*\sin(f*x+e)^2)-3/f^3*d^3*e^2*((f*x+e)*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*\sin(f*x+e)^2)+1/f^3*d^3*e^3*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+6/f*c^2*d*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)-6/f^3*d^3*e*((f*x+e)^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+1/8*(f*x+e)*\cos(f*x+e)^4-1/32*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)-15/64*f*x-15/64*e+3/8*(f*x+e)*\cos(f*x+e)^2-3/16*\sin(f*x+e)*\cos(f*x+e)-1/4*(f*x+e)^3)+6/f^3*d^3*e^2*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)+6/f^2*c*d^2*((f*x+e)^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+1/8*(f*x+e)*\cos(f*x+e)^4-1/32*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)-15/64*f*x-15/64*e+3/8*(f*x+e)*\cos(f*x+e)^2-3/16*\sin(f*x+e)*\cos(f*x+e)-1/4*(f*x+e)^3)-2/f^3*d^3*e^3*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-2*I/f^3*d^3*(-1/4*(f*x+e)^3*\cos(f*x+e)^4+3/4*(f*x+e)^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+3/32*(f*x+e)*\cos(f*x+e)^4-3/128*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)-45/256*f*x-45/256*e+9/32*(f*x+e)*\cos(f*x+e)^2-9/64*\sin(f*x+e)*\cos(f*x+e)-3/16*(f*x+e)^3)+3/2*I/f^2*c*d^2*e^2*\cos(f*x+e)^4-3/2*I/f*c^2*d*e*\cos(f*x+e)^4+12*I/f^2*c*d^2*e*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)-1/f^3*d^3*((f*x+e)^3*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+3/4*(f*x+e)^2*\cos(f*x+e)^2-3/2*(f*x+e)*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+3/8*(f*x+e)^2+3/8*\sin(f*x+e)^2-3/8*(f*x+e)^4)+6/f^2*c*d^2*e^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-6/f*c^2*d*e*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-1/2*I/f^3*d^3*e^3*\cos(f*x+e)^4-6*I/f*c^2*d*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)+6*I/f^3*d^3*e*(-1/4*(f*x+e)^2*\cos(f*x+e)^4+1/2*(f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/32*(f*x+e)^2+1/32*\cos(f*x+e)^4+3/32*\cos(f*x+e)^2)-6*I/f^2*c*d^2*(-1/4*(f*x+e)^2*\cos(f*x+e)^4+1/2*(f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/32*(f*x+e)^2+1/32*\cos(f*x+e)^4+3/32*\cos(f*x+e)^2)-6*I/f^3*d^3*e^2*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)-12/f^2*c*d^2*e*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3$


```

*8*exp(6*I*e), 0)), (x**4*(2*d**3*exp(2*I*e) + d**3)*exp(-4*I*e)/(16*a**2)
+ x**3*(2*c*d**2*exp(2*I*e) + c*d**2)*exp(-4*I*e)/(4*a**2) + x**2*(6*c**2*d
*exp(2*I*e) + 3*c**2*d)*exp(-4*I*e)/(8*a**2) + x*(2*c**3*exp(2*I*e) + c**3)
*exp(-4*I*e)/(4*a**2), True)) + c**3*x/(4*a**2) + 3*c**2*d*x**2/(8*a**2) +
c*d**2*x**3/(4*a**2) + d**3*x**4/(16*a**2)

```

$$3.25 \quad \int \frac{(c+dx)^2}{(a+ia \tan(e+fx))^2} dx$$

Optimal. Leaf size=202

$$\frac{d(c+dx)e^{-2ie-2ifx}}{4a^2f^2} + \frac{d(c+dx)e^{-4ie-4ifx}}{32a^2f^2} + \frac{i(c+dx)^2e^{-2ie-2ifx}}{4a^2f} + \frac{i(c+dx)^2e^{-4ie-4ifx}}{16a^2f} + \frac{(c+dx)^3}{12a^2d} - \frac{id^2e^{-2ie-2ifx}}{8a^2f^3} - \frac{id^2e^{-4ie-4ifx}}{128a^2f^3}$$

[Out] $-1/8*I*d^2*\exp(-2*I*e-2*I*f*x)/a^2/f^3-1/128*I*d^2*\exp(-4*I*e-4*I*f*x)/a^2/f^3+1/4*d*\exp(-2*I*e-2*I*f*x)*(d*x+c)/a^2/f^2+1/32*d*\exp(-4*I*e-4*I*f*x)*(d*x+c)/a^2/f^2+1/4*I*\exp(-2*I*e-2*I*f*x)*(d*x+c)^2/a^2/f+1/16*I*\exp(-4*I*e-4*I*f*x)*(d*x+c)^2/a^2/f+1/12*(d*x+c)^3/a^2/d$

Rubi [A] time = 0.21, antiderivative size = 202, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {3729, 2176, 2194}

$$\frac{d(c+dx)e^{-2ie-2ifx}}{4a^2f^2} + \frac{d(c+dx)e^{-4ie-4ifx}}{32a^2f^2} + \frac{i(c+dx)^2e^{-2ie-2ifx}}{4a^2f} + \frac{i(c+dx)^2e^{-4ie-4ifx}}{16a^2f} + \frac{(c+dx)^3}{12a^2d} - \frac{id^2e^{-2ie-2ifx}}{8a^2f^3} - \frac{id^2e^{-4ie-4ifx}}{128a^2f^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + I*a*Tan[e + f*x])^2,x]

[Out] $((-I/8)*d^2*E^{((-2*I)*e - (2*I)*f*x))/(a^2*f^3) - ((I/128)*d^2*E^{((-4*I)*e - (4*I)*f*x))/(a^2*f^3) + (d*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)})/(4*a^2*f^2) + (d*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)})/(32*a^2*f^2) + ((I/4)*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)^2})/(a^2*f) + ((I/16)*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)^2})/(a^2*f) + (c + d*x)^3/(12*a^2*d)$

Rule 2176

Int[((b_.)*(F_)^(g_.)*((e_.) + (f_.)*(x_)))^(n_.)*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[((c + d*x)^m*(b*F^(g*(e + f*x)))^n)/(f*g*n*Log[F]), x] - Dist[(d*m)/(f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*(b*F^(g*(e + f*x)))^n, x], x] /; FreeQ[{F, b, c, d, e, f, g, n}, x] && GtQ[m, 0] && IntegerQ[2*m] && !\$UseGamma == True

Rule 2194

Int[((F_)^(c_.)*((a_.) + (b_.)*(x_)))^(n_.), x_Symbol] :> Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 3729

Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] :> Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + E^(2*a*(e + f*x))/b)/(2*a))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[a^2 + b^2, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^2}{(a+ia \tan(e+fx))^2} dx &= \int \left(\frac{(c+dx)^2}{4a^2} + \frac{e^{-2ie-2ifx}(c+dx)^2}{2a^2} + \frac{e^{-4ie-4ifx}(c+dx)^2}{4a^2} \right) dx \\
&= \frac{(c+dx)^3}{12a^2d} + \frac{\int e^{-4ie-4ifx}(c+dx)^2 dx}{4a^2} + \frac{\int e^{-2ie-2ifx}(c+dx)^2 dx}{2a^2} \\
&= \frac{ie^{-2ie-2ifx}(c+dx)^2}{4a^2f} + \frac{ie^{-4ie-4ifx}(c+dx)^2}{16a^2f} + \frac{(c+dx)^3}{12a^2d} - \frac{(id) \int e^{-4ie-4ifx}(c+dx) dx}{8a^2f} \\
&= \frac{de^{-2ie-2ifx}(c+dx)}{4a^2f^2} + \frac{de^{-4ie-4ifx}(c+dx)}{32a^2f^2} + \frac{ie^{-2ie-2ifx}(c+dx)^2}{4a^2f} + \frac{ie^{-4ie-4ifx}(c+dx)}{16a^2f} \\
&= -\frac{id^2e^{-2ie-2ifx}}{8a^2f^3} - \frac{id^2e^{-4ie-4ifx}}{128a^2f^3} + \frac{de^{-2ie-2ifx}(c+dx)}{4a^2f^2} + \frac{de^{-4ie-4ifx}(c+dx)}{32a^2f^2} + \frac{ie^{-2ie-2ifx}(c+dx)^2}{4a^2f} + \frac{ie^{-4ie-4ifx}(c+dx)}{16a^2f}
\end{aligned}$$

Mathematica [A] time = 0.89, size = 282, normalized size = 1.40

$$\sec^2(e+fx)(\cos(fx)+i\sin(fx))^2 \left(\frac{2}{3}f^3x(3c^2+3cdx+d^2x^2)(\cos(2e)+i\sin(2e)) + \frac{1}{16}(\cos(2e)-i\sin(2e)) \cos(4e+2ifx) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + I*a*Tan[e + f*x])^2, x]

[Out] (Sec[e + f*x]^2*(Cos[f*x] + I*Sin[f*x])^2*((d + (1 + I)*c*f + (1 + I)*d*f*x)*((1 + I)*c*f + d*(-I + (1 + I)*f*x))*Cos[2*f*x] + ((d + (2 + 2*I)*c*f + (2 + 2*I)*d*f*x)*((2 + 2*I)*c*f + d*(-I + (2 + 2*I)*f*x))*Cos[4*f*x]*(Cos[2*e] - I*Sin[2*e]))/16 + (2*f^3*x*(3*c^2 + 3*c*d*x + d^2*x^2)*(Cos[2*e] + I*Sin[2*e]))/3 - I*(d + (1 + I)*c*f + (1 + I)*d*f*x)*((1 + I)*c*f + d*(-I + (1 + I)*f*x))*Sin[2*f*x] - (I/16)*(d + (2 + 2*I)*c*f + (2 + 2*I)*d*f*x)*((2 + 2*I)*c*f + d*(-I + (2 + 2*I)*f*x))*((Cos[2*e] - I*Sin[2*e])*Sin[4*f*x]))/(8*f^3*(a + I*a*Tan[e + f*x])^2)

fricas [A] time = 0.64, size = 160, normalized size = 0.79

$$\frac{(24i d^2 f^2 x^2 + 24i c^2 f^2 + 12 c d f - 3i d^2 + (48i c d f^2 + 12 d^2 f)x + 32(d^2 f^3 x^3 + 3 c d f^3 x^2 + 3 c^2 f^3 x)e^{4i f x + 4i e})}{384 a^2 f^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e))^2,x, algorithm="fricas")

[Out] 1/384*(24*I*d^2*f^2*x^2 + 24*I*c^2*f^2 + 12*c*d*f - 3*I*d^2 + (48*I*c*d*f^2 + 12*d^2*f)*x + 32*(d^2*f^3*x^3 + 3*c*d*f^3*x^2 + 3*c^2*f^3*x)*e^(4*I*f*x + 4*I*e) + (96*I*d^2*f^2*x^2 + 96*I*c^2*f^2 + 96*c*d*f - 48*I*d^2 + (192*I*c*d*f^2 + 96*d^2*f)*x)*e^(2*I*f*x + 2*I*e))*e^(-4*I*f*x - 4*I*e)/(a^2*f^3)

giac [A] time = 1.05, size = 227, normalized size = 1.12

$$\frac{(32 d^2 f^3 x^3 e^{4i f x + 4i e} + 96 c d f^3 x^2 e^{4i f x + 4i e} + 96 c^2 f^3 x e^{4i f x + 4i e} + 96i d^2 f^2 x^2 e^{2i f x + 2i e} + 24i d^2 f^2 x^2 + 192i c d f^2 x + 24i c^2 f^2) e^{4i f x + 4i e}}{384 a^2 f^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e))^2,x, algorithm="giac")

[Out] 1/384*(32*d^2*f^3*x^3*e^(4*I*f*x + 4*I*e) + 96*c*d*f^3*x^2*e^(4*I*f*x + 4*I*e) + 96*c^2*f^3*x*e^(4*I*f*x + 4*I*e) + 96*I*d^2*f^2*x^2*e^(2*I*f*x + 2*I*e) + 24i d^2 f^2 x^2 + 192i c d f^2 x + 24i c^2 f^2) e^{4i f x + 4i e}/(a^2 f^3)

$e) + 24*I*d^2*f^2*x^2 + 192*I*c*d*f^2*x*e^{(2*I*f*x + 2*I*e)} + 48*I*c*d*f^2*x + 96*I*c^2*f^2*e^{(2*I*f*x + 2*I*e)} + 96*d^2*f*x*e^{(2*I*f*x + 2*I*e)} + 24*I*c^2*f^2 + 12*d^2*f*x + 96*c*d*f*e^{(2*I*f*x + 2*I*e)} + 12*c*d*f - 48*I*d^2*e^{(2*I*f*x + 2*I*e)} - 3*I*d^2)*e^{(-4*I*f*x - 4*I*e)}/(a^2*f^3)$

maple [B] time = 0.75, size = 968, normalized size = 4.79

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)^2/(a+I*a*tan(f*x+e))^2,x)`

[Out] $1/a^2/f*(-I/f*c*d*e*\cos(f*x+e)^4+1/2*I*c^2*\cos(f*x+e)^4-2*I/f^2*d^2*(-1/4*(f*x+e)^2*\cos(f*x+e)^4+1/2*(f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/32*(f*x+e)^2+1/32*\cos(f*x+e)^4+3/32*\cos(f*x+e)^2)+1/2*I/f^2*d^2*e^2*\cos(f*x+e)^4-4*I/f*c*d*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)+4*I/f^2*d^2*e*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)+2/f^2*d^2*((f*x+e)^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+1/8*(f*x+e)*\cos(f*x+e)^4-1/32*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)-15/64*f*x-15/64*e+3/8*(f*x+e)*\cos(f*x+e)^2-3/16*\sin(f*x+e)*\cos(f*x+e)-1/4*(f*x+e)^3)+4/f*c*d*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)-4/f^2*d^2*e*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)+2*c^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-4/f*c*d*e*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+2/f^2*d^2*e^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-1/f^2*d^2*((f*x+e)^2*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+1/2*(f*x+e)*\cos(f*x+e)^2-1/4*\sin(f*x+e)*\cos(f*x+e)-1/4*f*x-1/4*e-1/3*(f*x+e)^3)-2/f*c*d*((f*x+e)*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*\sin(f*x+e)^2)+2/f^2*d^2*e*((f*x+e)*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)-1/4*(f*x+e)^2-1/4*\sin(f*x+e)^2)-c^2*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)+2/f*c*d*e*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e)-1/f^2*d^2*e^2*(1/2*\sin(f*x+e)*\cos(f*x+e)+1/2*f*x+1/2*e))$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)^2/(a+I*a*tan(f*x+e))^2,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima: expt: undefined: 0 to a negative exponent.

mupad [B] time = 2.99, size = 183, normalized size = 0.91

$\frac{c^2 x}{4 a^2} e^{-e 4 i-f x 4 i} \left(\frac{(-8 c^2 f^2 + c d f 4 i + d^2) 1 i}{128 a^2 f^3} - \frac{d^2 x^2 1 i}{16 a^2 f} + \frac{d x (-4 c f + d 1 i) 1 i}{32 a^2 f^2} \right) e^{-e 2 i-f x 2 i} \left(\frac{(-2 c^2 f^2 + c d f 2 i)}{8 a^2 f^3} \right)$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^2/(a + a*tan(e + f*x)*1i)^2,x)`

[Out] $(c^2*x)/(4*a^2) - \exp(-e*4i - f*x*4i)*(((d^2 - 8*c^2*f^2 + c*d*f*4i)*1i)/(128*a^2*f^3) - (d^2*x^2*1i)/(16*a^2*f) + (d*x*(d*1i - 4*c*f)*1i)/(32*a^2*f^2)) - \exp(-e*2i - f*x*2i)*(((d^2 - 2*c^2*f^2 + c*d*f*2i)*1i)/(8*a^2*f^3) - (d^2*x^2*1i)/(4*a^2*f) + (d*x*(d*1i - 2*c*f)*1i)/(4*a^2*f^2)) + (d^2*x^3)/(12*a^2) + (c*d*x^2)/(4*a^2)$

sympy [A] time = 0.45, size = 420, normalized size = 2.08

$$\left\{ \begin{array}{l} \frac{((64ia^2c^2f^5e^{2ie}+128ia^2cdf^5xe^{2ie}+32a^2cdf^4e^{2ie}+64ia^2d^2f^5x^2e^{2ie}+32a^2d^2f^4xe^{2ie}-8ia^2d^2f^3e^{2ie})e^{-4ifx}+(256ia^2c^2f^5e^{4ie}+512ia^2cdf^5xe^{4ie}+256a^2c^2f^5e^{4ie})}{1024a^4f^6} \\ \frac{x^3(2d^2e^{2ie}+d^2)e^{-4ie}}{12a^2} + \frac{x^2(2cde^{2ie}+cd)e^{-4ie}}{4a^2} + \frac{x(2c^2e^{2ie}+c^2)e^{-4ie}}{4a^2} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(a+I*a*tan(f*x+e))**2,x)

[Out] Piecewise((((64*I*a**2*c**2*f**5*exp(2*I*e) + 128*I*a**2*c*d*f**5*x*exp(2*I*e) + 32*a**2*c*d*f**4*exp(2*I*e) + 64*I*a**2*d**2*f**5*x**2*exp(2*I*e) + 32*a**2*d**2*f**4*x*exp(2*I*e) - 8*I*a**2*d**2*f**3*exp(2*I*e))*exp(-4*I*f*x) + (256*I*a**2*c**2*f**5*exp(4*I*e) + 512*I*a**2*c*d*f**5*x*exp(4*I*e) + 256*a**2*c*d*f**4*exp(4*I*e) + 256*I*a**2*d**2*f**5*x**2*exp(4*I*e) + 256*a**2*d**2*f**4*x*exp(4*I*e) - 128*I*a**2*d**2*f**3*exp(4*I*e))*exp(-2*I*f*x))*exp(-6*I*e)/(1024*a**4*f**6), Ne(1024*a**4*f**6*exp(6*I*e), 0)), (x**3*(2*d**2*exp(2*I*e) + d**2)*exp(-4*I*e)/(12*a**2) + x**2*(2*c*d*exp(2*I*e) + c*d)*exp(-4*I*e)/(4*a**2) + x*(2*c**2*exp(2*I*e) + c**2)*exp(-4*I*e)/(4*a**2), True)) + c**2*x/(4*a**2) + c*d*x**2/(4*a**2) + d**2*x**3/(12*a**2)

$$3.26 \quad \int \frac{c+dx}{(a+ia \tan(e+fx))^2} dx$$

Optimal. Leaf size=151

$$\frac{i(c+dx)}{4f(a^2+ia^2 \tan(e+fx))} + \frac{x(c+dx)}{4a^2} + \frac{3d}{16f^2(a^2+ia^2 \tan(e+fx))} - \frac{3idx}{16a^2f} - \frac{dx^2}{8a^2} + \frac{i(c+dx)}{4f(a+ia \tan(e+fx))^2} + \frac{i(c+dx)}{16f^2(a^2+ia^2 \tan(e+fx))}$$

[Out] $-3/16*I*d*x/a^2/f-1/8*d*x^2/a^2+1/4*x*(d*x+c)/a^2+1/16*d/f^2/(a+I*a*\tan(f*x+e))^2+1/4*I*(d*x+c)/f/(a+I*a*\tan(f*x+e))^2+3/16*d/f^2/(a^2+I*a^2*\tan(f*x+e))+1/4*I*(d*x+c)/f/(a^2+I*a^2*\tan(f*x+e))$

Rubi [A] time = 0.14, antiderivative size = 151, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {3479, 8, 3730}

$$\frac{i(c+dx)}{4f(a^2+ia^2 \tan(e+fx))} + \frac{x(c+dx)}{4a^2} + \frac{3d}{16f^2(a^2+ia^2 \tan(e+fx))} - \frac{3idx}{16a^2f} - \frac{dx^2}{8a^2} + \frac{i(c+dx)}{4f(a+ia \tan(e+fx))^2} + \frac{i(c+dx)}{16f^2(a^2+ia^2 \tan(e+fx))}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + I*a*Tan[e + f*x])^2, x]

[Out] $(((-3*I)/16)*d*x)/(a^2*f) - (d*x^2)/(8*a^2) + (x*(c + d*x))/(4*a^2) + d/(16*f^2*(a + I*a*Tan[e + f*x])^2) + ((I/4)*(c + d*x))/(f*(a + I*a*Tan[e + f*x])^2) + (3*d)/(16*f^2*(a^2 + I*a^2*Tan[e + f*x])) + ((I/4)*(c + d*x))/(f*(a^2 + I*a^2*Tan[e + f*x]))$

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 3479

Int[((a_) + (b_.)*tan[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := Simp[(a*(a + b*Tan[c + d*x])^n)/(2*b*d*n), x] + Dist[1/(2*a), Int[(a + b*Tan[c + d*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[a^2 + b^2, 0] && LtQ[n, 0]

Rule 3730

Int[((c_.) + (d_.)*(x_))^(m_.)*((a_) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] := With[{u = IntHide[(a + b*Tan[e + f*x])^n, x]}, Dist[(c + d*x)^m, u, x] - Dist[d*m, Int[Dist[(c + d*x)^(m - 1), u, x], x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && ILtQ[n, -1] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
\int \frac{c + dx}{(a + ia \tan(e + fx))^2} dx &= \frac{x(c + dx)}{4a^2} + \frac{i(c + dx)}{4f(a + ia \tan(e + fx))^2} + \frac{i(c + dx)}{4f(a^2 + ia^2 \tan(e + fx))} - d \int \left(\frac{x}{4a^2} + \dots \right) \\
&= -\frac{dx^2}{8a^2} + \frac{x(c + dx)}{4a^2} + \frac{i(c + dx)}{4f(a + ia \tan(e + fx))^2} + \frac{i(c + dx)}{4f(a^2 + ia^2 \tan(e + fx))} - \frac{(id)}{8f^2} \\
&= -\frac{dx^2}{8a^2} + \frac{x(c + dx)}{4a^2} + \frac{d}{16f^2(a + ia \tan(e + fx))^2} + \frac{i(c + dx)}{4f(a + ia \tan(e + fx))^2} + \frac{d}{8f^2} \\
&= -\frac{id}{8a^2 f} - \frac{dx^2}{8a^2} + \frac{x(c + dx)}{4a^2} + \frac{d}{16f^2(a + ia \tan(e + fx))^2} + \frac{i(c + dx)}{4f(a + ia \tan(e + fx))^2} \\
&= -\frac{3id}{16a^2 f} - \frac{dx^2}{8a^2} + \frac{x(c + dx)}{4a^2} + \frac{d}{16f^2(a + ia \tan(e + fx))^2} + \frac{i(c + dx)}{4f(a + ia \tan(e + fx))^2}
\end{aligned}$$

Mathematica [A] time = 0.59, size = 130, normalized size = 0.86

$$\frac{\sec^2(e + fx) \left((4cf(1 + 4ifx) + d(8if^2x^2 + 4fx - i)) \sin(2(e + fx)) + (4cf(4fx + i) + d(8f^2x^2 + 4ifx + 1)) \right)}{64a^2f^2(\tan(e + fx) - i)^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + I*a*Tan[e + f*x])^2, x]

[Out] -1/64*(Sec[e + f*x]^2*(8*(d + (2*I)*c*f + (2*I)*d*f*x) + (4*c*f*(I + 4*f*x) + d*(1 + (4*I)*f*x + 8*f^2*x^2))*Cos[2*(e + f*x)] + (4*c*f*(1 + (4*I)*f*x) + d*(-I + 4*f*x + (8*I)*f^2*x^2))*Sin[2*(e + f*x)])/(a^2*f^2*(-I + Tan[e + f*x])^2)

fricas [A] time = 0.61, size = 78, normalized size = 0.52

$$\frac{(4idfx + 4icf + 8(df^2x^2 + 2cf^2x)e^{4ifx+4ie}) + (16idfx + 16icf + 8d)e^{2ifx+2ie} + d)e^{-4ifx-4ie}}{64a^2f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e))^2,x, algorithm="fricas")

[Out] 1/64*(4*I*d*f*x + 4*I*c*f + 8*(d*f^2*x^2 + 2*c*f^2*x)*e^(4*I*f*x + 4*I*e) + (16*I*d*f*x + 16*I*c*f + 8*d)*e^(2*I*f*x + 2*I*e) + d)*e^(-4*I*f*x - 4*I*e)/(a^2*f^2)

giac [A] time = 2.03, size = 107, normalized size = 0.71

$$\frac{(8df^2x^2e^{4ifx+4ie} + 16cf^2xe^{4ifx+4ie} + 16idfxe^{2ifx+2ie} + 4idfx + 16icfe^{2ifx+2ie} + 4icf + 8de^{2ifx+2ie})}{64a^2f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e))^2,x, algorithm="giac")

[Out] 1/64*(8*d*f^2*x^2*e^(4*I*f*x + 4*I*e) + 16*c*f^2*x*e^(4*I*f*x + 4*I*e) + 16*I*d*f*x*e^(2*I*f*x + 2*I*e) + 4*I*d*f*x + 16*I*c*f*e^(2*I*f*x + 2*I*e) + 4*I*c*f + 8*d*e^(2*I*f*x + 2*I*e) + d)*e^(-4*I*f*x - 4*I*e)/(a^2*f^2)

maple [B] time = 0.68, size = 350, normalized size = 2.32

$$\frac{2id \left(\frac{(fx+e)(\cos^4(fx+e))}{4} + \frac{\left(\cos^3(fx+e) + \frac{3\cos(fx+e)}{2} \right) \sin(fx+e)}{16} + \frac{3fx}{32} + \frac{3e}{32} \right)}{f} + \frac{ic(\cos^4(fx+e))}{2} - \frac{ide(\cos^4(fx+e))}{2f} + \frac{2d \left((fx+e) \left(\frac{\cos^3(fx+e) + \frac{3\cos(fx+e)}{2}}{4} \right) \right)}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)/(a+I*a*tan(f*x+e))^2,x)

[Out] $\frac{1}{a^2 f} (-2I/f*d*(-1/4*(f*x+e)*\cos(f*x+e)^4 + 1/16*(\cos(f*x+e)^3 + 3/2*\cos(f*x+e))*\sin(f*x+e) + 3/32*f*x + 3/32*e) + 1/2*I*c*\cos(f*x+e)^4 - 1/2*I/f*d*e*\cos(f*x+e)^4 + 2/f*d*((f*x+e)*(1/4*(\cos(f*x+e)^3 + 3/2*\cos(f*x+e))*\sin(f*x+e) + 3/8*f*x + 3/8*e) - 3/16*(f*x+e)^2 + 1/16*\cos(f*x+e)^4 + 3/16*\cos(f*x+e)^2) + 2*c*(1/4*(\cos(f*x+e)^3 + 3/2*\cos(f*x+e))*\sin(f*x+e) + 3/8*f*x + 3/8*e) - 2/f*d*e*(1/4*(\cos(f*x+e)^3 + 3/2*\cos(f*x+e))*\sin(f*x+e) + 3/8*f*x + 3/8*e) - 1/f*d*((f*x+e)*(1/2*\sin(f*x+e)*\cos(f*x+e) + 1/2*f*x + 1/2*e) - 1/4*(f*x+e)^2 - 1/4*\sin(f*x+e)^2) - c*(1/2*\sin(f*x+e)*\cos(f*x+e) + 1/2*f*x + 1/2*e) + 1/f*d*e*(1/2*\sin(f*x+e)*\cos(f*x+e) + 1/2*f*x + 1/2*e))$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e))^2,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima: expt: undefined: 0 to a negative exponent.

mapad [B] time = 2.77, size = 103, normalized size = 0.68

$$\frac{d x^2}{8 a^2} - e^{-4i-f x 4i} \left(\frac{(-4 c f + d 1i) 1i}{64 a^2 f^2} - \frac{d x 1i}{16 a^2 f} \right) - e^{-2i-f x 2i} \left(\frac{(-2 c f + d 1i) 1i}{8 a^2 f^2} - \frac{d x 1i}{4 a^2 f} \right) + \frac{c x}{4 a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)/(a + a*tan(e + f*x)*1i)^2,x)

[Out] $\frac{(d*x^2)/(8*a^2) - \exp(-e*4i - f*x*4i)*(((d*1i - 4*c*f)*1i)/(64*a^2*f^2) - (d*x*1i)/(16*a^2*f)) - \exp(-e*2i - f*x*2i)*(((d*1i - 2*c*f)*1i)/(8*a^2*f^2) - (d*x*1i)/(4*a^2*f)) + (c*x)/(4*a^2)}$

sympy [A] time = 0.34, size = 228, normalized size = 1.51

$$\begin{cases} \frac{\left((32ia^2cf^3e^{2ie} + 32ia^2df^3xe^{2ie} + 8a^2df^2e^{2ie})e^{-4ifx} + (128ia^2cf^3e^{4ie} + 128ia^2df^3xe^{4ie} + 64a^2df^2e^{4ie})e^{-2ifx} \right) e^{-6ie}}{512a^4f^4} & \text{for } 512a^4f^4e^{6ie} \neq 0 \\ \frac{x^2(2de^{2ie} + d)e^{-4ie}}{8a^2} + \frac{x(2ce^{2ie} + c)e^{-4ie}}{4a^2} & \text{otherwise} \end{cases} + \frac{cx}{4a^2} + \frac{d}{8}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e))**2,x)

[Out] Piecewise((((32*I*a**2*c*f**3*exp(2*I*e) + 32*I*a**2*d*f**3*x*exp(2*I*e) + 8*a**2*d*f**2*exp(2*I*e))*exp(-4*I*f*x) + (128*I*a**2*c*f**3*exp(4*I*e) + 128*I*a**2*d*f**3*x*exp(4*I*e) + 64*a**2*d*f**2*exp(4*I*e))*exp(-2*I*f*x))*exp(-6*I*e)/(512*a**4*f**4), Ne(512*a**4*f**4*exp(6*I*e), 0)), (x**2*(2*d*exp(2*I*e) + d)*exp(-4*I*e)/(8*a**2) + x*(2*c*exp(2*I*e) + c)*exp(-4*I*e)/(4*a**2), True)) + c*x/(4*a**2) + d*x**2/(8*a**2)

$$3.27 \quad \int \frac{1}{(c+dx)(a+ia \tan(e+fx))^2} dx$$

Optimal. Leaf size=305

$$\frac{i\text{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{2a^2d} - \frac{i\text{Ci}\left(4xf + \frac{4cf}{d}\right) \sin\left(4e - \frac{4cf}{d}\right)}{4a^2d} + \frac{\text{Ci}\left(2xf + \frac{2cf}{d}\right) \cos\left(2e - \frac{2cf}{d}\right)}{2a^2d} + \frac{\text{Ci}\left(4xf + \frac{4cf}{d}\right) \cos\left(4e - \frac{4cf}{d}\right)}{4a^2d}$$

[Out] $\frac{1}{4} \text{Ci}\left(\frac{4cf}{d} + 4fx\right) \cos\left(4e - \frac{4cf}{d}\right) / a^{2/d} + \frac{1}{2} \text{Ci}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right) / a^{2/d} + \frac{1}{4} \ln(d*x+c) / a^{2/d} - \frac{1}{2} I \cos\left(-2e + \frac{2cf}{d}\right) \text{Si}\left(\frac{2cf}{d} + 2fx\right) / a^{2/d} - \frac{1}{4} I \cos\left(-4e + \frac{4cf}{d}\right) \text{Si}\left(\frac{4cf}{d} + 4fx\right) / a^{2/d} + \frac{1}{4} I \text{Ci}\left(\frac{4cf}{d} + 4fx\right) \sin\left(-4e + \frac{4cf}{d}\right) / a^{2/d} + \frac{1}{4} \text{Si}\left(\frac{4cf}{d} + 4fx\right) \sin\left(-4e + \frac{4cf}{d}\right) / a^{2/d} + \frac{1}{2} I \text{Ci}\left(\frac{2cf}{d} + 2fx\right) \sin\left(-2e + \frac{2cf}{d}\right) / a^{2/d} + \frac{1}{2} \text{Si}\left(\frac{2cf}{d} + 2fx\right) \sin\left(-2e + \frac{2cf}{d}\right) / a^{2/d}$

Rubi [A] time = 0.77, antiderivative size = 305, normalized size of antiderivative = 1.00, number of steps used = 21, number of rules used = 5, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.217$, Rules used = {3728, 3303, 3299, 3302, 3312}

$$\frac{i\text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{2a^2d} - \frac{i\text{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{4a^2d} + \frac{\text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right)}{2a^2d} + \frac{\text{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \cos\left(4e - \frac{4cf}{d}\right)}{4a^2d}$$

Antiderivative was successfully verified.

[In] Int[1/((c + d*x)*(a + I*a*Tan[e + f*x])^2), x]

[Out] $\frac{\text{Cos}\left[2e - \frac{2cf}{d}\right] \text{CosIntegral}\left[\frac{2cf}{d} + 2fx\right]}{2a^{2d}} + \frac{\text{Cos}\left[4e - \frac{4cf}{d}\right] \text{CosIntegral}\left[\frac{4cf}{d} + 4fx\right]}{4a^{2d}} + \frac{\text{Log}[c + d*x]}{4a^{2d}} - \frac{(I/4) \text{CosIntegral}\left[\frac{4cf}{d} + 4fx\right] \text{Sin}\left[4e - \frac{4cf}{d}\right]}{a^{2d}} - \frac{(I/2) \text{CosIntegral}\left[\frac{2cf}{d} + 2fx\right] \text{Sin}\left[2e - \frac{2cf}{d}\right]}{a^{2d}} - \frac{(I/2) \text{Cos}\left[2e - \frac{2cf}{d}\right] \text{SinIntegral}\left[\frac{2cf}{d} + 2fx\right]}{a^{2d}} - \frac{\text{Sin}\left[2e - \frac{2cf}{d}\right] \text{SinIntegral}\left[\frac{2cf}{d} + 2fx\right]}{2a^{2d}} - \frac{(I/4) \text{Cos}\left[4e - \frac{4cf}{d}\right] \text{SinIntegral}\left[\frac{4cf}{d} + 4fx\right]}{a^{2d}} - \frac{\text{Sin}\left[4e - \frac{4cf}{d}\right] \text{SinIntegral}\left[\frac{4cf}{d} + 4fx\right]}{4a^{2d}}$

Rule 3299

Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rule 3303

Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3312

Int[((c_) + (d_)*(x_))^(m_)*sin[(e_) + (f_)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3728

```
Int[((c_.) + (d_.)*(x_))^(m_)*((a_) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_),
x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + Cos[2*e + 2*f*x]/(
2*a) + Sin[2*e + 2*f*x]/(2*b))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f}, x]
&& EqQ[a^2 + b^2, 0] && ILtQ[m, 0] && ILtQ[n, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{(c+dx)(a+ia \tan(e+fx))^2} dx &= \int \left(\frac{1}{4a^2(c+dx)} + \frac{\cos(2e+2fx)}{2a^2(c+dx)} + \frac{\cos^2(2e+2fx)}{4a^2(c+dx)} - \frac{i \sin(2e+2fx)}{2a^2(c+dx)} - \frac{\sin^2(2e+2fx)}{4a^2(c+dx)} \right) dx \\ &= \frac{\log(c+dx)}{4a^2d} - \frac{i \int \frac{\sin(4e+4fx)}{c+dx} dx}{4a^2} - \frac{i \int \frac{\sin(2e+2fx)}{c+dx} dx}{2a^2} + \frac{\int \frac{\cos^2(2e+2fx)}{c+dx} dx}{4a^2} - \frac{\int \frac{\sin^2(2e+2fx)}{c+dx} dx}{4a^2} \\ &= \frac{\log(c+dx)}{4a^2d} - \frac{\int \left(\frac{1}{2(c+dx)} - \frac{\cos(4e+4fx)}{2(c+dx)} \right) dx}{4a^2} + \frac{\int \left(\frac{1}{2(c+dx)} + \frac{\cos(4e+4fx)}{2(c+dx)} \right) dx}{4a^2} \\ &= \frac{\cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{2a^2d} + \frac{\log(c+dx)}{4a^2d} - \frac{i \text{Ci}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{4a^2d} \\ &= \frac{\cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{2a^2d} + \frac{\log(c+dx)}{4a^2d} - \frac{i \text{Ci}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{4a^2d} \\ &= \frac{\cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{2a^2d} + \frac{\log(c+dx)}{4a^2d} - \frac{i \text{Ci}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{4a^2d} \end{aligned}$$

Mathematica [A] time = 0.52, size = 211, normalized size = 0.69

$$\frac{\left(\cos\left(2e - \frac{2cf}{d}\right) - i \sin\left(2e - \frac{2cf}{d}\right)\right) \left(\text{Ci}\left(\frac{4f(c+dx)}{d}\right) \left(\cos\left(2e - \frac{2cf}{d}\right) - i \sin\left(2e - \frac{2cf}{d}\right)\right) + 2\text{Ci}\left(\frac{2f(c+dx)}{d}\right) - \sin\left(2e - \frac{2cf}{d}\right)\right)}{4a^2d}$$

Warning: Unable to verify antiderivative.

[In] Integrate[1/((c + d*x)*(a + I*a*Tan[e + f*x])^2), x]

[Out] ((Cos[2*e - (2*c*f)/d] - I*Sin[2*e - (2*c*f)/d])*(2*CosIntegral[(2*f*(c + d*x))/d] + Cos[2*e - (2*c*f)/d]*Log[f*(c + d*x)] + CosIntegral[(4*f*(c + d*x))/d]*(Cos[2*e - (2*c*f)/d] - I*Sin[2*e - (2*c*f)/d]) + I*Log[f*(c + d*x)]*Sin[2*e - (2*c*f)/d] - (2*I)*SinIntegral[(2*f*(c + d*x))/d] - I*Cos[2*e - (2*c*f)/d]*SinIntegral[(4*f*(c + d*x))/d] - Sin[2*e - (2*c*f)/d]*SinIntegral[(4*f*(c + d*x))/d]))/(4*a^2*d)

fricas [A] time = 0.56, size = 80, normalized size = 0.26

$$\frac{2 \text{Ei}\left(\frac{-2i d f x - 2i c f}{d}\right) e^{\left(\frac{-2i d e + 2i c f}{d}\right)} + \text{Ei}\left(\frac{-4i d f x - 4i c f}{d}\right) e^{\left(\frac{-4i d e + 4i c f}{d}\right)} + \log\left(\frac{d x + c}{d}\right)}{4 a^2 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))^2,x, algorithm="fricas")

[Out] 1/4*(2*Ei((-2*I*d*f*x - 2*I*c*f)/d)*e^((-2*I*d*e + 2*I*c*f)/d) + Ei((-4*I*d*f*x - 4*I*c*f)/d)*e^((-4*I*d*e + 4*I*c*f)/d) + log((d*x + c)/d))/(a^2*d)

giac [A] time = 1.14, size = 420, normalized size = 1.38

$$2 \cos\left(\frac{2cf}{d}\right) \cos(2e) \operatorname{Ci}\left(-\frac{2(dfx+cf)}{d}\right) + \cos(2e)^2 \log(dx+c) + 2i \cos(2e) \operatorname{Ci}\left(-\frac{2(dfx+cf)}{d}\right) \sin\left(\frac{2cf}{d}\right) + 2i \cos$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))^2,x, algorithm="giac")

[Out] $\frac{1}{4}*(2*\cos(2*c*f/d)*\cos(2*e)*\cos_integral(-2*(d*f*x + c*f)/d) + \cos(2*e)^2*\log(d*x + c) + 2*I*\cos(2*e)*\cos_integral(-2*(d*f*x + c*f)/d)*\sin(2*c*f/d) + 2*I*\cos(2*c*f/d)*\cos_integral(-2*(d*f*x + c*f)/d)*\sin(2*e) + 2*I*\cos(2*e)*\log(d*x + c)*\sin(2*e) - 2*\cos_integral(-2*(d*f*x + c*f)/d)*\sin(2*c*f/d)*\sin(2*e) - \log(d*x + c)*\sin(2*e)^2 - 2*I*\cos(2*c*f/d)*\cos(2*e)*\sin_integral(2*(d*f*x + c*f)/d) + 2*\cos(2*e)*\sin(2*c*f/d)*\sin_integral(2*(d*f*x + c*f)/d) + 2*\cos(2*c*f/d)*\sin(2*e)*\sin_integral(2*(d*f*x + c*f)/d) + 2*I*\sin(2*c*f/d)*\sin(2*e)*\sin_integral(2*(d*f*x + c*f)/d) + \cos(4*c*f/d)*\cos_integral(-4*(d*f*x + c*f)/d) + I*\cos_integral(-4*(d*f*x + c*f)/d)*\sin(4*c*f/d) - I*\cos(4*c*f/d)*\sin_integral(4*(d*f*x + c*f)/d) + \sin(4*c*f/d)*\sin_integral(4*(d*f*x + c*f)/d))/(a^2*d*\cos(2*e)^2 + 2*I*a^2*d*\cos(2*e)*\sin(2*e) - a^2*d*\sin(2*e)^2)$

maple [A] time = 0.57, size = 382, normalized size = 1.25

$$\frac{i \operatorname{Si}\left(2fx + 2e + \frac{2cf-2de}{d}\right) \cos\left(\frac{2cf-2de}{d}\right)}{2a^2d} + \frac{i \operatorname{Ci}\left(2fx + 2e + \frac{2cf-2de}{d}\right) \sin\left(\frac{2cf-2de}{d}\right)}{2a^2d} - \frac{i \operatorname{Si}\left(4fx + 4e + \frac{4cf-4de}{d}\right) \cos}{4a^2d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)/(a+I*a*tan(f*x+e))^2,x)

[Out] $-1/2*I/a^2*\operatorname{Si}(2*f*x+2*e+2*(c*f-d*e)/d)*\cos(2*(c*f-d*e)/d)/d+1/2*I/a^2*\operatorname{Ci}(2*f*x+2*e+2*(c*f-d*e)/d)*\sin(2*(c*f-d*e)/d)/d-1/4*I/a^2*\operatorname{Si}(4*f*x+4*e+4*(c*f-d*e)/d)*\cos(4*(c*f-d*e)/d)/d+1/4*I/a^2*\operatorname{Ci}(4*f*x+4*e+4*(c*f-d*e)/d)*\sin(4*(c*f-d*e)/d)/d+1/4/a^2*\operatorname{Si}(4*f*x+4*e+4*(c*f-d*e)/d)*\sin(4*(c*f-d*e)/d)/d+1/4/a^2*\operatorname{Ci}(4*f*x+4*e+4*(c*f-d*e)/d)*\cos(4*(c*f-d*e)/d)/d+1/2/a^2*\operatorname{Si}(2*f*x+2*e+2*(c*f-d*e)/d)*\sin(2*(c*f-d*e)/d)/d+1/2/a^2*\operatorname{Ci}(2*f*x+2*e+2*(c*f-d*e)/d)*\cos(2*(c*f-d*e)/d)/d+1/4/a^2*\ln((f*x+e)*d+c*f-d*e)/d$

maxima [A] time = 0.84, size = 190, normalized size = 0.62

$$\frac{f \cos\left(-\frac{4(de-cf)}{d}\right) E_1\left(\frac{4i(fx+e)d-4ide+4icf}{d}\right) + 2f \cos\left(-\frac{2(de-cf)}{d}\right) E_1\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) + 2i f E_1\left(\frac{2i(fx+e)d-2ide}{d}\right)}{4a^2df}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))^2,x, algorithm="maxima")

[Out] $-1/4*(f*\cos(-4*(d*e - c*f)/d)*\exp_integral_e(1, (4*I*(f*x + e)*d - 4*I*d*e + 4*I*c*f)/d) + 2*f*\cos(-2*(d*e - c*f)/d)*\exp_integral_e(1, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d) + 2*I*f*\exp_integral_e(1, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d)*\sin(-2*(d*e - c*f)/d) + I*f*\exp_integral_e(1, (4*I*(f*x + e)*d - 4*I*d*e + 4*I*c*f)/d)*\sin(-4*(d*e - c*f)/d) - f*\log((f*x + e)*d - d*e + c*f))/(a^2*d*f)$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + a \tan(e + fx) i)^2 (c + dx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(1/((a + a*tan(e + f*x)*1i)^2*(c + d*x)),x)`

[Out] `int(1/((a + a*tan(e + f*x)*1i)^2*(c + d*x)), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{1}{c \tan^2(e+fx) - 2ic \tan(e+fx) - c + dx \tan^2(e+fx) - 2idx \tan(e+fx) - dx} dx}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))**2,x)`

[Out] `-Integral(1/(c*tan(e + f*x)**2 - 2*I*c*tan(e + f*x) - c + d*x*tan(e + f*x)*
*2 - 2*I*d*x*tan(e + f*x) - d*x), x)/a**2`

$$3.28 \quad \int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))^2} dx$$

Optimal. Leaf size=436

$$\frac{f \operatorname{Ci}\left(4xf + \frac{4cf}{d}\right) \sin\left(4e - \frac{4cf}{d}\right)}{a^2 d^2} - \frac{f \operatorname{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{a^2 d^2} - \frac{if \operatorname{Ci}\left(2xf + \frac{2cf}{d}\right) \cos\left(2e - \frac{2cf}{d}\right)}{a^2 d^2} - \frac{if \operatorname{Ci}\left(4xf + \frac{4cf}{d}\right) \cos\left(4e - \frac{4cf}{d}\right)}{a^2 d^2}$$

[Out] $-1/4/a^2/d/(d*x+c)-I*f*Ci(4*c*f/d+4*f*x)*\cos(-4*e+4*c*f/d)/a^2/d^2-I*f*Ci(2*c*f/d+2*f*x)*\cos(-2*e+2*c*f/d)/a^2/d^2-1/2*\cos(2*f*x+2*e)/a^2/d/(d*x+c)-1/4*\cos(2*f*x+2*e)^2/a^2/d/(d*x+c)-f*\cos(-2*e+2*c*f/d)*Si(2*c*f/d+2*f*x)/a^2/d^2-f*\cos(-4*e+4*c*f/d)*Si(4*c*f/d+4*f*x)/a^2/d^2+f*Ci(4*c*f/d+4*f*x)*\sin(-4*e+4*c*f/d)/a^2/d^2-I*f*Si(4*c*f/d+4*f*x)*\sin(-4*e+4*c*f/d)/a^2/d^2+f*Ci(2*c*f/d+2*f*x)*\sin(-2*e+2*c*f/d)/a^2/d^2-I*f*Si(2*c*f/d+2*f*x)*\sin(-2*e+2*c*f/d)/a^2/d^2+1/2*I*\sin(2*f*x+2*e)/a^2/d/(d*x+c)+1/4*\sin(2*f*x+2*e)^2/a^2/d/(d*x+c)+1/4*I*\sin(4*f*x+4*e)/a^2/d/(d*x+c)$

Rubi [A] time = 0.74, antiderivative size = 436, normalized size of antiderivative = 1.00, number of steps used = 24, number of rules used = 7, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.304$, Rules used = {3728, 3297, 3303, 3299, 3302, 3313, 12}

$$\frac{f \operatorname{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{a^2 d^2} - \frac{f \operatorname{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{a^2 d^2} - \frac{if \operatorname{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right)}{a^2 d^2} - \frac{if \operatorname{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \cos\left(4e - \frac{4cf}{d}\right)}{a^2 d^2}$$

Antiderivative was successfully verified.

[In] Int[1/((c + d*x)^2*(a + I*a*Tan[e + f*x])^2), x]

[Out] $-1/(4*a^2*d*(c + d*x)) - \operatorname{Cos}[2*e + 2*f*x]/(2*a^2*d*(c + d*x)) - \operatorname{Cos}[2*e + 2*f*x]^2/(4*a^2*d*(c + d*x)) - (I*f*\operatorname{Cos}[2*e - (2*c*f)/d]*\operatorname{CosIntegral}[(2*c*f)/d + 2*f*x])/(a^2*d^2) - (I*f*\operatorname{Cos}[4*e - (4*c*f)/d]*\operatorname{CosIntegral}[(4*c*f)/d + 4*f*x])/(a^2*d^2) - (f*\operatorname{CosIntegral}[(4*c*f)/d + 4*f*x]*\operatorname{Sin}[4*e - (4*c*f)/d])/(a^2*d^2) - (f*\operatorname{CosIntegral}[(2*c*f)/d + 2*f*x]*\operatorname{Sin}[2*e - (2*c*f)/d])/(a^2*d^2) + ((I/2)*\operatorname{Sin}[2*e + 2*f*x])/(a^2*d*(c + d*x)) + \operatorname{Sin}[2*e + 2*f*x]^2/(4*a^2*d*(c + d*x)) + ((I/4)*\operatorname{Sin}[4*e + 4*f*x])/(a^2*d*(c + d*x)) - (f*\operatorname{Cos}[2*e - (2*c*f)/d]*\operatorname{SinIntegral}[(2*c*f)/d + 2*f*x])/(a^2*d^2) + (I*f*\operatorname{Sin}[2*e - (2*c*f)/d]*\operatorname{SinIntegral}[(2*c*f)/d + 2*f*x])/(a^2*d^2) - (f*\operatorname{Cos}[4*e - (4*c*f)/d]*\operatorname{SinIntegral}[(4*c*f)/d + 4*f*x])/(a^2*d^2) + (I*f*\operatorname{Sin}[4*e - (4*c*f)/d]*\operatorname{SinIntegral}[(4*c*f)/d + 4*f*x])/(a^2*d^2)$

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3297

Int[((c_.) + (d_)*(x_))^(m_)*sin[(e_.) + (f_)*(x_)], x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]

Rule 3299

Int[sin[(e_.) + (f_)*(x_)]/((c_.) + (d_)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]
```

Rule 3313

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x]^n)/(d*(m + 1)), x] - Dist[(f*n)/(d*(m + 1)), Int[ExpandTrigReduce[(c + d*x)^(m + 1), Cos[e + f*x]*Sin[e + f*x]^(n - 1), x], x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && GeQ[m, -2] && LtQ[m, -1]
```

Rule 3728

```
Int[((c_.) + (d_.)*(x_))^(m_)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + Cos[2*e + 2*f*x])/(2*a) + Sin[2*e + 2*f*x]/(2*b)]^(n), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && ILtQ[m, 0] && ILtQ[n, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{(c + dx)^2(a + ia \tan(e + fx))^2} dx &= \int \left(\frac{1}{4a^2(c + dx)^2} + \frac{\cos(2e + 2fx)}{2a^2(c + dx)^2} + \frac{\cos^2(2e + 2fx)}{4a^2(c + dx)^2} - \frac{i \sin(2e + 2fx)}{2a^2(c + dx)^2} \right) dx \\ &= -\frac{1}{4a^2 d(c + dx)} - \frac{i \int \frac{\sin(4e + 4fx)}{(c + dx)^2} dx}{4a^2} - \frac{i \int \frac{\sin(2e + 2fx)}{(c + dx)^2} dx}{2a^2} + \frac{\int \frac{\cos^2(2e + 2fx)}{(c + dx)^2} dx}{4a^2} \\ &= -\frac{1}{4a^2 d(c + dx)} - \frac{\cos(2e + 2fx)}{2a^2 d(c + dx)} - \frac{\cos^2(2e + 2fx)}{4a^2 d(c + dx)} + \frac{i \sin(2e + 2fx)}{2a^2 d(c + dx)} + \frac{\sin(2e + 2fx)}{4a^2 d(c + dx)} \\ &= -\frac{1}{4a^2 d(c + dx)} - \frac{\cos(2e + 2fx)}{2a^2 d(c + dx)} - \frac{\cos^2(2e + 2fx)}{4a^2 d(c + dx)} + \frac{i \sin(2e + 2fx)}{2a^2 d(c + dx)} + \frac{\sin(2e + 2fx)}{4a^2 d(c + dx)} \\ &= -\frac{1}{4a^2 d(c + dx)} - \frac{\cos(2e + 2fx)}{2a^2 d(c + dx)} - \frac{\cos^2(2e + 2fx)}{4a^2 d(c + dx)} - \frac{if \cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{4f(c + dx)}{d}\right)}{a^2 d^2} \\ &= -\frac{1}{4a^2 d(c + dx)} - \frac{\cos(2e + 2fx)}{2a^2 d(c + dx)} - \frac{\cos^2(2e + 2fx)}{4a^2 d(c + dx)} - \frac{if \cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{4f(c + dx)}{d}\right)}{a^2 d^2} \end{aligned}$$

Mathematica [A] time = 1.61, size = 467, normalized size = 1.07

$$\frac{\left(\cos\left(2\left(f\left(x - \frac{c}{d}\right) + e\right)\right) - i \sin\left(2\left(f\left(x - \frac{c}{d}\right) + e\right)\right)\right) \left(4f(c + dx) \text{Ci}\left(\frac{4f(c + dx)}{d}\right)\right) \left(\sin\left(2e - \frac{2f(c + dx)}{d}\right) + i \cos\left(2e - \frac{2f(c + dx)}{d}\right)\right)}{4a^2 d^2}$$

Warning: Unable to verify antiderivative.

[In] Integrate[1/((c + d*x)^2*(a + I*a*Tan[e + f*x])^2),x]

[Out]
$$-1/4*((\text{Cos}[2*(e + f*(-(c/d) + x))] - I*\text{Sin}[2*(e + f*(-(c/d) + x))])*(2*d*\text{Cos}[(2*c*f)/d] + d*\text{Cos}[2*(e + f*(-(c/d) + x))] + d*\text{Cos}[2*(e + f*(c/d + x))] - (2*I)*d*\text{Sin}[(2*c*f)/d] + (4*I)*f*(c + d*x)*\text{CosIntegral}[(2*f*(c + d*x))/d]*(\text{Cos}[2*f*x] + I*\text{Sin}[2*f*x]) + I*d*\text{Sin}[2*(e + f*(-(c/d) + x))] - I*d*\text{Sin}[2*(e + f*(c/d + x))] + 4*f*(c + d*x)*\text{CosIntegral}[(4*f*(c + d*x))/d]*(I*\text{Cos}[2*e - (2*f*(c + d*x))/d] + \text{Sin}[2*e - (2*f*(c + d*x))/d]) + 4*c*f*\text{Cos}[2*f*x]*\text{SinIntegral}[(2*f*(c + d*x))/d] + 4*d*f*x*\text{Cos}[2*f*x]*\text{SinIntegral}[(2*f*(c + d*x))/d] + (4*I)*c*f*\text{Sin}[2*f*x]*\text{SinIntegral}[(2*f*(c + d*x))/d] + (4*I)*d*f*x*\text{Sin}[2*f*x]*\text{SinIntegral}[(2*f*(c + d*x))/d] + 4*c*f*\text{Cos}[2*e - (2*f*(c + d*x))/d]*\text{SinIntegral}[(4*f*(c + d*x))/d] + 4*d*f*x*\text{Cos}[2*e - (2*f*(c + d*x))/d]*\text{SinIntegral}[(4*f*(c + d*x))/d] - (4*I)*c*f*\text{Sin}[2*e - (2*f*(c + d*x))/d]*\text{SinIntegral}[(4*f*(c + d*x))/d] - (4*I)*d*f*x*\text{Sin}[2*e - (2*f*(c + d*x))/d]*\text{SinIntegral}[(4*f*(c + d*x))/d]))/(a^2*d^2*(c + d*x))$$

fricas [A] time = 0.44, size = 140, normalized size = 0.32

$$\frac{\left(\left((-4i d f x - 4i c f)\text{Ei}\left(\frac{-2i d f x - 2i c f}{d}\right)e^{\left(\frac{-2i d e + 2i c f}{d}\right)} + (-4i d f x - 4i c f)\text{Ei}\left(\frac{-4i d f x - 4i c f}{d}\right)e^{\left(\frac{-4i d e + 4i c f}{d}\right)} - d\right)e^{(4i f x + 4i e)} - \right)}{4(a^2 d^3 x + a^2 c d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^2,x, algorithm="fricas")

[Out]
$$1/4*(((-4*I*d*f*x - 4*I*c*f)*\text{Ei}((-2*I*d*f*x - 2*I*c*f)/d)*e^{((-2*I*d*e + 2*I*c*f)/d)} + (-4*I*d*f*x - 4*I*c*f)*\text{Ei}((-4*I*d*f*x - 4*I*c*f)/d)*e^{((-4*I*d*e + 4*I*c*f)/d)} - d)*e^{(4*I*f*x + 4*I*e)} - 2*d*e^{(2*I*f*x + 2*I*e)} - d)*e^{(-4*I*f*x - 4*I*e)}/(a^2*d^3*x + a^2*c*d^2)$$

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^2,x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.57, size = 536, normalized size = 1.23

$$if^2 \left[\frac{2 \sin(2fx+2e)}{((fx+e)d+cf-de)d} + \frac{4 \text{Si}\left(2fx+2e+\frac{2cf-2de}{d}\right) \sin\left(\frac{2cf-2de}{d}\right)}{d} + \frac{4 \text{Ci}\left(2fx+2e+\frac{2cf-2de}{d}\right) \cos\left(\frac{2cf-2de}{d}\right)}{d} \right] - if^2 \left[\frac{4 \sin(4fx+4e)}{((fx+e)d+cf-de)d} + \frac{16 \text{Si}\left(4fx+4e+\frac{4cf-4de}{d}\right) \sin\left(\frac{4cf-4de}{d}\right)}{d} \right]$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^2,x)

[Out]
$$1/a^2/f*(-1/4*I*f^2*(-2*\text{sin}(2*f*x+2*e)/((f*x+e)*d+c*f-d*e)/d+2*(2*\text{Si}(2*f*x+2*e+2*(c*f-d*e)/d)*\text{sin}(2*(c*f-d*e)/d)/d+2*\text{Ci}(2*f*x+2*e+2*(c*f-d*e)/d)*\text{cos}(2*(c*f-d*e)/d)/d)-1/16*I*f^2*(-4*\text{sin}(4*f*x+4*e)/((f*x+e)*d+c*f-d*e)/d+4*(4*\text{Si}(4*f*x+4*e+4*(c*f-d*e)/d)*\text{sin}(4*(c*f-d*e)/d)/d+4*\text{Ci}(4*f*x+4*e+4*(c*f-d*e)/d)*\text{cos}(4*(c*f-d*e)/d)/d)+1/16*f^2*(-4*\text{cos}(4*f*x+4*e)/((f*x+e)*d+c*f-d*e)/d-4*(4*\text{Si}(4*f*x+4*e+4*(c*f-d*e)/d)*\text{cos}(4*(c*f-d*e)/d)/d-4*\text{Ci}(4*f*x+4*e+4*(c*f-d*e)/d)*\text{sin}(4*(c*f-d*e)/d)/d)+1/4*f^2*(-2*\text{cos}(2*f*x+2*e)/((f*x+e)$$

$\frac{d+cf-d^2e}{d} - 2 \frac{(2 \operatorname{Si}(2fx+2e+2(cf-d^2e)/d) \cos(2(cf-d^2e)/d) - 2 \operatorname{Ci}(2fx+2e+2(cf-d^2e)/d) \sin(2(cf-d^2e)/d))}{d} - \frac{1}{4} f^2 \frac{((fx+e)d+cf-d^2e)}{d}$

maxima [A] time = 1.08, size = 210, normalized size = 0.48

$$\frac{64 f^2 \cos\left(-\frac{4(de-cf)}{d}\right) E_2\left(\frac{4i(fx+e)d-4ide+4icf}{d}\right) + 128 f^2 \cos\left(-\frac{2(de-cf)}{d}\right) E_2\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) + 128i f^2 E_2\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right)}{256 \left((fx+e)a^2d^2 - a^2d^2e + a^2cd\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^2,x, algorithm="maxima")

[Out] $-\frac{1}{256} (64 f^2 \cos(-4(d^2e - cf)/d) \exp_integral_e(2, (4I(fx+e)d - 4I^2d^2e + 4I^2cf)/d) + 128 f^2 \cos(-2(d^2e - cf)/d) \exp_integral_e(2, (2I(fx+e)d - 2I^2d^2e + 2I^2cf)/d) + 128 I f^2 \exp_integral_e(2, (2I(fx+e)d - 2I^2d^2e + 2I^2cf)/d) \sin(-2(d^2e - cf)/d) + 64 I f^2 \exp_integral_e(2, (4I(fx+e)d - 4I^2d^2e + 4I^2cf)/d) \sin(-4(d^2e - cf)/d) + 64 f^2) / (((fx+e)a^2d^2 - a^2d^2e + a^2cd) f)$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + a \tan(e + fx) i)^2 (c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + a*tan(e + f*x)*1i)^2*(c + d*x)^2), x)

[Out] int(1/((a + a*tan(e + f*x)*1i)^2*(c + d*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{1}{c^2 \tan^2(e+fx) - 2ic^2 \tan(e+fx) - c^2 + 2cdx \tan^2(e+fx) - 4icdx \tan(e+fx) - 2cdx + d^2x^2 \tan^2(e+fx) - 2id^2x^2 \tan(e+fx) - d^2x^2} dx}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**2/(a+I*a*tan(f*x+e))**2,x)

[Out] $-\frac{\operatorname{Integral}\left(\frac{1}{(c^2 \tan^2(e + fx) - 2I^2c^2 \tan(e + fx) - c^2 + 2c^2d^2x \tan(e + fx) - 4I^2c^2d^2x \tan(e + fx) - 2c^2d^2x + d^2x^2 \tan^2(e + fx) - 2I^2d^2x^2 \tan(e + fx) - d^2x^2)}{a^2}\right), x)}{a^2}$

$$3.29 \quad \int \frac{(c+dx)^3}{(a+ia \tan(e+fx))^3} dx$$

Optimal. Leaf size=396

$$\frac{9id^2(c+dx)e^{-2ie-2ifx}}{32a^3f^3} - \frac{9id^2(c+dx)e^{-4ie-4ifx}}{256a^3f^3} - \frac{id^2(c+dx)e^{-6ie-6ifx}}{288a^3f^3} + \frac{9d(c+dx)^2e^{-2ie-2ifx}}{32a^3f^2} + \frac{9d(c+dx)^2e^{-4ie-4ifx}}{128a^3f^2}$$

[Out] $-9/64*d^3*exp(-2*I*e-2*I*f*x)/a^3/f^4-9/1024*d^3*exp(-4*I*e-4*I*f*x)/a^3/f^4-1/1728*d^3*exp(-6*I*e-6*I*f*x)/a^3/f^4-9/32*I*d^2*exp(-2*I*e-2*I*f*x)*(d*x+c)/a^3/f^3-9/256*I*d^2*exp(-4*I*e-4*I*f*x)*(d*x+c)/a^3/f^3-1/288*I*d^2*exp(-6*I*e-6*I*f*x)*(d*x+c)/a^3/f^3+9/32*d*exp(-2*I*e-2*I*f*x)*(d*x+c)^2/a^3/f^2+9/128*d*exp(-4*I*e-4*I*f*x)*(d*x+c)^2/a^3/f^2+1/96*d*exp(-6*I*e-6*I*f*x)*(d*x+c)^2/a^3/f^2+3/16*I*exp(-2*I*e-2*I*f*x)*(d*x+c)^3/a^3/f+3/32*I*exp(-4*I*e-4*I*f*x)*(d*x+c)^3/a^3/f+1/48*I*exp(-6*I*e-6*I*f*x)*(d*x+c)^3/a^3/f+1/32*(d*x+c)^4/a^3/d$

Rubi [A] time = 0.40, antiderivative size = 396, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {3729, 2176, 2194}

$$\frac{9id^2(c+dx)e^{-2ie-2ifx}}{32a^3f^3} - \frac{9id^2(c+dx)e^{-4ie-4ifx}}{256a^3f^3} - \frac{id^2(c+dx)e^{-6ie-6ifx}}{288a^3f^3} + \frac{9d(c+dx)^2e^{-2ie-2ifx}}{32a^3f^2} + \frac{9d(c+dx)^2e^{-4ie-4ifx}}{128a^3f^2}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + I*a*Tan[e + f*x])^3, x]

[Out] $(-9*d^3*E^{((-2*I)*e - (2*I)*f*x))/(64*a^3*f^4) - (9*d^3*E^{((-4*I)*e - (4*I)*f*x))/(1024*a^3*f^4) - (d^3*E^{((-6*I)*e - (6*I)*f*x))/(1728*a^3*f^4) - (((9*I)/32)*d^2*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)})/(a^3*f^3) - (((9*I)/256)*d^2*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)})/(a^3*f^3) - ((I/288)*d^2*E^{((-6*I)*e - (6*I)*f*x)*(c + d*x)})/(a^3*f^3) + (9*d*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)^2})/(32*a^3*f^2) + (9*d*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)^2})/(128*a^3*f^2) + (d*E^{((-6*I)*e - (6*I)*f*x)*(c + d*x)^2})/(96*a^3*f^2) + (((3*I)/16)*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)^3})/(a^3*f) + (((3*I)/32)*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)^3})/(a^3*f) + ((I/48)*E^{((-6*I)*e - (6*I)*f*x)*(c + d*x)^3})/(a^3*f) + (c + d*x)^4/(32*a^3*d)$

Rule 2176

Int[((b_.)*(F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] := Simp[((c + d*x)^m*(b*F^(g*(e + f*x)))^n)/(f*g*n*Log[F]), x] - Dist[(d*m)/(f*g*n*Log[F]), Int[(c + d*x)^(m-1)*(b*F^(g*(e + f*x)))^n, x], x] /; FreeQ[{F, b, c, d, e, f, g, n}, x] && GtQ[m, 0] && IntegerQ[2*m] && !UseGamma == True

Rule 2194

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 3729

Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + E^((2*a*(e + f*x))/b)/(2*a))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[a^2 + b^2, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^3}{(a+ia \tan(e+fx))^3} dx &= \int \left(\frac{(c+dx)^3}{8a^3} + \frac{3e^{-2ie-2ifx}(c+dx)^3}{8a^3} + \frac{3e^{-4ie-4ifx}(c+dx)^3}{8a^3} + \frac{e^{-6ie-6ifx}(c+dx)^3}{8a^3} \right) dx \\
&= \frac{(c+dx)^4}{32a^3d} + \frac{\int e^{-6ie-6ifx}(c+dx)^3 dx}{8a^3} + \frac{3 \int e^{-2ie-2ifx}(c+dx)^3 dx}{8a^3} + \frac{3 \int e^{-4ie-4ifx}(c+dx)^3 dx}{8a^3} \\
&= \frac{3ie^{-2ie-2ifx}(c+dx)^3}{16a^3f} + \frac{3ie^{-4ie-4ifx}(c+dx)^3}{32a^3f} + \frac{ie^{-6ie-6ifx}(c+dx)^3}{48a^3f} + \frac{(c+dx)^4}{32a^3d} - \frac{id}{32a^3} \\
&= \frac{9de^{-2ie-2ifx}(c+dx)^2}{32a^3f^2} + \frac{9de^{-4ie-4ifx}(c+dx)^2}{128a^3f^2} + \frac{de^{-6ie-6ifx}(c+dx)^2}{96a^3f^2} + \frac{3ie^{-2ie-2ifx}(c+dx)}{16a^3f} \\
&= -\frac{9id^2e^{-2ie-2ifx}(c+dx)}{32a^3f^3} - \frac{9id^2e^{-4ie-4ifx}(c+dx)}{256a^3f^3} - \frac{id^2e^{-6ie-6ifx}(c+dx)}{288a^3f^3} + \frac{9de^{-2ie-2ifx}(c+dx)}{32a^3} \\
&= -\frac{9d^3e^{-2ie-2ifx}}{64a^3f^4} - \frac{9d^3e^{-4ie-4ifx}}{1024a^3f^4} - \frac{d^3e^{-6ie-6ifx}}{1728a^3f^4} - \frac{9id^2e^{-2ie-2ifx}(c+dx)}{32a^3f^3} - \frac{9id^2e^{-4ie-4ifx}(c+dx)}{256a^3f^3}
\end{aligned}$$

Mathematica [A] time = 2.74, size = 667, normalized size = 1.68

$$i \sec^3(e+fx) \left(3456ic^3f^4x \sin(3(e+fx)) - 2592c^3f^3 \sin(e+fx) + 576c^3f^3 \sin(3(e+fx)) + 5184ic^2df^4x^2 \sin(3(e+fx)) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^3/(a + I*a*Tan[e + f*x])^3,x]

[Out] ((I/27648)*Sec[e + f*x]^3*(243*((32*I)*c^3*f^3 + 8*c^2*d*f^2*(5 + (12*I)*f*x) + 4*c*d^2*f*(-9*I + 20*f*x + (24*I)*f^2*x^2) + d^3*(-17 - (36*I)*f*x + 40*f^2*x^2 + (32*I)*f^3*x^3))*Cos[e + f*x] + 16*(36*c^3*f^3*(I + 6*f*x) + 18*c^2*d*f^2*(1 + (6*I)*f*x + 18*f^2*x^2) + 6*c*d^2*f*(-I + 6*f*x + (18*I)*f^2*x^2 + 36*f^3*x^3) + d^3*(-1 - (6*I)*f*x + 18*f^2*x^2 + (36*I)*f^3*x^3 + 54*f^4*x^4))*Cos[3*(e + f*x)] - (3645*I)*d^3*Sin[e + f*x] + 6804*c*d^2*f*Sin[e + f*x] + (5832*I)*c^2*d*f^2*Sin[e + f*x] - 2592*c^3*f^3*Sin[e + f*x] + 6804*d^3*f*x*Sin[e + f*x] + (11664*I)*c*d^2*f^2*x*Sin[e + f*x] - 7776*c^2*d*f^3*x*Sin[e + f*x] + (5832*I)*d^3*f^2*x^2*Sin[e + f*x] - 7776*c*d^2*f^3*x^2*Sin[e + f*x] - 2592*d^3*f^3*x^3*Sin[e + f*x] + (16*I)*d^3*Sin[3*(e + f*x)] - 96*c*d^2*f*Sin[3*(e + f*x)] - (288*I)*c^2*d*f^2*Sin[3*(e + f*x)] + 576*c^3*f^3*Sin[3*(e + f*x)] - 96*d^3*f*x*Sin[3*(e + f*x)] - (576*I)*c*d^2*f^2*x*Sin[3*(e + f*x)] + 1728*c^2*d*f^3*x*Sin[3*(e + f*x)] + (3456*I)*c^3*f^4*x*Sin[3*(e + f*x)] - (288*I)*d^3*f^2*x^2*Sin[3*(e + f*x)] + 1728*c*d^2*f^3*x^2*Sin[3*(e + f*x)] + (5184*I)*c^2*d*f^4*x^2*Sin[3*(e + f*x)] + 576*d^3*f^3*x^3*Sin[3*(e + f*x)] + (3456*I)*c*d^2*f^4*x^3*Sin[3*(e + f*x)] + (864*I)*d^3*f^4*x^4*Sin[3*(e + f*x)])))/(a^3*f^4*(-I + Tan[e + f*x])^3)

fricas [A] time = 0.61, size = 362, normalized size = 0.91

$$\frac{(576id^3f^3x^3 + 576ic^3f^3 + 288c^2df^2 - 96icd^2f - 16d^3 + (1728icd^2f^3 + 288d^3f^2)x^2 + (1728ic^2df^3 + 576cd^2f^2))}{(a^3f^4(-I + \tan(e+fx))^3)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e))^3,x, algorithm="fricas")

[Out] 1/27648*(576*I*d^3*f^3*x^3 + 576*I*c^3*f^3 + 288*c^2*d*f^2 - 96*I*c*d^2*f - 16*d^3 + (1728*I*c*d^2*f^3 + 288*d^3*f^2)*x^2 + (1728*I*c^2*d*f^3 + 576*c*d^2*f^2 - 96*I*d^3*f)*x + 864*(d^3*f^4*x^4 + 4*c*d^2*f^4*x^3 + 6*c^2*d*f^4*x^2 + 4*c^3*f^4*x)*e^(6*I*f*x + 6*I*e) + (5184*I*d^3*f^3*x^3 + 5184*I*c^3*f^3 + 7776*c^2*d*f^2 - 7776*I*c*d^2*f - 3888*d^3 + (15552*I*c*d^2*f^3 + 7776

```
*d^3*f^2)*x^2 + (15552*I*c^2*d*f^3 + 15552*c*d^2*f^2 - 7776*I*d^3*f)*x)*e^(
4*I*f*x + 4*I*e) + (2592*I*d^3*f^3*x^3 + 2592*I*c^3*f^3 + 1944*c^2*d*f^2 -
972*I*c*d^2*f - 243*d^3 + (7776*I*c*d^2*f^3 + 1944*d^3*f^2)*x^2 + (7776*I*c
^2*d*f^3 + 3888*c*d^2*f^2 - 972*I*d^3*f)*x)*e^(2*I*f*x + 2*I*e))*e^(-6*I*f*x
x - 6*I*e)/(a^3*f^4)
```

giac [A] time = 2.33, size = 573, normalized size = 1.45

$$\frac{(864d^3f^4x^4e^{(6ifx+6ie)} + 3456cd^2f^4x^3e^{(6ifx+6ie)} + 5184c^2df^4x^2e^{(6ifx+6ie)} + 5184id^3f^3x^3e^{(4ifx+4ie)} + 2592id^3f^3x^3e^{(2ifx+2ie)})}{a^3f^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e))^3,x, algorithm="giac")
```

```
[Out] 1/27648*(864*d^3*f^4*x^4*e^(6*I*f*x + 6*I*e) + 3456*c*d^2*f^4*x^3*e^(6*I*f*x
x + 6*I*e) + 5184*c^2*d*f^4*x^2*e^(6*I*f*x + 6*I*e) + 5184*I*d^3*f^3*x^3*e^(
(4*I*f*x + 4*I*e) + 2592*I*d^3*f^3*x^3*e^(2*I*f*x + 2*I*e) + 576*I*d^3*f^3*x
x^3 + 3456*c^3*f^4*x*e^(6*I*f*x + 6*I*e) + 15552*I*c*d^2*f^3*x^2*e^(4*I*f*x
+ 4*I*e) + 7776*I*c*d^2*f^3*x^2*e^(2*I*f*x + 2*I*e) + 1728*I*c*d^2*f^3*x^2
+ 15552*I*c^2*d*f^3*x*e^(4*I*f*x + 4*I*e) + 7776*d^3*f^2*x^2*e^(4*I*f*x +
4*I*e) + 7776*I*c^2*d*f^3*x*e^(2*I*f*x + 2*I*e) + 1944*d^3*f^2*x^2*e^(2*I*f
*x + 2*I*e) + 1728*I*c^2*d*f^3*x + 288*d^3*f^2*x^2 + 5184*I*c^3*f^3*e^(4*I*
f*x + 4*I*e) + 15552*c*d^2*f^2*x*e^(4*I*f*x + 4*I*e) + 2592*I*c^3*f^3*e^(2*
I*f*x + 2*I*e) + 3888*c*d^2*f^2*x*e^(2*I*f*x + 2*I*e) + 576*I*c^3*f^3 + 576
*c*d^2*f^2*x + 7776*c^2*d*f^2*e^(4*I*f*x + 4*I*e) - 7776*I*d^3*f*x*e^(4*I*f
*x + 4*I*e) + 1944*c^2*d*f^2*e^(2*I*f*x + 2*I*e) - 972*I*d^3*f*x*e^(2*I*f*x
+ 2*I*e) + 288*c^2*d*f^2 - 96*I*d^3*f*x - 7776*I*c*d^2*f*e^(4*I*f*x + 4*I*
e) - 972*I*c*d^2*f*e^(2*I*f*x + 2*I*e) - 96*I*c*d^2*f - 3888*d^3*e^(4*I*f*x
+ 4*I*e) - 243*d^3*e^(2*I*f*x + 2*I*e) - 16*d^3)*e^(-6*I*f*x - 6*I*e)/(a^3
*f^4)
```

maple [B] time = 0.93, size = 3404, normalized size = 8.60

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^3/(a+I*a*tan(f*x+e))^3,x)
```

```
[Out] 1/a^3/f*(2/3*I*c^3*cos(f*x+e)^6-3/4*I/f^2*c*d^2*e^2*cos(f*x+e)^4-2*I/f*c^2*
d*e*cos(f*x+e)^6+2*I/f^2*c*d^2*e^2*cos(f*x+e)^6+4/f^3*d^3*((f*x+e)^3*(1/6*(
cos(f*x+e)^5+5/4*cos(f*x+e)^3+15/8*cos(f*x+e))*sin(f*x+e)+5/16*f*x+5/16*e)+
1/12*(f*x+e)^2*cos(f*x+e)^6-1/6*(f*x+e)*(1/6*(cos(f*x+e)^5+5/4*cos(f*x+e)^3
+15/8*cos(f*x+e))*sin(f*x+e)+5/16*f*x+5/16*e)+245/768*(f*x+e)^2-1/216*cos(f
*x+e)^6-65/2304*cos(f*x+e)^4-65/768*cos(f*x+e)^2+5/32*(f*x+e)^2*cos(f*x+e)^
4-5/16*(f*x+e)*(1/4*(cos(f*x+e)^3+3/2*cos(f*x+e))*sin(f*x+e)+3/8*f*x+3/8*e)
+15/32*(f*x+e)^2*cos(f*x+e)^2-15/16*(f*x+e)*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*
f*x+1/2*e)+15/64*sin(f*x+e)^2-15/64*(f*x+e)^4)-3/f^3*d^3*((f*x+e)^3*(1/4*(c
os(f*x+e)^3+3/2*cos(f*x+e))*sin(f*x+e)+3/8*f*x+3/8*e)+3/16*(f*x+e)^2*cos(f*
x+e)^4-3/8*(f*x+e)*(1/4*(cos(f*x+e)^3+3/2*cos(f*x+e))*sin(f*x+e)+3/8*f*x+3/
8*e)+45/128*(f*x+e)^2-3/128*cos(f*x+e)^4-9/128*cos(f*x+e)^2+9/16*(f*x+e)^2*
cos(f*x+e)^2-9/8*(f*x+e)*(1/2*sin(f*x+e)*cos(f*x+e)+1/2*f*x+1/2*e)+9/32*sin
(f*x+e)^2-9/32*(f*x+e)^4)-1/4*I*c^3*cos(f*x+e)^4-3*c^3*(1/4*(cos(f*x+e)^3+3
/2*cos(f*x+e))*sin(f*x+e)+3/8*f*x+3/8*e)+4*c^3*(1/6*(cos(f*x+e)^5+5/4*cos(f
*x+e)^3+15/8*cos(f*x+e))*sin(f*x+e)+5/16*f*x+5/16*e)-9/f*c^2*d*((f*x+e)*(1/
4*(cos(f*x+e)^3+3/2*cos(f*x+e))*sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/
16*cos(f*x+e)^4+3/16*cos(f*x+e)^2)+9/f^3*d^3*e*((f*x+e)^2*(1/4*(cos(f*x+e)^
3+3/2*cos(f*x+e))*sin(f*x+e)+3/8*f*x+3/8*e)+1/8*(f*x+e)*cos(f*x+e)^4-1/32*(
cos(f*x+e)^3+3/2*cos(f*x+e))*sin(f*x+e)-15/64*f*x-15/64*e+3/8*(f*x+e)*cos(f
```

$$\begin{aligned}
& *x+e)^2-3/16*\sin(f*x+e)*\cos(f*x+e)-1/4*(f*x+e)^3-9/f^3*d^3*e^2*((f*x+e)*(1 \\
& /4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1 \\
& /16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)-9/f^2*c*d^2*((f*x+e)^2*(1/4*(\cos(f*x+e) \\
& ^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+1/8*(f*x+e)*\cos(f*x+e)^4-1/32* \\
& (\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)-15/64*f*x-15/64*e+3/8*(f*x+e)*\cos(\\
& f*x+e)^2-3/16*\sin(f*x+e)*\cos(f*x+e)-1/4*(f*x+e)^3)+3/f^3*d^3*e^3*(1/4*(\cos(\\
& f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+I/f^3*d^3*(-1/4*(f*x+e)^ \\
& 3*\cos(f*x+e)^4+3/4*(f*x+e)^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+ \\
& 3/8*f*x+3/8*e)+3/32*(f*x+e)*\cos(f*x+e)^4-3/128*(\cos(f*x+e)^3+3/2*\cos(f*x+e) \\
&)*\sin(f*x+e)-45/256*f*x-45/256*e+9/32*(f*x+e)*\cos(f*x+e)^2-9/64*\sin(f*x+e)* \\
& \cos(f*x+e)-3/16*(f*x+e)^3)-4*I/f^3*d^3*(-1/6*(f*x+e)^3*\cos(f*x+e)^6+1/2*(f* \\
& x+e)^2*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16 \\
& *f*x+5/16*e)+1/36*(f*x+e)*\cos(f*x+e)^6-1/216*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3 \\
& +15/8*\cos(f*x+e))*\sin(f*x+e)-245/2304*f*x-245/2304*e+5/96*(f*x+e)*\cos(f*x+e) \\
&)^4-5/384*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+5/32*(f*x+e)*\cos(f*x+e)^ \\
& 2-5/64*\sin(f*x+e)*\cos(f*x+e)-5/48*(f*x+e)^3)-4/f^3*d^3*e^3*(1/6*(\cos(f*x+e) \\
& ^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)+12/f^2*c*d \\
& ^2*((f*x+e)^2*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+ \\
& e)+5/16*f*x+5/16*e)+1/18*(f*x+e)*\cos(f*x+e)^6-1/108*(\cos(f*x+e)^5+5/4*\cos(f \\
& *x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)-245/1152*f*x-245/1152*e+5/48*(f*x+e)*co \\
& s(f*x+e)^4-5/192*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+5/16*(f*x+e)*\cos(\\
& f*x+e)^2-5/32*\sin(f*x+e)*\cos(f*x+e)-5/24*(f*x+e)^3)+12/f*c^2*d*((f*x+e)*(1/ \\
& 6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16* \\
& e)-5/32*(f*x+e)^2+1/36*\cos(f*x+e)^6+5/96*\cos(f*x+e)^4+5/32*\cos(f*x+e)^2)-12 \\
& /f^3*d^3*e*((f*x+e)^2*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))* \\
& \sin(f*x+e)+5/16*f*x+5/16*e)+1/18*(f*x+e)*\cos(f*x+e)^6-1/108*(\cos(f*x+e)^5+5 \\
& /4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)-245/1152*f*x-245/1152*e+5/48*(f \\
& *x+e)*\cos(f*x+e)^4-5/192*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+5/16*(f*x \\
& +e)*\cos(f*x+e)^2-5/32*\sin(f*x+e)*\cos(f*x+e)-5/24*(f*x+e)^3)+12/f^3*d^3*e^2* \\
& ((f*x+e)*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/ \\
& 16*f*x+5/16*e)-5/32*(f*x+e)^2+1/36*\cos(f*x+e)^6+5/96*\cos(f*x+e)^4+5/32*\cos(\\
& f*x+e)^2)+3*I/f^3*d^3*e^2*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2 \\
& *\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)+12*I/f^3*d^3*e*(-1/6*(f*x+e)^2*\cos \\
& (f*x+e)^6+1/3*(f*x+e)*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))* \\
& \sin(f*x+e)+5/16*f*x+5/16*e)-5/96*(f*x+e)^2+1/108*\cos(f*x+e)^6+5/288*\cos(f*x \\
& +e)^4+5/96*\cos(f*x+e)^2)-12*I/f^3*d^3*e^2*(-1/6*(f*x+e)*\cos(f*x+e)^6+1/36*(\\
& \cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/96*f*x+5/96*e)+ \\
& 3*I/f^2*c*d^2*(-1/4*(f*x+e)^2*\cos(f*x+e)^4+1/2*(f*x+e)*(1/4*(\cos(f*x+e)^3+3 \\
& /2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/32*(f*x+e)^2+1/32*\cos(f*x+e)^4+3 \\
& /32*\cos(f*x+e)^2)+3*I/f*c^2*d*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3 \\
& +3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)-12*I/f^2*c*d^2*(-1/6*(f*x+e)^2 \\
& *\cos(f*x+e)^6+1/3*(f*x+e)*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+ \\
& e))*\sin(f*x+e)+5/16*f*x+5/16*e)-5/96*(f*x+e)^2+1/108*\cos(f*x+e)^6+5/288*\cos \\
& (f*x+e)^4+5/96*\cos(f*x+e)^2)-12*I/f*c^2*d*(-1/6*(f*x+e)*\cos(f*x+e)^6+1/36*(\\
& \cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/96*f*x+5/96*e)+ \\
& 1/4*I/f^3*d^3*e^3*\cos(f*x+e)^4-2/3*I/f^3*d^3*e^3*\cos(f*x+e)^6+12/f^2*c*d^2* \\
& e^2*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f* \\
& x+5/16*e)-9/f^2*c*d^2*e^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8 \\
& *f*x+3/8*e)+9/f*c^2*d*e*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f \\
& *x+3/8*e)+18/f^2*c*d^2*e*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f* \\
& x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)-24/ \\
& f^2*c*d^2*e*((f*x+e)*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*s \\
& in(f*x+e)+5/16*f*x+5/16*e)-5/32*(f*x+e)^2+1/36*\cos(f*x+e)^6+5/96*\cos(f*x+e) \\
& ^4+5/32*\cos(f*x+e)^2)-12/f*c^2*d*e*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8 \\
& *\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)-3*I/f^3*d^3*e*(-1/4*(f*x+e)^2*\cos(\\
& f*x+e)^4+1/2*(f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+ \\
& 3/8*e)-3/32*(f*x+e)^2+1/32*\cos(f*x+e)^4+3/32*\cos(f*x+e)^2)-6*I/f^2*c*d^2*e* \\
& (-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/ \\
& 32*f*x+3/32*e)+3/4*I/f*c^2*d*e*\cos(f*x+e)^4+24*I/f^2*c*d^2*e*(-1/6*(f*x+e)*
\end{aligned}$$

$\cos(f*x+e)^6+1/36*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/96*f*x+5/96*e)$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+I*a*tan(f*x+e))^3,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 3.85, size = 411, normalized size = 1.04

$$e^{-e^{2i-fx}x^{2i}} \left(\frac{(12c^3f^3 - c^2df^218i - 18cd^2f + d^39i)1i}{64a^3f^4} + \frac{d^3x^33i}{16a^3f} - \frac{dx(-2c^2f^2 + cdf2i + d^2)9i}{32a^3f^3} - \frac{d^2x^2}{64a^3f^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + a*tan(e + f*x)*1i)^3,x)

[Out] $\exp(-e^{2i-fx}x^{2i}) * ((d^3*9i + 12*c^3*f^3 - c^2*d*f^2*18i - 18*c*d^2*f)*1i)/(64*a^3*f^4) + (d^3*x^3*3i)/(16*a^3*f) - (d*x*(d^2 - 2*c^2*f^2 + c*d*f*2i)*9i)/(32*a^3*f^3) - (d^2*x^2*(d*1i - 2*c*f)*9i)/(32*a^3*f^2) + \exp(-e^{4i-fx}x^{4i}) * ((d^3*9i + 96*c^3*f^3 - c^2*d*f^2*72i - 36*c*d^2*f)*1i)/(1024*a^3*f^4) + (d^3*x^3*3i)/(32*a^3*f) - (d*x*(d^2 - 8*c^2*f^2 + c*d*f*4i)*9i)/(256*a^3*f^3) - (d^2*x^2*(d*1i - 4*c*f)*9i)/(128*a^3*f^2) + \exp(-e^{6i-fx}x^{6i}) * ((d^3*1i + 36*c^3*f^3 - c^2*d*f^2*18i - 6*c*d^2*f)*1i)/(1728*a^3*f^4) + (d^3*x^3*1i)/(48*a^3*f) - (d*x*(d^2 - 18*c^2*f^2 + c*d*f*6i)*1i)/(288*a^3*f^3) - (d^2*x^2*(d*1i - 6*c*f)*1i)/(96*a^3*f^2) + (c^3*x)/(8*a^3) + (d^3*x^4)/(32*a^3) + (3*c^2*d*x^2)/(16*a^3) + (c*d^2*x^3)/(8*a^3)$

sympy [A] time = 0.92, size = 949, normalized size = 2.40

$$\frac{\left((-2359296ia^6c^3f^{11}e^{6ie} - 7077888ia^6c^2df^{11}xe^{6ie} - 1179648a^6c^2df^{10}e^{6ie} - 7077888ia^6cd^2f^{11}x^2e^{6ie} - 2359296a^6cd^2f^{10}xe^{6ie} + 393216ia^6cd^2f^9e^{6ie} - \dots \right)}{\frac{x^4(3d^3e^{4ie} + 3d^3e^{2ie} + d^3)e^{-6ie}}{32a^3} + \frac{x^3(3cd^2e^{4ie} + 3cd^2e^{2ie} + cd^2)e^{-6ie}}{8a^3} + \frac{x^2(9c^2de^{4ie} + 9c^2de^{2ie} + 3c^2d)e^{-6ie}}{16a^3} + \frac{x(3c^3e^{4ie} + 3c^3e^{2ie} + c^3)e^{-6ie}}{8a^3}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(a+I*a*tan(f*x+e))**3,x)

[Out] $\text{Piecewise}((-((-2359296*I*a**6*c**3*f**11*\exp(6*I*e) - 7077888*I*a**6*c**2*d*f**11*x*\exp(6*I*e) - 1179648*a**6*c**2*d*f**10*\exp(6*I*e) - 7077888*I*a**6*c*d**2*f**11*x**2*\exp(6*I*e) - 2359296*a**6*c*d**2*f**10*x*\exp(6*I*e) + 393216*I*a**6*c*d**2*f**9*\exp(6*I*e) - 2359296*I*a**6*d**3*f**11*x**3*\exp(6*I*e) - 1179648*a**6*d**3*f**10*x**2*\exp(6*I*e) + 393216*I*a**6*d**3*f**9*x*\exp(6*I*e) + 65536*a**6*d**3*f**8*\exp(6*I*e))*\exp(-6*I*f*x) + (-10616832*I*a**6*c**3*f**11*\exp(8*I*e) - 31850496*I*a**6*c**2*d*f**11*x*\exp(8*I*e) - 7962624*a**6*c**2*d*f**10*\exp(8*I*e) - 31850496*I*a**6*c*d**2*f**11*x**2*\exp(8*I*e) - 15925248*a**6*c*d**2*f**10*x*\exp(8*I*e) + 3981312*I*a**6*c*d**2*f**9*\exp(8*I*e) - 10616832*I*a**6*d**3*f**11*x**3*\exp(8*I*e) - 7962624*a**6*d**3*f**10*x**2*\exp(8*I*e) + 3981312*I*a**6*d**3*f**9*x*\exp(8*I*e) + 995328*a**6*d**3*f**8*\exp(8*I*e))*\exp(-4*I*f*x) + (-21233664*I*a**6*c**3*f**11*\exp(10*I*e) - 63700992*I*a**6*c**2*d*f**11*x*\exp(10*I*e) - 31850496*a**6*c**2*d*f**10*\exp(10*I*e) - 63700992*I*a**6*c*d**2*f**11*x**2*\exp(10*I*e) - 63700992*a**6*c*d**2*f**10*x*\exp(10*I*e) + 31850496*I*a**6*c*d**2*f**9*\exp(10*I*e) - 21233664*I*a**6*d**3*f**11*x**3*\exp(10*I*e) - 31850496*a**6*d**3*f**10*x**2*\exp(10*I*e) - 995328*a**6*d**3*f**8*\exp(10*I*e))*\exp(4*I*f*x)$

```

x**2*exp(10*I*e) + 31850496*I*a**6*d**3*f**9*x*exp(10*I*e) + 15925248*a**6*
d**3*f**8*exp(10*I*e))*exp(-2*I*f*x))*exp(-12*I*e)/(113246208*a**9*f**12),
Ne(113246208*a**9*f**12*exp(12*I*e), 0)), (x**4*(3*d**3*exp(4*I*e) + 3*d**3
*exp(2*I*e) + d**3)*exp(-6*I*e)/(32*a**3) + x**3*(3*c*d**2*exp(4*I*e) + 3*c
*d**2*exp(2*I*e) + c*d**2)*exp(-6*I*e)/(8*a**3) + x**2*(9*c**2*d*exp(4*I*e)
+ 9*c**2*d*exp(2*I*e) + 3*c**2*d)*exp(-6*I*e)/(16*a**3) + x*(3*c**3*exp(4*
I*e) + 3*c**3*exp(2*I*e) + c**3)*exp(-6*I*e)/(8*a**3), True)) + c**3*x/(8*a
**3) + 3*c**2*d*x**2/(16*a**3) + c*d**2*x**3/(8*a**3) + d**3*x**4/(32*a**3)

```

$$3.30 \quad \int \frac{(c+dx)^2}{(a+ia \tan(e+fx))^3} dx$$

Optimal. Leaf size=294

$$\frac{3d(c+dx)e^{-2ie-2ifx}}{16a^3f^2} + \frac{3d(c+dx)e^{-4ie-4ifx}}{64a^3f^2} + \frac{d(c+dx)e^{-6ie-6ifx}}{144a^3f^2} + \frac{3i(c+dx)^2e^{-2ie-2ifx}}{16a^3f} + \frac{3i(c+dx)^2e^{-4ie-4ifx}}{32a^3f} + \frac{i(c+dx)^2e^{-6ie-6ifx}}{48a^3f}$$

[Out] $-3/32*I*d^2*\exp(-2*I*e-2*I*f*x)/a^3/f^3-3/256*I*d^2*\exp(-4*I*e-4*I*f*x)/a^3/f^3-1/864*I*d^2*\exp(-6*I*e-6*I*f*x)/a^3/f^3+3/16*d*\exp(-2*I*e-2*I*f*x)*(d*x+c)/a^3/f^2+3/64*d*\exp(-4*I*e-4*I*f*x)*(d*x+c)/a^3/f^2+1/144*d*\exp(-6*I*e-6*I*f*x)*(d*x+c)/a^3/f^2+3/16*I*\exp(-2*I*e-2*I*f*x)*(d*x+c)^2/a^3/f+3/32*I*\exp(-4*I*e-4*I*f*x)*(d*x+c)^2/a^3/f+1/48*I*\exp(-6*I*e-6*I*f*x)*(d*x+c)^2/a^3/f+1/24*(d*x+c)^3/a^3/d$

Rubi [A] time = 0.27, antiderivative size = 294, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 3, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.130$, Rules used = {3729, 2176, 2194}

$$\frac{3d(c+dx)e^{-2ie-2ifx}}{16a^3f^2} + \frac{3d(c+dx)e^{-4ie-4ifx}}{64a^3f^2} + \frac{d(c+dx)e^{-6ie-6ifx}}{144a^3f^2} + \frac{3i(c+dx)^2e^{-2ie-2ifx}}{16a^3f} + \frac{3i(c+dx)^2e^{-4ie-4ifx}}{32a^3f} + \frac{i(c+dx)^2e^{-6ie-6ifx}}{48a^3f}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + I*a*Tan[e + f*x])^3, x]

[Out] $(((-3*I)/32)*d^2*E^{((-2*I)*e - (2*I)*f*x))/(a^3*f^3) - ((3*I)/256)*d^2*E^{((-4*I)*e - (4*I)*f*x))/(a^3*f^3) - ((I/864)*d^2*E^{((-6*I)*e - (6*I)*f*x))/(a^3*f^3) + (3*d*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)})/(16*a^3*f^2) + (3*d*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)})/(64*a^3*f^2) + (d*E^{((-6*I)*e - (6*I)*f*x)*(c + d*x)})/(144*a^3*f^2) + (((3*I)/16)*E^{((-2*I)*e - (2*I)*f*x)*(c + d*x)^2})/(a^3*f) + (((3*I)/32)*E^{((-4*I)*e - (4*I)*f*x)*(c + d*x)^2})/(a^3*f) + ((I/48)*E^{((-6*I)*e - (6*I)*f*x)*(c + d*x)^2})/(a^3*f) + (c + d*x)^3/(24*a^3*d)$

Rule 2176

Int[((b_.)*(F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] := Simp[((c + d*x)^m*(b*F^(g*(e + f*x)))^n)/(f*g*n*Log[F]), x] - Dist[(d*m)/(f*g*n*Log[F]), Int[(c + d*x)^(m-1)*(b*F^(g*(e + f*x)))^n, x], x] /; FreeQ[{F, b, c, d, e, f, g, n}, x] && GtQ[m, 0] && IntegerQ[2*m] && !UseGamma == True

Rule 2194

Int[(F_)^((c_.)*((a_.) + (b_.)*(x_)))^(n_.), x_Symbol] := Simp[(F^(c*(a + b*x)))^n/(b*c*n*Log[F]), x] /; FreeQ[{F, a, b, c, n}, x]

Rule 3729

Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + E^((2*a*(e + f*x))/b)/(2*a))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[a^2 + b^2, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned}
\int \frac{(c+dx)^2}{(a+ia \tan(e+fx))^3} dx &= \int \left(\frac{(c+dx)^2}{8a^3} + \frac{3e^{-2ie-2ifx}(c+dx)^2}{8a^3} + \frac{3e^{-4ie-4ifx}(c+dx)^2}{8a^3} + \frac{e^{-6ie-6ifx}(c+dx)^2}{8a^3} \right) dx \\
&= \frac{(c+dx)^3}{24a^3d} + \frac{\int e^{-6ie-6ifx}(c+dx)^2 dx}{8a^3} + \frac{3 \int e^{-2ie-2ifx}(c+dx)^2 dx}{8a^3} + \frac{3 \int e^{-4ie-4ifx}(c+dx)^2 dx}{8a^3} \\
&= \frac{3ie^{-2ie-2ifx}(c+dx)^2}{16a^3f} + \frac{3ie^{-4ie-4ifx}(c+dx)^2}{32a^3f} + \frac{ie^{-6ie-6ifx}(c+dx)^2}{48a^3f} + \frac{(c+dx)^3}{24a^3d} - \frac{id}{24a^3d} \\
&= \frac{3de^{-2ie-2ifx}(c+dx)}{16a^3f^2} + \frac{3de^{-4ie-4ifx}(c+dx)}{64a^3f^2} + \frac{de^{-6ie-6ifx}(c+dx)}{144a^3f^2} + \frac{3ie^{-2ie-2ifx}(c+dx)}{16a^3f} \\
&= -\frac{3id^2e^{-2ie-2ifx}}{32a^3f^3} - \frac{3id^2e^{-4ie-4ifx}}{256a^3f^3} - \frac{id^2e^{-6ie-6ifx}}{864a^3f^3} + \frac{3de^{-2ie-2ifx}(c+dx)}{16a^3f^2} + \frac{3de^{-4ie-4ifx}(c+dx)}{64a^3f^2}
\end{aligned}$$

Mathematica [A] time = 1.81, size = 405, normalized size = 1.38

$$i \sec^3(e+fx) \left(81 (24ic^2f^2 + 4cdf(5 + 12ifx) + d^2(24if^2x^2 + 20fx - 9i)) \cos(e+fx) + 8(18c^2f^2(6fx+i) + 6c^2f^2) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + I*a*Tan[e + f*x])^3,x]

[Out] ((I/6912)*Sec[e + f*x]^3*(81*((24*I)*c^2*f^2 + 4*c*d*f*(5 + (12*I)*f*x) + d^2*(-9*I + 20*f*x + (24*I)*f^2*x^2))*Cos[e + f*x] + 8*(18*c^2*f^2*(I + 6*f*x) + 6*c*d*f*(1 + (6*I)*f*x + 18*f^2*x^2) + d^2*(-I + 6*f*x + (18*I)*f^2*x^2 + 36*f^3*x^3))*Cos[3*(e + f*x)] + 567*d^2*Sin[e + f*x] + (972*I)*c*d*f*Sin[e + f*x] - 648*c^2*f^2*Sin[e + f*x] + (972*I)*d^2*f*x*Sin[e + f*x] - 1296*c*d*f^2*x*Sin[e + f*x] - 648*d^2*f^2*x^2*Sin[e + f*x] - 8*d^2*Sin[3*(e + f*x)] - (48*I)*c*d*f*Sin[3*(e + f*x)] + 144*c^2*f^2*Sin[3*(e + f*x)] - (48*I)*d^2*f*x*Sin[3*(e + f*x)] + 288*c*d*f^2*x*Sin[3*(e + f*x)] + (864*I)*c^2*f^3*x*Sin[3*(e + f*x)] + 144*d^2*f^2*x^2*Sin[3*(e + f*x)] + (864*I)*c*d*f^3*x^2*Sin[3*(e + f*x)] + (288*I)*d^2*f^3*x^3*Sin[3*(e + f*x)]))/(a^3*f^3*(-I + Tan[e + f*x])^3)

fricas [A] time = 0.52, size = 216, normalized size = 0.73

$$\left(144i d^2 f^2 x^2 + 144i c^2 f^2 + 48 cdf - 8i d^2 + (288i cdf^2 + 48 d^2 f)x + 288 (d^2 f^3 x^3 + 3 cdf^3 x^2 + 3 c^2 f^3 x) e^{(6ifx+6ie)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e))^3,x, algorithm="fricas")

[Out] 1/6912*(144*I*d^2*f^2*x^2 + 144*I*c^2*f^2 + 48*c*d*f - 8*I*d^2 + (288*I*c*d*f^2 + 48*d^2*f)*x + 288*(d^2*f^3*x^3 + 3*c*d*f^3*x^2 + 3*c^2*f^3*x)*e^(6*I*f*x + 6*I*e) + (1296*I*d^2*f^2*x^2 + 1296*I*c^2*f^2 + 1296*c*d*f - 648*I*d^2 + (2592*I*c*d*f^2 + 1296*d^2*f)*x)*e^(4*I*f*x + 4*I*e) + (648*I*d^2*f^2*x^2 + 648*I*c^2*f^2 + 324*c*d*f - 81*I*d^2 + (1296*I*c*d*f^2 + 324*d^2*f)*x)*e^(2*I*f*x + 2*I*e))*e^(-6*I*f*x - 6*I*e)/(a^3*f^3)

giac [A] time = 2.56, size = 331, normalized size = 1.13

$$\left(288 d^2 f^3 x^3 e^{(6ifx+6ie)} + 864 cdf^3 x^2 e^{(6ifx+6ie)} + 864 c^2 f^3 x e^{(6ifx+6ie)} + 1296i d^2 f^2 x^2 e^{(4ifx+4ie)} + 648i d^2 f^2 x^2 e^{(2ifx+2ie)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e))^3,x, algorithm="giac")

[Out] $1/6912*(288*d^2*f^3*x^3*e^{(6*I*f*x + 6*I*e)} + 864*c*d*f^3*x^2*e^{(6*I*f*x + 6*I*e)} + 864*c^2*f^3*x*e^{(6*I*f*x + 6*I*e)} + 1296*I*d^2*f^2*x^2*e^{(4*I*f*x + 4*I*e)} + 648*I*d^2*f^2*x^2*e^{(2*I*f*x + 2*I*e)} + 144*I*d^2*f^2*x^2 + 2592*I*c*d*f^2*x*e^{(4*I*f*x + 4*I*e)} + 1296*I*c*d*f^2*x*e^{(2*I*f*x + 2*I*e)} + 288*I*c*d*f^2*x + 1296*I*c^2*f^2*e^{(4*I*f*x + 4*I*e)} + 1296*d^2*f*x*e^{(4*I*f*x + 4*I*e)} + 648*I*c^2*f^2*e^{(2*I*f*x + 2*I*e)} + 324*d^2*f*x*e^{(2*I*f*x + 2*I*e)} + 144*I*c^2*f^2 + 48*d^2*f*x + 1296*c*d*f*e^{(4*I*f*x + 4*I*e)} + 324*c*d*f*e^{(2*I*f*x + 2*I*e)} + 48*c*d*f - 648*I*d^2*e^{(4*I*f*x + 4*I*e)} - 81*I*d^2*e^{(2*I*f*x + 2*I*e)} - 8*I*d^2)*e^{(-6*I*f*x - 6*I*e)}/(a^3*f^3)$

maple [B] time = 0.89, size = 1525, normalized size = 5.19

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(a+I*a*tan(f*x+e))^3,x)

[Out] $1/a^3/f*(8*I/f^2*d^2*e^{(-1/6*(f*x+e)*\cos(f*x+e)^6+1/36*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/96*f*x+5/96*e)+2/3*I*c^2*\cos(f*x+e)^6-1/4*I*c^2*\cos(f*x+e)^4-2*I/f^2*d^2*e^{(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)-8*I/f*c*d*(-1/6*(f*x+e)*\cos(f*x+e)^6+1/36*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/96*f*x+5/96*e)+1/2*I/f*c*d*e*\cos(f*x+e)^4+4/f^2*d^2*((f*x+e)^2*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)+1/18*(f*x+e)*\cos(f*x+e)^6-1/108*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)-245/1152*f*x-245/1152*e+5/48*(f*x+e)*\cos(f*x+e)^4-5/192*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+5/16*(f*x+e)*\cos(f*x+e)^2-5/32*\sin(f*x+e)*\cos(f*x+e)-5/24*(f*x+e)^3)+8/f*c*d*((f*x+e)*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)-5/32*(f*x+e)^2+1/36*\cos(f*x+e)^6+5/96*\cos(f*x+e)^4+5/32*\cos(f*x+e)^2)-8/f^2*d^2*e^{((f*x+e)^2)-1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)-5/32*(f*x+e)^2+1/36*\cos(f*x+e)^6+5/96*\cos(f*x+e)^4+5/32*\cos(f*x+e)^2)+4*c^2*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)-8/f*c*d*e*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)+4/f^2*d^2*e^2*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)+2/3*I/f^2*d^2*e^2*\cos(f*x+e)^6+2*I/f*c*d*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)-1/4*I/f^2*d^2*e^2*\cos(f*x+e)^4-4*I/f^2*d^2*(-1/6*(f*x+e)^2*\cos(f*x+e)^6+1/3*(f*x+e)*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)-5/96*(f*x+e)^2+1/108*\cos(f*x+e)^6+5/288*\cos(f*x+e)^4+5/96*\cos(f*x+e)^2)+I/f^2*d^2*(-1/4*(f*x+e)^2*\cos(f*x+e)^4+1/2*(f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/32*(f*x+e)^2+1/32*\cos(f*x+e)^4+3/32*\cos(f*x+e)^2)-4/3*I/f*c*d*e*\cos(f*x+e)^6-3/f^2*d^2*((f*x+e)^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+1/8*(f*x+e)*\cos(f*x+e)^4-1/32*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)-15/64*f*x-15/64*e+3/8*(f*x+e)*\cos(f*x+e)^2-3/16*\sin(f*x+e)*\cos(f*x+e)-1/4*(f*x+e)^3)-6/f*c*d*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)+6/f^2*d^2*e^{((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)-3*c^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+6/f*c*d*e*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/f^2*d^2*e^2*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e))$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+I*a*tan(f*x+e))^3,x, algorithm="maxima")

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima:
expt: undefined: 0 to a negative exponent.

mupad [B] time = 3.37, size = 263, normalized size = 0.89

$$\frac{c^2 x}{8 a^3} e^{-e 2 i-f x 2 i} \left(\frac{(-6 c^2 f^2 + c d f 6 i + 3 d^2) 1 i}{32 a^3 f^3} - \frac{d^2 x^2 3 i}{16 a^3 f} + \frac{d x (-2 c f + d 1 i) 3 i}{16 a^3 f^2} \right) e^{-e 4 i-f x 4 i} \left(\frac{(-24 c^2 f^2 + c d f 6 i + 3 d^2) 1 i}{256 a^3 f^3} - \frac{d^2 x^2 3 i}{16 a^3 f} + \frac{d x (-2 c f + d 1 i) 3 i}{16 a^3 f^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + a*tan(e + f*x)*1i)^3,x)

[Out] (c^2*x)/(8*a^3) - exp(- e*2i - f*x*2i)*(((3*d^2 - 6*c^2*f^2 + c*d*f*6i)*1i)/(32*a^3*f^3) - (d^2*x^2*3i)/(16*a^3*f) + (d*x*(d*1i - 2*c*f)*3i)/(16*a^3*f^2)) - exp(- e*4i - f*x*4i)*(((3*d^2 - 24*c^2*f^2 + c*d*f*12i)*1i)/(256*a^3*f^3) - (d^2*x^2*3i)/(32*a^3*f) + (d*x*(d*1i - 4*c*f)*3i)/(64*a^3*f^2)) - exp(- e*6i - f*x*6i)*(((d^2 - 18*c^2*f^2 + c*d*f*6i)*1i)/(864*a^3*f^3) - (d^2*x^2*1i)/(48*a^3*f) + (d*x*(d*1i - 6*c*f)*1i)/(144*a^3*f^2)) + (d^2*x^3)/(24*a^3) + (c*d*x^2)/(8*a^3)

sympy [A] time = 0.70, size = 592, normalized size = 2.01

$$\left\{ \begin{array}{l} \frac{((-147456 i a^6 c^2 f^8 e^{6 i e}-294912 i a^6 c d f^8 x e^{6 i e}-49152 a^6 c d f^7 e^{6 i e}-147456 i a^6 d^2 f^8 x^2 e^{6 i e}-49152 a^6 d^2 f^7 x e^{6 i e}+8192 i a^6 d^2 f^6 e^{6 i e}) e^{-6 i f x}+(-663552 i a^6 c^2 f^8 e^{-6 i e}+3 d^2 e^{4 i e}+3 d^2 e^{2 i e}+d^2) e^{-6 i e}}{24 a^3} + \frac{x^2(3 c d e^{4 i e}+3 c d e^{2 i e}+c d) e^{-6 i e}}{8 a^3} + \frac{x(3 c^2 e^{4 i e}+3 c^2 e^{2 i e}+c^2) e^{-6 i e}}{8 a^3} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(a+I*a*tan(f*x+e))**3,x)

[Out] Piecewise((((-147456*I*a**6*c**2*f**8*exp(6*I*e) - 294912*I*a**6*c*d*f**8*x*exp(6*I*e) - 49152*a**6*c*d*f**7*exp(6*I*e) - 147456*I*a**6*d**2*f**8*x**2*exp(6*I*e) - 49152*a**6*d**2*f**7*x*exp(6*I*e) + 8192*I*a**6*d**2*f**6*exp(6*I*e))*exp(-6*I*f*x) + (-663552*I*a**6*c**2*f**8*exp(8*I*e) - 1327104*I*a**6*c*d*f**8*x*exp(8*I*e) - 331776*a**6*c*d*f**7*exp(8*I*e) - 663552*I*a**6*d**2*f**8*x**2*exp(8*I*e) - 331776*a**6*d**2*f**7*x*exp(8*I*e) + 82944*I*a**6*d**2*f**6*exp(8*I*e))*exp(-4*I*f*x) + (-1327104*I*a**6*c**2*f**8*exp(10*I*e) - 2654208*I*a**6*c*d*f**8*x*exp(10*I*e) - 1327104*a**6*c*d*f**7*exp(10*I*e) - 1327104*I*a**6*d**2*f**8*x**2*exp(10*I*e) - 1327104*a**6*d**2*f**7*x*exp(10*I*e) + 663552*I*a**6*d**2*f**6*exp(10*I*e))*exp(-2*I*f*x)), Ne(7077888*a**9*f**9*exp(12*I*e), 0)), (x**3*(3*d**2*exp(4*I*e) + 3*d**2*exp(2*I*e) + d**2)*exp(-6*I*e)/(24*a**3) + x**2*(3*c*d*exp(4*I*e) + 3*c*d*exp(2*I*e) + c*d)*exp(-6*I*e)/(8*a**3) + x*(3*c**2*exp(4*I*e) + 3*c**2*exp(2*I*e) + c**2)*exp(-6*I*e)/(8*a**3), True)) + c**2*x/(8*a**3) + c*d*x**2/(8*a**3) + d**2*x**3/(24*a**3)

$$3.31 \quad \int \frac{c+dx}{(a+ia \tan(e+fx))^3} dx$$

Optimal. Leaf size=209

$$\frac{i(c+dx)}{8f(a^3+ia^3 \tan(e+fx))} + \frac{x(c+dx)}{8a^3} + \frac{11d}{96f^2(a^3+ia^3 \tan(e+fx))} - \frac{11idx}{96a^3f} - \frac{dx^2}{16a^3} + \frac{i(c+dx)}{8af(a+ia \tan(e+fx))^2} + \dots$$

[Out] $-11/96*I*d*x/a^3/f-1/16*d*x^2/a^3+1/8*x*(d*x+c)/a^3+1/36*d/f^2/(a+I*a*\tan(f*x+e))^3+1/6*I*(d*x+c)/f/(a+I*a*\tan(f*x+e))^3+5/96*d/a/f^2/(a+I*a*\tan(f*x+e))^2+1/8*I*(d*x+c)/a/f/(a+I*a*\tan(f*x+e))^2+11/96*d/f^2/(a^3+I*a^3*\tan(f*x+e))+1/8*I*(d*x+c)/f/(a^3+I*a^3*\tan(f*x+e))$

Rubi [A] time = 0.26, antiderivative size = 209, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 3, integrand size = 21, $\frac{\text{number of rules}}{\text{integrand size}} = 0.143$, Rules used = {3479, 8, 3730}

$$\frac{i(c+dx)}{8f(a^3+ia^3 \tan(e+fx))} + \frac{x(c+dx)}{8a^3} + \frac{11d}{96f^2(a^3+ia^3 \tan(e+fx))} - \frac{11idx}{96a^3f} - \frac{dx^2}{16a^3} + \frac{i(c+dx)}{8af(a+ia \tan(e+fx))^2} + \dots$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + I*a*Tan[e + f*x])^3, x]

[Out] $(((-11*I)/96)*d*x)/(a^3*f) - (d*x^2)/(16*a^3) + (x*(c + d*x))/(8*a^3) + d/(36*f^2*(a + I*a*Tan[e + f*x])^3) + ((I/6)*(c + d*x))/(f*(a + I*a*Tan[e + f*x])^3) + (5*d)/(96*a*f^2*(a + I*a*Tan[e + f*x])^2) + ((I/8)*(c + d*x))/(a*f*(a + I*a*Tan[e + f*x])^2) + (11*d)/(96*f^2*(a^3 + I*a^3*Tan[e + f*x])) + ((I/8)*(c + d*x))/(f*(a^3 + I*a^3*Tan[e + f*x]))$

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 3479

Int[((a_) + (b_.)*tan[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := Simp[(a*(a + b*Tan[c + d*x])^n)/(2*b*d*n), x] + Dist[1/(2*a), Int[(a + b*Tan[c + d*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d}, x] && EqQ[a^2 + b^2, 0] && LtQ[n, 0]

Rule 3730

Int[((c_.) + (d_.)*(x_))^(m_.)*((a_) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] := With[{u = IntHide[(a + b*Tan[e + f*x])^n, x]}, Dist[(c + d*x)^m, u, x] - Dist[d*m, Int[Dist[(c + d*x)^(m - 1), u, x], x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && ILtQ[n, -1] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
\int \frac{c+dx}{(a+ia \tan(e+fx))^3} dx &= \frac{x(c+dx)}{8a^3} + \frac{i(c+dx)}{6f(a+ia \tan(e+fx))^3} + \frac{i(c+dx)}{8af(a+ia \tan(e+fx))^2} + \frac{i(c+dx)}{8f(a^3+ia^3 \tan(e+fx))} \\
&= -\frac{dx^2}{16a^3} + \frac{x(c+dx)}{8a^3} + \frac{i(c+dx)}{6f(a+ia \tan(e+fx))^3} + \frac{i(c+dx)}{8af(a+ia \tan(e+fx))^2} + \frac{i(c+dx)}{8f(a^3+ia^3 \tan(e+fx))} \\
&= -\frac{dx^2}{16a^3} + \frac{x(c+dx)}{8a^3} + \frac{d}{36f^2(a+ia \tan(e+fx))^3} + \frac{i(c+dx)}{6f(a+ia \tan(e+fx))^3} + \frac{i(c+dx)}{32af^2} \\
&= -\frac{idx}{16a^3f} - \frac{dx^2}{16a^3} + \frac{x(c+dx)}{8a^3} + \frac{d}{36f^2(a+ia \tan(e+fx))^3} + \frac{i(c+dx)}{6f(a+ia \tan(e+fx))^3} \\
&= -\frac{3idx}{32a^3f} - \frac{dx^2}{16a^3} + \frac{x(c+dx)}{8a^3} + \frac{d}{36f^2(a+ia \tan(e+fx))^3} + \frac{i(c+dx)}{6f(a+ia \tan(e+fx))^3} \\
&= -\frac{11idx}{96a^3f} - \frac{dx^2}{16a^3} + \frac{x(c+dx)}{8a^3} + \frac{d}{36f^2(a+ia \tan(e+fx))^3} + \frac{i(c+dx)}{6f(a+ia \tan(e+fx))^3}
\end{aligned}$$

Mathematica [A] time = 0.91, size = 205, normalized size = 0.98

$$i \sec^3(e+fx) \left(4(6cf(6fx+i) + d(18f^2x^2 + 6ifx + 1)) \cos(3(e+fx)) + 27(12icf + d(5 + 12ifx)) \cos(e+fx) + \dots \right)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + I*a*Tan[e + f*x])^3, x]

[Out] ((I/1152)*Sec[e + f*x]^3*(27*((12*I)*c*f + d*(5 + (12*I)*f*x))*Cos[e + f*x] + 4*(6*c*f*(I + 6*f*x) + d*(1 + (6*I)*f*x + 18*f^2*x^2))*Cos[3*(e + f*x)] + (81*I)*d*Sin[e + f*x] - 108*c*f*Sin[e + f*x] - 108*d*f*x*Sin[e + f*x] - (4*I)*d*Sin[3*(e + f*x)] + 24*c*f*Sin[3*(e + f*x)] + 24*d*f*x*Sin[3*(e + f*x)]) + (144*I)*c*f^2*x*Sin[3*(e + f*x)] + (72*I)*d*f^2*x^2*Sin[3*(e + f*x)])/(a^3*f^2*(-I + Tan[e + f*x])^3)

fricas [A] time = 0.70, size = 103, normalized size = 0.49

$$\frac{(24i d f x + 24i c f + 72(d f^2 x^2 + 2 c f^2 x) e^{(6i f x + 6i e)} + (216i d f x + 216i c f + 108 d) e^{(4i f x + 4i e)} + (108i d f x + 108i c f + 27 d) e^{(2i f x + 2i e)} + 4 d) e^{(-6i f x - 6i e)}}{1152 a^3 f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e))^3,x, algorithm="fricas")

[Out] 1/1152*(24*I*d*f*x + 24*I*c*f + 72*(d*f^2*x^2 + 2*c*f^2*x))*e^(6*I*f*x + 6*I*e) + (216*I*d*f*x + 216*I*c*f + 108*d)*e^(4*I*f*x + 4*I*e) + (108*I*d*f*x + 108*I*c*f + 27*d)*e^(2*I*f*x + 2*I*e) + 4*d)*e^(-6*I*f*x - 6*I*e)/(a^3*f^2)

giac [A] time = 2.13, size = 151, normalized size = 0.72

$$\frac{(72 d f^2 x^2 e^{(6i f x + 6i e)} + 144 c f^2 x e^{(6i f x + 6i e)} + 216i d f x e^{(4i f x + 4i e)} + 108i d f x e^{(2i f x + 2i e)} + 24i d f x + 216i c f e^{(4i f x + 4i e)} + 27 d) e^{(-6i f x - 6i e)}}{1152 a^3 f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e))^3,x, algorithm="giac")

[Out] $1/1152*(72*d*f^2*x^2*e^{(6*I*f*x + 6*I*e)} + 144*c*f^2*x*e^{(6*I*f*x + 6*I*e)} + 216*I*d*f*x*e^{(4*I*f*x + 4*I*e)} + 108*I*d*f*x*e^{(2*I*f*x + 2*I*e)} + 24*I*d*f*x + 216*I*c*f*e^{(4*I*f*x + 4*I*e)} + 108*I*c*f*e^{(2*I*f*x + 2*I*e)} + 24*I*c*f + 108*d*e^{(4*I*f*x + 4*I*e)} + 27*d*e^{(2*I*f*x + 2*I*e)} + 4*d)*e^{(-6*I*f*x - 6*I*e)}/(a^3*f^2)$

maple [B] time = 0.85, size = 527, normalized size = 2.52

$$\frac{4id \left(-\frac{(fx+e)(\cos^6(fx+e))}{6} + \frac{\left(\cos^5(fx+e) + \frac{5(\cos^3(fx+e))}{4} + \frac{15\cos(fx+e)}{8} \right) \sin(fx+e)}{36} + \frac{5fx}{96} + \frac{5e}{96} \right)}{f} + \frac{2ic(\cos^6(fx+e))}{3} - \frac{2ide(\cos^6(fx+e))}{3f} + \frac{4d}{3} \left(\frac{fx+e}{3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)/(a+I*a*tan(f*x+e))^3,x)`

[Out] $1/a^3/f*(-4*I/f*d*(-1/6*(f*x+e)*\cos(f*x+e)^6+1/36*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/96*f*x+5/96*e)+2/3*I*c*\cos(f*x+e)^6-2/3*I/f*d*e*\cos(f*x+e)^6+4/f*d*((f*x+e)*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)-5/32*(f*x+e)^2+1/36*\cos(f*x+e)^6+5/96*\cos(f*x+e)^4+5/32*\cos(f*x+e)^2)+4*c*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)-4/f*d*e*(1/6*(\cos(f*x+e)^5+5/4*\cos(f*x+e)^3+15/8*\cos(f*x+e))*\sin(f*x+e)+5/16*f*x+5/16*e)+I/f*d*(-1/4*(f*x+e)*\cos(f*x+e)^4+1/16*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/32*f*x+3/32*e)-1/4*I*c*\cos(f*x+e)^4+1/4*I/f*d*e*\cos(f*x+e)^4-3/f*d*((f*x+e)*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)-3/16*(f*x+e)^2+1/16*\cos(f*x+e)^4+3/16*\cos(f*x+e)^2)-3*c*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e)+3/f*d*e*(1/4*(\cos(f*x+e)^3+3/2*\cos(f*x+e))*\sin(f*x+e)+3/8*f*x+3/8*e))$

maxima [F(-2)] time = 0.00, size = 0, normalized size = 0.00

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)/(a+I*a*tan(f*x+e))^3,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError >> ECL says: Error executing code in Maxima: expt: undefined: 0 to a negative exponent.

mupad [B] time = 3.03, size = 146, normalized size = 0.70

$$\frac{dx^2}{16a^3} e^{-e4i-fx4i} \left(\frac{(-12cf+d3i)1i}{128a^3f^2} - \frac{dx3i}{32a^3f} \right) e^{-e6i-fx6i} \left(\frac{(-6cf+d1i)1i}{288a^3f^2} - \frac{dx1i}{48a^3f} \right) e^{-e2i-fx2i} \left(\frac{-6c}{3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)/(a + a*tan(e + f*x)*1i)^3,x)`

[Out] $(d*x^2)/(16*a^3) - \exp(-e*4i - f*x*4i)*(((d*3i - 12*c*f)*1i)/(128*a^3*f^2) - (d*x*3i)/(32*a^3*f)) - \exp(-e*6i - f*x*6i)*(((d*1i - 6*c*f)*1i)/(288*a^3*f^2) - (d*x*1i)/(48*a^3*f)) - \exp(-e*2i - f*x*2i)*(((d*3i - 6*c*f)*1i)/(32*a^3*f^2) - (d*x*3i)/(16*a^3*f)) + (c*x)/(8*a^3)$

sympy [A] time = 0.52, size = 320, normalized size = 1.53

$$\left\{ \frac{((-24576ia^6cf^5e^{6ie}-24576ia^6df^5xe^{6ie}-4096a^6df^4e^{6ie})e^{-6ifx}+(-110592ia^6cf^5e^{8ie}-110592ia^6df^5xe^{8ie}-27648a^6df^4e^{8ie})e^{-4ifx}+(-221184ia^6cf^5e^{10ie}-221184ia^6df^5xe^{10ie}-110592a^6df^4e^{10ie})e^{-2ifx}}{1179648a^9f^6} \right. \\ \left. + \frac{x^2(3de^{4ie}+3de^{2ie}+d)e^{-6ie}}{16a^3} + \frac{x(3ce^{4ie}+3ce^{2ie}+c)e^{-6ie}}{8a^3} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+I*a*tan(f*x+e))**3,x)

[Out] Piecewise((-((-24576*I*a**6*c*f**5*exp(6*I*e) - 24576*I*a**6*d*f**5*x*exp(6*I*e) - 4096*a**6*d*f**4*exp(6*I*e))*exp(-6*I*f*x) + (-110592*I*a**6*c*f**5*exp(8*I*e) - 110592*I*a**6*d*f**5*x*exp(8*I*e) - 27648*a**6*d*f**4*exp(8*I*e))*exp(-4*I*f*x) + (-221184*I*a**6*c*f**5*exp(10*I*e) - 221184*I*a**6*d*f**5*x*exp(10*I*e) - 110592*a**6*d*f**4*exp(10*I*e))*exp(-2*I*f*x))*exp(-12*I*e)/(1179648*a**9*f**6), Ne(1179648*a**9*f**6*exp(12*I*e), 0)), (x**2*(3*d*exp(4*I*e) + 3*d*exp(2*I*e) + d)*exp(-6*I*e)/(16*a**3) + x*(3*c*exp(4*I*e) + 3*c*exp(2*I*e) + c)*exp(-6*I*e)/(8*a**3), True)) + c*x/(8*a**3) + d*x**2/(16*a**3)

$$3.32 \quad \int \frac{1}{(c+dx)(a+ia \tan(e+fx))^3} dx$$

Optimal. Leaf size=449

$$\frac{3i\text{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{i\text{Ci}\left(6xf + \frac{6cf}{d}\right) \sin\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3i\text{Ci}\left(4xf + \frac{4cf}{d}\right) \sin\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{Ci}\left(2xf + \frac{2cf}{d}\right) \cos\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{3\text{Ci}\left(6xf + \frac{6cf}{d}\right) \cos\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3\text{Ci}\left(4xf + \frac{4cf}{d}\right) \cos\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{3\text{Ci}\left(6xf + \frac{6cf}{d}\right) \sin\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3\text{Ci}\left(4xf + \frac{4cf}{d}\right) \sin\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{Ci}\left(2xf + \frac{2cf}{d}\right) \cos\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{3\text{Ci}\left(6xf + \frac{6cf}{d}\right) \cos\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3\text{Ci}\left(4xf + \frac{4cf}{d}\right) \cos\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{Ci}\left(2xf + \frac{2cf}{d}\right) \sin\left(2e - \frac{2cf}{d}\right)}{8a^3d}$$

[Out] $1/8 * \text{Ci}(6*c*f/d + 6*f*x) * \cos(-6*e + 6*c*f/d) / a^{3/d} + 3/8 * \text{Ci}(4*c*f/d + 4*f*x) * \cos(-4*e + 4*c*f/d) / a^{3/d} + 3/8 * \text{Ci}(2*c*f/d + 2*f*x) * \cos(-2*e + 2*c*f/d) / a^{3/d} + 1/8 * \ln(d*x + c) / a^{3/d} - 3/8 * I * \cos(-2*e + 2*c*f/d) * \text{Si}(2*c*f/d + 2*f*x) / a^{3/d} - 3/8 * I * \cos(-4*e + 4*c*f/d) * \text{Si}(4*c*f/d + 4*f*x) / a^{3/d} - 1/8 * I * \cos(-6*e + 6*c*f/d) * \text{Si}(6*c*f/d + 6*f*x) / a^{3/d} + 1/8 * I * \text{Ci}(6*c*f/d + 6*f*x) * \sin(-6*e + 6*c*f/d) / a^{3/d} + 1/8 * \text{Si}(6*c*f/d + 6*f*x) * \sin(-6*e + 6*c*f/d) / a^{3/d} + 3/8 * I * \text{Ci}(4*c*f/d + 4*f*x) * \sin(-4*e + 4*c*f/d) / a^{3/d} + 3/8 * \text{Si}(4*c*f/d + 4*f*x) * \sin(-4*e + 4*c*f/d) / a^{3/d} + 3/8 * I * \text{Ci}(2*c*f/d + 2*f*x) * \sin(-2*e + 2*c*f/d) / a^{3/d} + 3/8 * \text{Si}(2*c*f/d + 2*f*x) * \sin(-2*e + 2*c*f/d) / a^{3/d}$

Rubi [A] time = 1.78, antiderivative size = 449, normalized size of antiderivative = 1.00, number of steps used = 53, number of rules used = 7, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.304$, Rules used = {3728, 3303, 3299, 3302, 3312, 4406, 4428}

$$\frac{3i\text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{i\text{CosIntegral}\left(\frac{6cf}{d} + 6fx\right) \sin\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3i\text{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{3\text{CosIntegral}\left(\frac{6cf}{d} + 6fx\right) \cos\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3\text{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \cos\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{3\text{CosIntegral}\left(\frac{6cf}{d} + 6fx\right) \sin\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3\text{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \cos\left(2e - \frac{2cf}{d}\right)}{8a^3d} - \frac{3\text{CosIntegral}\left(\frac{6cf}{d} + 6fx\right) \cos\left(6e - \frac{6cf}{d}\right)}{8a^3d} - \frac{3\text{CosIntegral}\left(\frac{4cf}{d} + 4fx\right) \cos\left(4e - \frac{4cf}{d}\right)}{8a^3d} + \frac{3\text{CosIntegral}\left(\frac{2cf}{d} + 2fx\right) \sin\left(2e - \frac{2cf}{d}\right)}{8a^3d}$$

Antiderivative was successfully verified.

[In] Int[1/((c + d*x)*(a + I*a*Tan[e + f*x])^3), x]

[Out] $(3 * \text{Cos}[2*e - (2*c*f)/d] * \text{CosIntegral}[(2*c*f)/d + 2*f*x]) / (8*a^3*d) + (3 * \text{Cos}[4*e - (4*c*f)/d] * \text{CosIntegral}[(4*c*f)/d + 4*f*x]) / (8*a^3*d) + (\text{Cos}[6*e - (6*c*f)/d] * \text{CosIntegral}[(6*c*f)/d + 6*f*x]) / (8*a^3*d) + \text{Log}[c + d*x] / (8*a^3*d) - ((I/8) * \text{CosIntegral}[(6*c*f)/d + 6*f*x] * \text{Sin}[6*e - (6*c*f)/d]) / (a^3*d) - (((3*I)/8) * \text{CosIntegral}[(4*c*f)/d + 4*f*x] * \text{Sin}[4*e - (4*c*f)/d]) / (a^3*d) - (((3*I)/8) * \text{CosIntegral}[(2*c*f)/d + 2*f*x] * \text{Sin}[2*e - (2*c*f)/d]) / (a^3*d) - (((3*I)/8) * \text{Cos}[2*e - (2*c*f)/d] * \text{SinIntegral}[(2*c*f)/d + 2*f*x]) / (a^3*d) - (3 * \text{Sin}[2*e - (2*c*f)/d] * \text{SinIntegral}[(2*c*f)/d + 2*f*x]) / (8*a^3*d) - (((3*I)/8) * \text{Cos}[4*e - (4*c*f)/d] * \text{SinIntegral}[(4*c*f)/d + 4*f*x]) / (a^3*d) - (3 * \text{Sin}[4*e - (4*c*f)/d] * \text{SinIntegral}[(4*c*f)/d + 4*f*x]) / (8*a^3*d) - ((I/8) * \text{Cos}[6*e - (6*c*f)/d] * \text{SinIntegral}[(6*c*f)/d + 6*f*x]) / (a^3*d) - (\text{Sin}[6*e - (6*c*f)/d] * \text{SinIntegral}[(6*c*f)/d + 6*f*x]) / (8*a^3*d)$

Rule 3299

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3728

```
Int[((c_.) + (d_.)*(x_))^(m_)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + Cos[2*e + 2*f*x])/(2*a) + Sin[2*e + 2*f*x]/(2*b)]^(-n), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && ILtQ[m, 0] && ILtQ[n, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 4428

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.)*Sin[(c_.) + (d_.)*(x_)]^(q_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x]^p*Sin[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[p, 0] && IGtQ[q, 0] && IntegerQ[m]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{(c+dx)(a+ia \tan(e+fx))^3} dx &= \int \left(\frac{1}{8a^3(c+dx)} + \frac{3 \cos(2e+2fx)}{8a^3(c+dx)} + \frac{3 \cos^2(2e+2fx)}{8a^3(c+dx)} + \frac{\cos^3(2e+2fx)}{8a^3(c+dx)} \right) dx \\ &= \frac{\log(c+dx)}{8a^3d} + \frac{i \int \frac{\sin^3(2e+2fx)}{c+dx} dx}{8a^3} - \frac{(3i) \int \frac{\sin(2e+2fx)}{c+dx} dx}{8a^3} - \frac{(3i) \int \frac{\cos^2(2e+2fx) \sin(2e+2fx)}{c+dx} dx}{8a^3} \\ &= \frac{\log(c+dx)}{8a^3d} + \frac{i \int \left(\frac{3 \sin(2e+2fx)}{4(c+dx)} - \frac{\sin(6e+6fx)}{4(c+dx)} \right) dx}{8a^3} - \frac{(3i) \int \left(\frac{\sin(2e+2fx)}{4(c+dx)} + \frac{\sin(6e+6fx)}{4(c+dx)} \right) dx}{8a^3} \\ &= \frac{3 \cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{8a^3d} + \frac{\log(c+dx)}{8a^3d} - \frac{3i \text{Ci}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{8a^3d} \\ &= \frac{3 \cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{8a^3d} + \frac{\log(c+dx)}{8a^3d} - \frac{3i \text{Ci}\left(\frac{4cf}{d} + 4fx\right) \sin\left(4e - \frac{4cf}{d}\right)}{8a^3d} \\ &= \frac{3 \cos\left(2e - \frac{2cf}{d}\right) \text{Ci}\left(\frac{2cf}{d} + 2fx\right)}{8a^3d} + \frac{\cos\left(6e - \frac{6cf}{d}\right) \text{Ci}\left(\frac{6cf}{d} + 6fx\right)}{8a^3d} + \frac{\log(c+dx)}{8a^3d} \end{aligned}$$

Mathematica [A] time = 0.80, size = 336, normalized size = 0.75

$$\frac{\sec^3(e+fx)(\cos(fx) + i \sin(fx))^3 \left(\cos\left(e - \frac{4cf}{d}\right) - i \sin\left(e - \frac{4cf}{d}\right) \right) \left(-i \text{Ci}\left(\frac{6f(c+dx)}{d}\right) \sin\left(2e - \frac{2cf}{d}\right) + \text{Ci}\left(\frac{6f(c+dx)}{d}\right) \right)}{8a^3d}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[1/((c + d*x)*(a + I*a*Tan[e + f*x])^3), x]
```


[Out] $(\text{Sec}[e + f*x]^3 * (\text{Cos}[f*x] + I * \text{Sin}[f*x])^3 * (\text{Cos}[3*e] * \text{Log}[f*(c + d*x)] + I * \text{Log}[f*(c + d*x)] * \text{Sin}[3*e] + (\text{Cos}[e - (4*c*f)/d] - I * \text{Sin}[e - (4*c*f)/d]) * (3 * \text{CosIntegral}[(4*f*(c + d*x))/d] + \text{Cos}[2*e - (2*c*f)/d] * \text{CosIntegral}[(6*f*(c + d*x))/d] + 3 * \text{CosIntegral}[(2*f*(c + d*x))/d] * (\text{Cos}[2*e - (2*c*f)/d] + I * \text{Sin}[2*e - (2*c*f)/d]) - I * \text{CosIntegral}[(6*f*(c + d*x))/d] * \text{Sin}[2*e - (2*c*f)/d] - (3 * I) * \text{Cos}[2*e - (2*c*f)/d] * \text{SinIntegral}[(2*f*(c + d*x))/d] + 3 * \text{Sin}[2*e - (2*c*f)/d] * \text{SinIntegral}[(2*f*(c + d*x))/d] - (3 * I) * \text{SinIntegral}[(4*f*(c + d*x))/d] - I * \text{Cos}[2*e - (2*c*f)/d] * \text{SinIntegral}[(6*f*(c + d*x))/d] - \text{Sin}[2*e - (2*c*f)/d] * \text{SinIntegral}[(6*f*(c + d*x))/d])) / (8*d*(a + I*a*\text{Tan}[e + f*x])^3)$

fricas [A] time = 0.44, size = 111, normalized size = 0.25

$$\frac{3 \operatorname{Ei}\left(\frac{-2i d f x - 2i c f}{d}\right) e^{\left(\frac{-2i d e + 2i c f}{d}\right)} + 3 \operatorname{Ei}\left(\frac{-4i d f x - 4i c f}{d}\right) e^{\left(\frac{-4i d e + 4i c f}{d}\right)} + \operatorname{Ei}\left(\frac{-6i d f x - 6i c f}{d}\right) e^{\left(\frac{-6i d e + 6i c f}{d}\right)} + \log\left(\frac{d x + c}{d}\right)}{8 a^3 d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))^3,x, algorithm="fricas")

[Out] $1/8 * (3 * \operatorname{Ei}((-2 * I * d * f * x - 2 * I * c * f) / d) * e^{((-2 * I * d * e + 2 * I * c * f) / d)} + 3 * \operatorname{Ei}((-4 * I * d * f * x - 4 * I * c * f) / d) * e^{((-4 * I * d * e + 4 * I * c * f) / d)} + \operatorname{Ei}((-6 * I * d * f * x - 6 * I * c * f) / d) * e^{((-6 * I * d * e + 6 * I * c * f) / d)} + \log((d * x + c) / d)) / (a^3 * d)$

giac [B] time = 1.46, size = 846, normalized size = 1.88

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))^3,x, algorithm="giac")

[Out] $(3 * \cos(2 * c * f / d) * \cos(2 * e)^2 * \cos_integral(-2 * (d * f * x + c * f) / d) + \cos(2 * e)^3 * \log(d * x + c) + 3 * I * \cos(2 * e)^2 * \cos_integral(-2 * (d * f * x + c * f) / d) * \sin(2 * c * f / d) + 6 * I * \cos(2 * c * f / d) * \cos(2 * e) * \cos_integral(-2 * (d * f * x + c * f) / d) * \sin(2 * e) + 3 * I * \cos(2 * e)^2 * \log(d * x + c) * \sin(2 * e) - 6 * \cos(2 * e) * \cos_integral(-2 * (d * f * x + c * f) / d) * \sin(2 * c * f / d) * \sin(2 * e) - 3 * \cos(2 * c * f / d) * \cos_integral(-2 * (d * f * x + c * f) / d) * \sin(2 * e)^2 - 3 * \cos(2 * e) * \log(d * x + c) * \sin(2 * e)^2 - 3 * I * \cos_integral(-2 * (d * f * x + c * f) / d) * \sin(2 * c * f / d) * \sin(2 * e)^2 - I * \log(d * x + c) * \sin(2 * e)^3 - 3 * I * \cos(2 * c * f / d) * \cos(2 * e)^2 * \sin_integral(2 * (d * f * x + c * f) / d) + 3 * \cos(2 * e)^2 * \sin(2 * c * f / d) * \sin_integral(2 * (d * f * x + c * f) / d) + 6 * \cos(2 * c * f / d) * \cos(2 * e) * \sin(2 * e) * \sin_integral(2 * (d * f * x + c * f) / d) + 6 * I * \cos(2 * e) * \sin(2 * c * f / d) * \sin(2 * e) * \sin_integral(2 * (d * f * x + c * f) / d) + 3 * I * \cos(2 * c * f / d) * \sin(2 * e)^2 * \sin_integral(2 * (d * f * x + c * f) / d) - 3 * \sin(2 * c * f / d) * \sin(2 * e)^2 * \sin_integral(2 * (d * f * x + c * f) / d) + 3 * \cos(4 * c * f / d) * \cos(2 * e) * \cos_integral(-4 * (d * f * x + c * f) / d) + 3 * I * \cos(2 * e) * \cos_integral(-4 * (d * f * x + c * f) / d) * \sin(4 * c * f / d) + 3 * I * \cos(4 * c * f / d) * \cos_integral(-4 * (d * f * x + c * f) / d) * \sin(2 * e) - 3 * \cos_integral(-4 * (d * f * x + c * f) / d) * \sin(4 * c * f / d) * \sin(2 * e) - 3 * I * \cos(4 * c * f / d) * \cos(2 * e) * \sin_integral(4 * (d * f * x + c * f) / d) + 3 * \cos(2 * e) * \sin(4 * c * f / d) * \sin_integral(4 * (d * f * x + c * f) / d) + 3 * \cos(4 * c * f / d) * \sin(2 * e) * \sin_integral(4 * (d * f * x + c * f) / d) + 3 * I * \sin(4 * c * f / d) * \sin(2 * e) * \sin_integral(4 * (d * f * x + c * f) / d) + \cos(6 * c * f / d) * \cos_integral(-6 * (d * f * x + c * f) / d) + I * \cos_integral(-6 * (d * f * x + c * f) / d) * \sin(6 * c * f / d) - I * \cos(6 * c * f / d) * \sin_integral(6 * (d * f * x + c * f) / d) + \sin(6 * c * f / d) * \sin_integral(6 * (d * f * x + c * f) / d)) / (8 * a^3 * d * \cos(2 * e)^3 + 24 * I * a^3 * d * \cos(2 * e)^2 * \sin(2 * e) - 24 * a^3 * d * \cos(2 * e) * \sin(2 * e)^2 - 8 * I * a^3 * d * \sin(2 * e)^3)$

maple [A] time = 0.62, size = 560, normalized size = 1.25

$$\frac{3i \operatorname{Si}\left(4fx + 4e + \frac{4cf - 4de}{d}\right) \cos\left(\frac{4cf - 4de}{d}\right)}{8a^3d} + \frac{3i \operatorname{Ci}\left(4fx + 4e + \frac{4cf - 4de}{d}\right) \sin\left(\frac{4cf - 4de}{d}\right)}{8a^3d} - \frac{3i \operatorname{Si}\left(2fx + 2e + \frac{2cf - 2de}{d}\right)}{8a^3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)/(a+I*a*tan(f*x+e))^3,x)

[Out]
$$-3/8*I/a^3*Si(4*f*x+4*e+4*(c*f-d*e)/d)*cos(4*(c*f-d*e)/d)/d+3/8*I/a^3*Ci(4*f*x+4*e+4*(c*f-d*e)/d)*sin(4*(c*f-d*e)/d)/d-3/8*I/a^3*Si(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d+3/8*I/a^3*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d-1/8*I/a^3*Si(6*f*x+6*e+6*(c*f-d*e)/d)*cos(6*(c*f-d*e)/d)/d+1/8*I/a^3*Ci(6*f*x+6*e+6*(c*f-d*e)/d)*sin(6*(c*f-d*e)/d)/d+1/8/a^3*Si(6*f*x+6*e+6*(c*f-d*e)/d)*sin(6*(c*f-d*e)/d)/d+1/8/a^3*Ci(6*f*x+6*e+6*(c*f-d*e)/d)*cos(6*(c*f-d*e)/d)/d+3/8/a^3*Si(4*f*x+4*e+4*(c*f-d*e)/d)*sin(4*(c*f-d*e)/d)/d+3/8/a^3*Ci(4*f*x+4*e+4*(c*f-d*e)/d)*cos(4*(c*f-d*e)/d)/d+3/8/a^3*Si(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d+3/8/a^3*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d+1/8/a^3*ln((f*x+e)*d+c*f-d*e)/d$$

maxima [A] time = 3.02, size = 270, normalized size = 0.60

$$f \cos\left(-\frac{6(de-cf)}{d}\right) E_1\left(\frac{6i(fx+e)d-6ide+6icf}{d}\right) + 3f \cos\left(-\frac{4(de-cf)}{d}\right) E_1\left(\frac{4i(fx+e)d-4ide+4icf}{d}\right) + 3f \cos\left(-\frac{2(de-cf)}{d}\right) E_1\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))^3,x, algorithm="maxima")

[Out]
$$-1/8*(f*cos(-6*(d*e - c*f)/d)*exp_integral_e(1, (6*I*(f*x + e)*d - 6*I*d*e + 6*I*c*f)/d) + 3*f*cos(-4*(d*e - c*f)/d)*exp_integral_e(1, (4*I*(f*x + e)*d - 4*I*d*e + 4*I*c*f)/d) + 3*f*cos(-2*(d*e - c*f)/d)*exp_integral_e(1, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d) + 3*I*f*exp_integral_e(1, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d)*sin(-2*(d*e - c*f)/d) + 3*I*f*exp_integral_e(1, (4*I*(f*x + e)*d - 4*I*d*e + 4*I*c*f)/d)*sin(-4*(d*e - c*f)/d) + I*f*exp_integral_e(1, (6*I*(f*x + e)*d - 6*I*d*e + 6*I*c*f)/d)*sin(-6*(d*e - c*f)/d) - f*log((f*x + e)*d - d*e + c*f))/(a^3*d*f)$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + a \tan(e + f x) i)^3 (c + d x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + a*tan(e + f*x)*1i)^3*(c + d*x)),x)

[Out] int(1/((a + a*tan(e + f*x)*1i)^3*(c + d*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{i \int \frac{1}{c \tan^3(e+fx) - 3ic \tan^2(e+fx) - 3c \tan(e+fx) + ic + dx \tan^3(e+fx) - 3idx \tan^2(e+fx) - 3dx \tan(e+fx) + idx} dx}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+I*a*tan(f*x+e))^3,x)

[Out]
$$I*Integral(1/(c*tan(e + f*x)**3 - 3*I*c*tan(e + f*x)**2 - 3*c*tan(e + f*x) + I*c + d*x*tan(e + f*x)**3 - 3*I*d*x*tan(e + f*x)**2 - 3*d*x*tan(e + f*x) + I*d*x), x)/a**3$$

$$3.33 \quad \int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))^3} dx$$

Optimal. Leaf size=712

$$\frac{3f\text{Ci}\left(6xf + \frac{6cf}{d}\right)\sin\left(6e - \frac{6cf}{d}\right)}{4a^3d^2} - \frac{3f\text{Ci}\left(4xf + \frac{4cf}{d}\right)\sin\left(4e - \frac{4cf}{d}\right)}{2a^3d^2} - \frac{3f\text{Ci}\left(2xf + \frac{2cf}{d}\right)\sin\left(2e - \frac{2cf}{d}\right)}{4a^3d^2} - 3f\text{Ci}\left(\frac{2cf}{d}\right)$$

[Out] $-1/8/a^3/d/(d*x+c)-3/4*I*f*Ci(2*c*f/d+2*f*x)*\cos(-2*e+2*c*f/d)/a^3/d^2-1/8*I*\sin(2*f*x+2*e)^3/a^3/d/(d*x+c)+3/32*I*\sin(6*f*x+6*e)/a^3/d/(d*x+c)-9/32*\cos(2*f*x+2*e)/a^3/d/(d*x+c)-3/8*\cos(2*f*x+2*e)^2/a^3/d/(d*x+c)-1/8*\cos(2*f*x+2*e)^3/a^3/d/(d*x+c)-3/32*\cos(6*f*x+6*e)/a^3/d/(d*x+c)-3/4*f*\cos(-2*e+2*c*f/d)*Si(2*c*f/d+2*f*x)/a^3/d^2-3/2*f*\cos(-4*e+4*c*f/d)*Si(4*c*f/d+4*f*x)/a^3/d^2-3/4*f*\cos(-6*e+6*c*f/d)*Si(6*c*f/d+6*f*x)/a^3/d^2+3/4*f*Ci(6*c*f/d+6*f*x)*\sin(-6*e+6*c*f/d)/a^3/d^2-3/4*I*f*Si(2*c*f/d+2*f*x)*\sin(-2*e+2*c*f/d)/a^3/d^2+3/2*f*Ci(4*c*f/d+4*f*x)*\sin(-4*e+4*c*f/d)/a^3/d^2-3/4*I*f*Si(6*c*f/d+6*f*x)*\sin(-6*e+6*c*f/d)/a^3/d^2+3/4*f*Ci(2*c*f/d+2*f*x)*\sin(-2*e+2*c*f/d)/a^3/d^2+15/32*I*\sin(2*f*x+2*e)/a^3/d/(d*x+c)+3/8*I*\sin(4*f*x+4*e)/a^3/d/(d*x+c)+3/8*\sin(2*f*x+2*e)^2/a^3/d/(d*x+c)-3/4*I*f*Ci(6*c*f/d+6*f*x)*\cos(-6*e+6*c*f/d)/a^3/d^2-3/2*I*f*Ci(4*c*f/d+4*f*x)*\cos(-4*e+4*c*f/d)/a^3/d^2-3/2*I*f*Si(4*c*f/d+4*f*x)*\sin(-4*e+4*c*f/d)/a^3/d^2$

Rubi [A] time = 1.73, antiderivative size = 712, normalized size of antiderivative = 1.00, number of steps used = 60, number of rules used = 9, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.391$, Rules used = {3728, 3297, 3303, 3299, 3302, 3313, 12, 4406, 4428}

$$\frac{3f\text{CosIntegral}\left(\frac{6cf}{d} + 6fx\right)\sin\left(6e - \frac{6cf}{d}\right)}{4a^3d^2} - \frac{3f\text{CosIntegral}\left(\frac{4cf}{d} + 4fx\right)\sin\left(4e - \frac{4cf}{d}\right)}{2a^3d^2} - \frac{3f\text{CosIntegral}\left(\frac{2cf}{d}\right)}{4a^3d^2}$$

Antiderivative was successfully verified.

[In] Int[1/((c + d*x)^2*(a + I*a*Tan[e + f*x])^3),x]

[Out] $-1/(8*a^3*d*(c + d*x)) - (9*\text{Cos}[2*e + 2*f*x])/(32*a^3*d*(c + d*x)) - (3*\text{Cos}[2*e + 2*f*x]^2)/(8*a^3*d*(c + d*x)) - \text{Cos}[2*e + 2*f*x]^3/(8*a^3*d*(c + d*x)) - (3*\text{Cos}[6*e + 6*f*x])/(32*a^3*d*(c + d*x)) - (((3*I)/4)*f*\text{Cos}[2*e - (2*c*f)/d]*\text{CosIntegral}[(2*c*f)/d + 2*f*x])/(a^3*d^2) - (((3*I)/2)*f*\text{Cos}[4*e - (4*c*f)/d]*\text{CosIntegral}[(4*c*f)/d + 4*f*x])/(a^3*d^2) - (((3*I)/4)*f*\text{Cos}[6*e - (6*c*f)/d]*\text{CosIntegral}[(6*c*f)/d + 6*f*x])/(a^3*d^2) - (3*f*\text{CosIntegral}[(6*c*f)/d + 6*f*x]*\text{Sin}[6*e - (6*c*f)/d])/(4*a^3*d^2) - (3*f*\text{CosIntegral}[(4*c*f)/d + 4*f*x]*\text{Sin}[4*e - (4*c*f)/d])/(2*a^3*d^2) - (3*f*\text{CosIntegral}[(2*c*f)/d + 2*f*x]*\text{Sin}[2*e - (2*c*f)/d])/(4*a^3*d^2) + (((15*I)/32)*\text{Sin}[2*e + 2*f*x])/(a^3*d*(c + d*x)) + (3*\text{Sin}[2*e + 2*f*x]^2)/(8*a^3*d*(c + d*x)) - ((I/8)*\text{Sin}[2*e + 2*f*x]^3)/(a^3*d*(c + d*x)) + (((3*I)/8)*\text{Sin}[4*e + 4*f*x])/(a^3*d*(c + d*x)) + (((3*I)/32)*\text{Sin}[6*e + 6*f*x])/(a^3*d*(c + d*x)) - (3*f*\text{Cos}[2*e - (2*c*f)/d]*\text{SinIntegral}[(2*c*f)/d + 2*f*x])/(4*a^3*d^2) + (((3*I)/4)*f*\text{Sin}[2*e - (2*c*f)/d]*\text{SinIntegral}[(2*c*f)/d + 2*f*x])/(a^3*d^2) - (3*f*\text{Cos}[4*e - (4*c*f)/d]*\text{SinIntegral}[(4*c*f)/d + 4*f*x])/(2*a^3*d^2) + (((3*I)/2)*f*\text{Sin}[4*e - (4*c*f)/d]*\text{SinIntegral}[(4*c*f)/d + 4*f*x])/(a^3*d^2) - (3*f*\text{Cos}[6*e - (6*c*f)/d]*\text{SinIntegral}[(6*c*f)/d + 6*f*x])/(4*a^3*d^2) + (((3*I)/4)*f*\text{Sin}[6*e - (6*c*f)/d]*\text{SinIntegral}[(6*c*f)/d + 6*f*x])/(a^3*d^2)$

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3297

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x]/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]
```

Rule 3313

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x]^n/(d*(m + 1)), x] - Dist[(f*n)/(d*(m + 1)), Int[ExpandTrigReduce[(c + d*x)^(m + 1), Cos[e + f*x]*Sin[e + f*x]^(n - 1), x], x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && GeQ[m, -2] && LtQ[m, -1]
```

Rule 3728

```
Int[((c_.) + (d_.)*(x_))^(m_)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + Cos[2*e + 2*f*x]/(2*a) + Sin[2*e + 2*f*x]/(2*b))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[a^2 + b^2, 0] && ILtQ[m, 0] && ILtQ[n, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 4428

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.)*Sin[(c_.) + (d_.)*(x_)]^(q_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x]^p*Sin[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[p, 0] && IGtQ[q, 0] && IntegerQ[m]
```

Rubi steps

$$\begin{aligned}
\int \frac{1}{(c+dx)^2(a+ia \tan(e+fx))^3} dx &= \int \left(\frac{1}{8a^3(c+dx)^2} + \frac{3 \cos(2e+2fx)}{8a^3(c+dx)^2} + \frac{3 \cos^2(2e+2fx)}{8a^3(c+dx)^2} + \frac{\cos^3(2e+2fx)}{8a^3(c+dx)^2} \right) dx \\
&= \frac{1}{8a^3 d(c+dx)} + \frac{i \int \frac{\sin^3(2e+2fx)}{(c+dx)^2} dx}{8a^3} - \frac{(3i) \int \frac{\sin(2e+2fx)}{(c+dx)^2} dx}{8a^3} - \frac{(3i) \int \frac{\cos^2(2e+2fx)}{(c+dx)^2} dx}{8a^3} \\
&= \frac{1}{8a^3 d(c+dx)} - \frac{3 \cos(2e+2fx)}{8a^3 d(c+dx)} - \frac{3 \cos^2(2e+2fx)}{8a^3 d(c+dx)} - \frac{\cos^3(2e+2fx)}{8a^3 d(c+dx)} \\
&= \frac{1}{8a^3 d(c+dx)} - \frac{3 \cos(2e+2fx)}{8a^3 d(c+dx)} - \frac{3 \cos^2(2e+2fx)}{8a^3 d(c+dx)} - \frac{\cos^3(2e+2fx)}{8a^3 d(c+dx)} \\
&= \frac{1}{8a^3 d(c+dx)} - \frac{9 \cos(2e+2fx)}{32a^3 d(c+dx)} - \frac{3 \cos^2(2e+2fx)}{8a^3 d(c+dx)} - \frac{\cos^3(2e+2fx)}{8a^3 d(c+dx)} \\
&= \frac{1}{8a^3 d(c+dx)} - \frac{9 \cos(2e+2fx)}{32a^3 d(c+dx)} - \frac{3 \cos^2(2e+2fx)}{8a^3 d(c+dx)} - \frac{\cos^3(2e+2fx)}{8a^3 d(c+dx)} \\
&= \frac{1}{8a^3 d(c+dx)} - \frac{9 \cos(2e+2fx)}{32a^3 d(c+dx)} - \frac{3 \cos^2(2e+2fx)}{8a^3 d(c+dx)} - \frac{\cos^3(2e+2fx)}{8a^3 d(c+dx)}
\end{aligned}$$

Mathematica [A] time = 3.16, size = 833, normalized size = 1.17

$$\sec^3(e+fx) \left(\sin\left(\frac{3cf}{d}\right) - i \cos\left(\frac{3cf}{d}\right) \right) \left(3d \cos\left(e+f\left(x-\frac{3c}{d}\right)\right) + d \cos\left(3\left(e+f\left(x-\frac{c}{d}\right)\right)\right) + d \cos\left(3\left(e+f\left(\frac{c}{d}+x\right)\right)\right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[1/((c+d*x)^2*(a+I*a*Tan[e+f*x])^3),x]

[Out] (Sec[e+f*x]^3*((-I)*Cos[(3*c*f)/d]+Sin[(3*c*f)/d])*(3*d*Cos[e+f*((-3*c)/d+x)]+d*Cos[3*(e+f*((-c)/d+x))] + d*Cos[3*(e+f*(c/d+x))] + 3*d*Cos[e+f*((3*c)/d+x)] + (6*I)*c*f*Cos[3*e-(3*f*(c+d*x))/d]*CosIntegral[(6*f*(c+d*x))/d] + (6*I)*d*f*x*Cos[3*e-(3*f*(c+d*x))/d]*CosIntegral[(6*f*(c+d*x))/d] + (6*I)*f*(c+d*x)*CosIntegral[(2*f*(c+d*x))/d]*(Cos[e-(c*f)/d+3*f*x]+I*Sin[e-(c*f)/d+3*f*x]) + (3*I)*d*Sin[e+f*((-3*c)/d+x)] + I*d*Sin[3*(e+f*((-c)/d+x))] - I*d*Sin[3*(e+f*(c/d+x))] - (3*I)*d*Sin[e+f*((3*c)/d+x)] + 6*c*f*CosIntegral[(6*f*(c+d*x))/d]*Sin[3*e-(3*f*(c+d*x))/d] + 6*d*f*x*CosIntegral[(6*f*(c+d*x))/d]*Sin[3*e-(3*f*(c+d*x))/d] + 12*f*(c+d*x)*CosIntegral[(4*f*(c+d*x))/d]*(I*Cos[e-(f*(c+3*d*x))/d]+Sin[e-(f*(c+3*d*x))/d]) + 6*c*f*Cos[e-(c*f)/d+3*f*x]*SinIntegral[(2*f*(c+d*x))/d] + 6*d*f*x*Cos[e-(c*f)/d+3*f*x]*SinIntegral[(2*f*(c+d*x))/d] + (6*I)*c*f*Sin[e-(c*f)/d+3*f*x]*SinIntegral[(2*f*(c+d*x))/d] + (6*I)*d*f*x*Sin[e-(c*f)/d+3*f*x]*SinIntegral[(2*f*(c+d*x))/d] + 12*c*f*Cos[e-(f*(c+3*d*x))/d]*SinIntegral[(4*f*(c+d*x))/d] + 12*d*f*x*Cos[e-(f*(c+3*d*x))/d]*SinIntegral[(4*f*(c+d*x))/d] - (12*I)*c*f*Sin[e-(f*(c+3*d*x))/d]*SinIntegral[(4*f*(c+d*x))/d] - (12*I)*d*f*x*Sin[e-(f*(c+3*d*x))/d]*SinIntegral[(4*f*(c+d*x))/d] + 6*c*f*Cos[3*e-(3*f*(c+d*x))/d]*SinIntegral[(6*f*(c+d*x))/d] + 6*d*f*x*Cos[3*e-(3*f*(c+d*x))/d]*SinIntegral[(6*f*(c+d*x))/d] - (6*I)*c*f*Sin[3*e-(3*f*(c+d*x))/d]*SinIntegral[(6*f*(c+d*x))/d] - (6

*I)*d*f*x*Sin[3*e - (3*f*(c + d*x))/d]*SinIntegral[(6*f*(c + d*x))/d)]/(8*a^3*d^2*(c + d*x)*(-I + Tan[e + f*x])^3)

fricas [A] time = 0.45, size = 192, normalized size = 0.27

$$\frac{\left(\left(-6i d f x - 6i c f\right) \operatorname{Ei}\left(\frac{-2i d f x - 2i c f}{d}\right) e^{\left(\frac{-2i d e + 2i c f}{d}\right)} + \left(-12i d f x - 12i c f\right) \operatorname{Ei}\left(\frac{-4i d f x - 4i c f}{d}\right) e^{\left(\frac{-4i d e + 4i c f}{d}\right)} + \left(-6i d f x - 6i c f\right) \operatorname{Ei}\left(\frac{-6i d f x - 6i c f}{d}\right) e^{\left(\frac{-6i d e + 6i c f}{d}\right)} - d\right) e^{\left(\frac{6i f x + 6i e}{d}\right)} - 3d e^{\left(\frac{4i f x + 4i e}{d}\right)} - 3d e^{\left(\frac{2i f x + 2i e}{d}\right)} - d\right) e^{\left(\frac{-6i f x - 6i e}{d}\right)}}{8\left(a^3 d^3 x + a^3 c d^2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^3,x, algorithm="fricas")

[Out] 1/8*(((-6*I*d*f*x - 6*I*c*f)*Ei((-2*I*d*f*x - 2*I*c*f)/d)*e^((-2*I*d*e + 2*I*c*f)/d) + (-12*I*d*f*x - 12*I*c*f)*Ei((-4*I*d*f*x - 4*I*c*f)/d)*e^((-4*I*d*e + 4*I*c*f)/d) + (-6*I*d*f*x - 6*I*c*f)*Ei((-6*I*d*f*x - 6*I*c*f)/d)*e^((-6*I*d*e + 6*I*c*f)/d) - d)*e^(6*I*f*x + 6*I*e) - 3*d*e^(4*I*f*x + 4*I*e) - 3*d*e^(2*I*f*x + 2*I*e) - d)*e^(-6*I*f*x - 6*I*e)/(a^3*d^3*x + a^3*c*d^2)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^3,x, algorithm="giac")

[Out] Timed out

maple [A] time = 0.63, size = 787, normalized size = 1.11

$$3if^2 \left(-\frac{4 \sin(4fx+4e)}{((fx+e)d+cf-de)d} + \frac{16 \operatorname{Si}\left(4fx+4e+\frac{4cf-4de}{d}\right) \sin\left(\frac{4cf-4de}{d}\right)}{d} + \frac{16 \operatorname{Ci}\left(4fx+4e+\frac{4cf-4de}{d}\right) \cos\left(\frac{4cf-4de}{d}\right)}{d} \right) - 3if^2 \left(-\frac{2 \sin(2fx+2e)}{((fx+e)d+cf-de)d} + \frac{4 \operatorname{Si}\left(2fx+2e+\frac{2cf-2de}{d}\right) \sin\left(\frac{2cf-2de}{d}\right)}{d} + \frac{4 \operatorname{Ci}\left(2fx+2e+\frac{2cf-2de}{d}\right) \cos\left(\frac{2cf-2de}{d}\right)}{d} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^3,x)

[Out] 1/a^3/f*(-3/32*I*f^2*(-4*sin(4*f*x+4*e)/((f*x+e)*d+c*f-d*e)/d+4*(4*Si(4*f*x+4*e+4*(c*f-d*e)/d)*sin(4*(c*f-d*e)/d)/d+4*Ci(4*f*x+4*e+4*(c*f-d*e)/d)*cos(4*(c*f-d*e)/d)/d)-3/16*I*f^2*(-2*sin(2*f*x+2*e)/((f*x+e)*d+c*f-d*e)/d+2*(2*Si(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d+2*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d)-1/48*I*f^2*(-6*sin(6*f*x+6*e)/((f*x+e)*d+c*f-d*e)/d+6*(6*Si(6*f*x+6*e+6*(c*f-d*e)/d)*sin(6*(c*f-d*e)/d)/d+6*Ci(6*f*x+6*e+6*(c*f-d*e)/d)*cos(6*(c*f-d*e)/d)/d)+1/48*f^2*(-6*cos(6*f*x+6*e)/((f*x+e)*d+c*f-d*e)/d-6*(6*Si(6*f*x+6*e+6*(c*f-d*e)/d)*cos(6*(c*f-d*e)/d)/d-6*Ci(6*f*x+6*e+6*(c*f-d*e)/d)*sin(6*(c*f-d*e)/d)/d)+3/32*f^2*(-4*cos(4*f*x+4*e)/((f*x+e)*d+c*f-d*e)/d-4*(4*Si(4*f*x+4*e+4*(c*f-d*e)/d)*cos(4*(c*f-d*e)/d)/d-4*Ci(4*f*x+4*e+4*(c*f-d*e)/d)*sin(4*(c*f-d*e)/d)/d)+3/16*f^2*(-2*cos(2*f*x+2*e)/((f*x+e)*d+c*f-d*e)/d-2*(2*Si(2*f*x+2*e+2*(c*f-d*e)/d)*cos(2*(c*f-d*e)/d)/d-2*Ci(2*f*x+2*e+2*(c*f-d*e)/d)*sin(2*(c*f-d*e)/d)/d)-1/8*f^2/((f*x+e)*d+c*f-d*e)/d)

maxima [A] time = 4.08, size = 294, normalized size = 0.41

$$8192 f^2 \cos\left(-\frac{6(de-cf)}{d}\right) E_2\left(\frac{6i(fx+e)d-6ide+6icf}{d}\right) + 24576 f^2 \cos\left(-\frac{4(de-cf)}{d}\right) E_2\left(\frac{4i(fx+e)d-4ide+4icf}{d}\right) + 24576 f^2 \cos\left(-\frac{2(de-cf)}{d}\right) E_2\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right) + 24576 f^2 \cos\left(-\frac{4(de-cf)}{d}\right) E_2\left(\frac{4i(fx+e)d-4ide+4icf}{d}\right) + 24576 f^2 \cos\left(-\frac{2(de-cf)}{d}\right) E_2\left(\frac{2i(fx+e)d-2ide+2icf}{d}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+I*a*tan(f*x+e))^3,x, algorithm="maxima")

[Out]
$$-1/65536*(8192*f^2*\cos(-6*(d*e - c*f)/d)*\exp_integral_e(2, (6*I*(f*x + e)*d - 6*I*d*e + 6*I*c*f)/d) + 24576*f^2*\cos(-4*(d*e - c*f)/d)*\exp_integral_e(2, (4*I*(f*x + e)*d - 4*I*d*e + 4*I*c*f)/d) + 24576*f^2*\cos(-2*(d*e - c*f)/d)*\exp_integral_e(2, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d) + 24576*I*f^2*\exp_integral_e(2, (2*I*(f*x + e)*d - 2*I*d*e + 2*I*c*f)/d)*\sin(-2*(d*e - c*f)/d) + 24576*I*f^2*\exp_integral_e(2, (4*I*(f*x + e)*d - 4*I*d*e + 4*I*c*f)/d)*\sin(-4*(d*e - c*f)/d) + 8192*I*f^2*\exp_integral_e(2, (6*I*(f*x + e)*d - 6*I*d*e + 6*I*c*f)/d)*\sin(-6*(d*e - c*f)/d) + 8192*f^2)/(((f*x + e)*a^3*d^2 - a^3*d^2*e + a^3*c*d*f)*f)$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{1}{(a + a \tan(e + f x) i)^3 (c + d x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + a*tan(e + f*x)*1i)^3*(c + d*x)^2),x)

[Out] int(1/((a + a*tan(e + f*x)*1i)^3*(c + d*x)^2), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$i \int \frac{1}{c^2 \tan^3(e+fx) - 3ic^2 \tan^2(e+fx) - 3c^2 \tan(e+fx) + ic^2 + 2cdx \tan^3(e+fx) - 6icdx \tan^2(e+fx) - 6cdx \tan(e+fx) + 2icdx + d^2x^2 \tan^3(e+fx) - 3id^2x^2 \tan^2(e+fx) - 3id^2x^2 \tan(e+fx) + d^2x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**2/(a+I*a*tan(f*x+e))**3,x)

[Out]
$$I*\text{Integral}(1/(c**2*\tan(e + f*x)**3 - 3*I*c**2*\tan(e + f*x)**2 - 3*c**2*\tan(e + f*x) + I*c**2 + 2*c*d*x*\tan(e + f*x)**3 - 6*I*c*d*x*\tan(e + f*x)**2 - 6*c*d*x*\tan(e + f*x) + 2*I*c*d*x + d**2*x**2*\tan(e + f*x)**3 - 3*I*d**2*x**2*\tan(e + f*x)**2 - 3*d**2*x**2*\tan(e + f*x) + I*d**2*x**2), x)/a**3$$

3.34 $\int (c + dx)^m (a + ia \tan(e + fx))^2 dx$

Optimal. Leaf size=26

$$\text{Int}((c + dx)^m (a + ia \tan(e + fx))^2, x)$$

[Out] Unintegrable((d*x+c)^m*(a+I*a*tan(f*x+e))^2,x)

Rubi [A] time = 0.05, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int (c + dx)^m (a + ia \tan(e + fx))^2 dx$$

Verification is Not applicable to the result.

[In] Int[(c + d*x)^m*(a + I*a*Tan[e + f*x])^2,x]

[Out] Defer[Int][(c + d*x)^m*(a + I*a*Tan[e + f*x])^2, x]

Rubi steps

$$\int (c + dx)^m (a + ia \tan(e + fx))^2 dx = \int (c + dx)^m (a + ia \tan(e + fx))^2 dx$$

Mathematica [A] time = 39.44, size = 0, normalized size = 0.00

$$\int (c + dx)^m (a + ia \tan(e + fx))^2 dx$$

Verification is Not applicable to the result.

[In] Integrate[(c + d*x)^m*(a + I*a*Tan[e + f*x])^2,x]

[Out] Integrate[(c + d*x)^m*(a + I*a*Tan[e + f*x])^2, x]

fricas [A] time = 0.52, size = 0, normalized size = 0.00

$$\frac{-2i(dx + c)^m a^2 + \left(f e^{(2i f x + 2i e)} + f \right) \text{integral} \left(-\frac{2 \left(-i a^2 d m - 2 (a^2 d f x + a^2 c f) e^{(2i f x + 2i e)} \right) (dx + c)^m}{d f x + c f + (d f x + c f) e^{(2i f x + 2i e)}}, x \right)}{f e^{(2i f x + 2i e)} + f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m*(a+I*a*tan(f*x+e))^2,x, algorithm="fricas")

[Out] (-2*I*(d*x + c)^m*a^2 + (f*e^(2*I*f*x + 2*I*e) + f)*integral(-2*(-I*a^2*d*m - 2*(a^2*d*f*x + a^2*c*f)*e^(2*I*f*x + 2*I*e))*(d*x + c)^m/(d*f*x + c*f + (d*f*x + c*f)*e^(2*I*f*x + 2*I*e)), x))/(f*e^(2*I*f*x + 2*I*e) + f)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int (ia \tan(fx + e) + a)^2 (dx + c)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m*(a+I*a*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate((I*a*tan(f*x + e) + a)^2*(d*x + c)^m, x)

maple [A] time = 0.40, size = 0, normalized size = 0.00

$$\int (dx + c)^m (a + ia \tan(fx + e))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^m*(a+I*a*tan(f*x+e))^2,x)

[Out] int((d*x+c)^m*(a+I*a*tan(f*x+e))^2,x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\frac{(dx + c)^{m+1} a^2}{d(m+1)} + \int \frac{3(dx + c)^m a^2 \cos(4fx + 4e)^2 - 4(dx + c)^m a^2 \cos(2fx + 2e)^2 + 3(dx + c)^m a^2 \sin(4fx + 4e) \sin(2fx + 2e)}{2(2 \cos(2fx + 2e) + 1) \cos(4fx + 4e)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m*(a+I*a*tan(f*x+e))^2,x, algorithm="maxima")

[Out] (d*x + c)^(m + 1)*a^2/(d*(m + 1)) + integrate((3*(d*x + c)^m*a^2*cos(4*f*x + 4*e)^2 - 4*(d*x + c)^m*a^2*cos(2*f*x + 2*e)^2 + 3*(d*x + c)^m*a^2*sin(4*f*x + 4*e)*sin(2*f*x + 2*e) - 4*(d*x + c)^m*a^2*cos(2*f*x + 2*e)^2 - 4*(d*x + c)^m*a^2*cos(2*f*x + 2*e) - (d*x + c)^m*a^2 + 2*(2*(d*x + c)^m*a^2*cos(2*f*x + 2*e) + (d*x + c)^m*a^2)*cos(4*f*x + 4*e))/(2*(2*cos(2*f*x + 2*e) + 1)*cos(4*f*x + 4*e) + cos(4*f*x + 4*e)^2 + 4*cos(2*f*x + 2*e)^2 + sin(4*f*x + 4*e)^2 + 4*sin(4*f*x + 4*e)*sin(2*f*x + 2*e) + 4*sin(2*f*x + 2*e)^2 + 4*cos(2*f*x + 2*e) + 1), x) + I*integrate(-4*(2*(d*x + c)^m*a^2*cos(4*f*x + 4*e)*sin(2*f*x + 2*e) - (2*(d*x + c)^m*a^2*cos(2*f*x + 2*e) + (d*x + c)^m*a^2)*sin(4*f*x + 4*e))/(2*(2*cos(2*f*x + 2*e) + 1)*cos(4*f*x + 4*e) + cos(4*f*x + 4*e)^2 + 4*cos(2*f*x + 2*e)^2 + sin(4*f*x + 4*e)^2 + 4*sin(4*f*x + 4*e)*sin(2*f*x + 2*e) + 4*sin(2*f*x + 2*e)^2 + 4*cos(2*f*x + 2*e) + 1), x)

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int (a + a \tan(e + fx) i)^2 (c + dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + a*tan(e + f*x)*1i)^2*(c + d*x)^m,x)

[Out] int((a + a*tan(e + f*x)*1i)^2*(c + d*x)^m, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$-a^2 \left(\int (c + dx)^m \tan^2(e + fx) dx + \int (-2i(c + dx)^m \tan(e + fx)) dx + \int -(c + dx)^m dx \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**m*(a+I*a*tan(f*x+e))**2,x)

[Out] -a**2*(Integral((c + d*x)**m*tan(e + f*x)**2, x) + Integral(-2*I*(c + d*x)**m*tan(e + f*x), x) + Integral(-(c + d*x)**m, x))

3.35 $\int (c + dx)^m (a + ia \tan(e + fx)) dx$

Optimal. Leaf size=24

$$\text{Int}((c + dx)^m (a + ia \tan(e + fx)), x)$$

[Out] Unintegrable((d*x+c)^m*(a+I*a*tan(f*x+e)), x)

Rubi [A] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int (c + dx)^m (a + ia \tan(e + fx)) dx$$

Verification is Not applicable to the result.

[In] Int[(c + d*x)^m*(a + I*a*Tan[e + f*x]), x]

[Out] Defer[Int] [(c + d*x)^m*(a + I*a*Tan[e + f*x]), x]

Rubi steps

$$\int (c + dx)^m (a + ia \tan(e + fx)) dx = \int (c + dx)^m (a + ia \tan(e + fx)) dx$$

Mathematica [A] time = 15.61, size = 0, normalized size = 0.00

$$\int (c + dx)^m (a + ia \tan(e + fx)) dx$$

Verification is Not applicable to the result.

[In] Integrate[(c + d*x)^m*(a + I*a*Tan[e + f*x]), x]

[Out] Integrate[(c + d*x)^m*(a + I*a*Tan[e + f*x]), x]

fricas [A] time = 0.57, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{2(dx + c)^m a e^{(2i fx + 2ie)}}{e^{(2i fx + 2ie)} + 1}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m*(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] integral(2*(d*x + c)^m*a*e^(2*I*f*x + 2*I*e)/(e^(2*I*f*x + 2*I*e) + 1), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int (ia \tan(fx + e) + a)(dx + c)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m*(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] integrate((I*a*tan(f*x + e) + a)*(d*x + c)^m, x)

maple [A] time = 0.56, size = 0, normalized size = 0.00

$$\int (dx + c)^m (a + ia \tan(fx + e)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^m*(a+I*a*tan(f*x+e)),x)

[Out] int((d*x+c)^m*(a+I*a*tan(f*x+e)),x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$2ia \int \frac{(dx+c)^m \sin(2fx+2e)}{\cos(2fx+2e)^2 + \sin(2fx+2e)^2 + 2\cos(2fx+2e) + 1} dx + \frac{(dx+c)^{m+1}a}{d(m+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m*(a+I*a*tan(f*x+e)),x, algorithm="maxima")

[Out] 2*I*a*integrate((d*x + c)^m*sin(2*f*x + 2*e)/(cos(2*f*x + 2*e)^2 + sin(2*f*x + 2*e)^2 + 2*cos(2*f*x + 2*e) + 1), x) + (d*x + c)^(m + 1)*a/(d*(m + 1))

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int (a + a \tan(e + fx) 1i) (c + dx)^m dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + a*tan(e + f*x)*1i)*(c + d*x)^m,x)

[Out] int((a + a*tan(e + f*x)*1i)*(c + d*x)^m, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$ia \left(\int (-i(c + dx)^m) dx + \int (c + dx)^m \tan(e + fx) dx \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**m*(a+I*a*tan(f*x+e)),x)

[Out] I*a*(Integral(-I*(c + d*x)**m, x) + Integral((c + d*x)**m*tan(e + f*x), x))

$$3.36 \quad \int \frac{(c+dx)^m}{a+ia \tan(e+fx)} dx$$

Optimal. Leaf size=98

$$\frac{(c+dx)^{m+1}}{2ad(m+1)} + \frac{i2^{-m-2}e^{-2i\left(\frac{e-cf}{d}\right)}(c+dx)^m \left(\frac{if(c+dx)}{d}\right)^{-m} \Gamma\left(m+1, \frac{2if(c+dx)}{d}\right)}{af}$$

[Out] $1/2*(d*x+c)^{(1+m)}/a/d/(1+m)+I*2^{(-2-m)}*(d*x+c)^m*\text{GAMMA}(1+m,2*I*f*(d*x+c)/d)/a/\exp(2*I*(e-c*f/d))/f/((I*f*(d*x+c)/d)^m)$

Rubi [A] time = 0.12, antiderivative size = 98, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.087$, Rules used = {3727, 2181}

$$\frac{(c+dx)^{m+1}}{2ad(m+1)} + \frac{i2^{-m-2}e^{-2i\left(\frac{e-cf}{d}\right)}(c+dx)^m \left(\frac{if(c+dx)}{d}\right)^{-m} \text{Gamma}\left(m+1, \frac{2if(c+dx)}{d}\right)}{af}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^m/(a + I*a*Tan[e + f*x]), x]

[Out] $(c+d*x)^{(1+m)}/(2*a*d*(1+m)) + (I*2^{(-2-m)}*(c+d*x)^m*\text{Gamma}[1+m, ((2*I)*f*(c+d*x))/d])/(a*E^{((2*I)*(e-(c*f)/d)}*f*((I*f*(c+d*x))/d)^m)$

Rule 2181

Int[(F_)^((g_)*(e_) + (f_)*(x_))*((c_) + (d_)*(x_))^(m_), x_Symbol]
 :> -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, -(f*g*Log[F])/d]*(c + d*x)]/(d*(-(f*g*Log[F])/d)^(IntPart[m] + 1)*(-(f*g*Log[F])*(c + d*x)/d)^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !IntegerQ[m]

Rule 3727

Int[((c_) + (d_)*(x_))^(m_)/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol]
 :> Simp[(c + d*x)^(m + 1)/(2*a*d*(m + 1)), x] + Dist[1/(2*a), Int[(c + d*x)^m*E^((2*a*(e + f*x))/b), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[a^2 + b^2, 0] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^m}{a+ia \tan(e+fx)} dx &= \frac{(c+dx)^{1+m}}{2ad(1+m)} + \frac{\int e^{-2i(e+fx)}(c+dx)^m dx}{2a} \\ &= \frac{(c+dx)^{1+m}}{2ad(1+m)} + \frac{i2^{-2-m}e^{-2i\left(\frac{e-cf}{d}\right)}(c+dx)^m \left(\frac{if(c+dx)}{d}\right)^{-m} \Gamma\left(1+m, \frac{2if(c+dx)}{d}\right)}{af} \end{aligned}$$

Mathematica [B] time = 1.37, size = 205, normalized size = 2.09

$$\frac{2^{-m-2}(c+dx)^m \sec(e+fx) \left(-\frac{if(c+dx)}{d}\right)^m \left(\frac{f^2(c+dx)^2}{d^2}\right)^{-m} \left(\sin\left(f\left(\frac{c}{d}+x\right)\right) - i \cos\left(f\left(\frac{c}{d}+x\right)\right)\right) \left(f2^{m+1}(c+dx) \left(\frac{if(c+dx)}{d}\right)\right)}{adf(m+1)(\tan(e+fx))}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^m/(a + I*a*Tan[e + f*x]),x]

[Out] $(2^{-2-m})(c + dx)^m \left(\frac{(-I) f (c + dx)}{d} \right)^m \text{Sec}[e + fx] (2^{1+m} f (c + dx) \left(\frac{I f (c + dx)}{d} \right)^m (\cos[e - (cf)/d] + I \sin[e - (cf)/d]) + d (1+m) \Gamma[1+m, ((2I) f (c + dx))/d] (I \cos[e - (cf)/d] + \sin[e - (cf)/d]) \left(\frac{(-I) \cos[fx/d + x] + \sin[fx/d + x]}{a d f (1+m)} \right) \left(\frac{f^2 (c + dx)^2}{d^2} \right)^m (-I + \tan[e + fx])$

fricas [A] time = 0.46, size = 84, normalized size = 0.86

$$\frac{(idm + id)e^{\left(\frac{dm \log\left(\frac{2if}{d}\right) + 2ide - 2icf}{d} \right)} \Gamma\left(m + 1, \frac{2idfx + 2icf}{d}\right) + 2(df x + cf)(dx + c)^m}{4(adfm + adf)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e)),x, algorithm="fricas")

[Out] $1/4 * ((I*d*m + I*d) * e^{-(d*m*log(2*I*f/d) + 2*I*d*e - 2*I*c*f)/d} * \text{gamma}(m + 1, (2*I*d*f*x + 2*I*c*f)/d) + 2*(d*f*x + c*f)*(d*x + c)^m) / (a*d*f*m + a*d*f)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^m}{ia \tan(fx + e) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e)),x, algorithm="giac")

[Out] integrate((d*x + c)^m/(I*a*tan(f*x + e) + a), x)

maple [F] time = 0.83, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^m}{a + ia \tan(fx + e)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^m/(a+I*a*tan(f*x+e)),x)

[Out] int((d*x+c)^m/(a+I*a*tan(f*x+e)),x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{(dm + d) \int (dx + c)^m \cos(2fx + 2e) dx - (idm + id) \int (dx + c)^m \sin(2fx + 2e) dx + e^{(m \log(dx+c) + \log(dx+c))}}{2(adm + ad)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e)),x, algorithm="maxima")

[Out] $1/2 * ((d*m + d) * \text{integrate}((d*x + c)^m * \cos(2*f*x + 2*e), x) - (I*d*m + I*d) * \text{integrate}((d*x + c)^m * \sin(2*f*x + 2*e), x) + e^{(m * \log(d*x + c) + \log(d*x + c))}) / (a*d*m + a*d)$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^m}{a + a \tan(e + fx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((c + d*x)^m/(a + a*tan(e + f*x)*1i),x)`

[Out] `int((c + d*x)^m/(a + a*tan(e + f*x)*1i), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{i \int \frac{(c+dx)^m}{\tan(e+fx)-i} dx}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)**m/(a+I*a*tan(f*x+e)),x)`

[Out] `-I*Integral((c + d*x)**m/(tan(e + f*x) - I), x)/a`

$$3.37 \quad \int \frac{(c+dx)^m}{(a+ia \tan(e+fx))^2} dx$$

Optimal. Leaf size=171

$$\frac{i2^{-m-2}e^{-2i\left(\frac{e-cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(m+1,\frac{2if(c+dx)}{d}\right)}{a^2f} + \frac{i4^{-m-2}e^{-4i\left(\frac{e-cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(m+1,\frac{4if(c+dx)}{d}\right)}{a^2f}$$

[Out] 1/4*(d*x+c)^(1+m)/a^2/d/(1+m)+I*2^(-2-m)*(d*x+c)^m*GAMMA(1+m,2*I*f*(d*x+c)/d)/a^2/exp(2*I*(e-c*f/d))/f/((I*f*(d*x+c)/d)^m)+I*4^(-2-m)*(d*x+c)^m*GAMMA(1+m,4*I*f*(d*x+c)/d)/a^2/exp(4*I*(e-c*f/d))/f/((I*f*(d*x+c)/d)^m)

Rubi [A] time = 0.18, antiderivative size = 171, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.087$, Rules used = {3729, 2181}

$$\frac{i2^{-m-2}e^{-2i\left(\frac{e-cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(m+1,\frac{2if(c+dx)}{d}\right)}{a^2f} + \frac{i4^{-m-2}e^{-4i\left(\frac{e-cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(m+1,\frac{4if(c+dx)}{d}\right)}{a^2f}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^m/(a + I*a*Tan[e + f*x])^2,x]

[Out] (c + d*x)^(1 + m)/(4*a^2*d*(1 + m)) + (I*2^(-2 - m)*(c + d*x)^m*Gamma[1 + m, ((2*I)*f*(c + d*x))/d])/ (a^2*E^((2*I)*(e - (c*f)/d))*f*((I*f*(c + d*x))/d)^m) + (I*4^(-2 - m)*(c + d*x)^m*Gamma[1 + m, ((4*I)*f*(c + d*x))/d])/ (a^2*E^((4*I)*(e - (c*f)/d))*f*((I*f*(c + d*x))/d)^m)

Rule 2181

Int[(F_)^((g_.)*((e_.) + (f_.)*(x_)))*((c_.) + (d_.)*(x_))^(m_), x_Symbol] :> -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, (-((f*g*Log[F])/d))*(c + d*x])]/(d*(-((f*g*Log[F])/d))^(IntPart[m] + 1)*(-((f*g*Log[F])(c + d*x))/d)^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !IntegerQ[m]

Rule 3729

Int[((c_.) + (d_.)*(x_))^(m_)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] :> Int[ExpandIntegrand[(c + d*x)^m, (1/(2*a) + E^((2*a*(e + f*x))/b)/(2*a))^(-n), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[a^2 + b^2, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^m}{(a+ia \tan(e+fx))^2} dx &= \int \left(\frac{(c+dx)^m}{4a^2} + \frac{e^{-2ie-2ifx}(c+dx)^m}{2a^2} + \frac{e^{-4ie-4ifx}(c+dx)^m}{4a^2} \right) dx \\ &= \frac{(c+dx)^{1+m}}{4a^2d(1+m)} + \frac{\int e^{-4ie-4ifx}(c+dx)^m dx}{4a^2} + \frac{\int e^{-2ie-2ifx}(c+dx)^m dx}{2a^2} \\ &= \frac{(c+dx)^{1+m}}{4a^2d(1+m)} + \frac{i2^{-2-m}e^{-2i\left(\frac{e-cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(1+m,\frac{2if(c+dx)}{d}\right)}{a^2f} + \frac{i4^{-2-m}e^{-4i\left(\frac{e-cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(1+m,\frac{4if(c+dx)}{d}\right)}{a^2f} \end{aligned}$$

Mathematica [A] time = 48.07, size = 192, normalized size = 1.12

$$\frac{(c + dx)^m \sec^2(e + fx)(\cos(fx) + i \sin(fx))^2 \left(\frac{4e^{2ie} f(c+dx)}{d(m+1)} + i4^{-m} e^{\frac{4icf}{d} - 2ie} \left(\frac{if(c+dx)}{d} \right)^{-m} \Gamma\left(m + 1, \frac{4if(c+dx)}{d}\right) + i2^{2-m} e^{\frac{2icf}{d}} \right)}{16f(a + ia \tan(e + fx))^2}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^m/(a + I*a*Tan[e + f*x])^2, x]

[Out] ((c + d*x)^m*((4*E^((2*I)*e)*f*(c + d*x))/(d*(1 + m)) + (I*2^(2 - m)*E^(((2*I)*c*f)/d)*Gamma[1 + m, ((2*I)*f*(c + d*x))/d])/((I*f*(c + d*x))/d)^m + (I*E^((-2*I)*e + ((4*I)*c*f)/d)*Gamma[1 + m, ((4*I)*f*(c + d*x))/d])/(4^m*((I*f*(c + d*x))/d)^m)*Sec[e + f*x]^2*(Cos[f*x] + I*Sin[f*x])^2/(16*f*(a + I*a*Tan[e + f*x])^2)

fricas [A] time = 0.60, size = 140, normalized size = 0.82

$$\frac{(idm + id)e^{\left(-\frac{dm \log\left(\frac{4if}{d}\right) + 4ide - 4icf}{d}\right)} \Gamma\left(m + 1, \frac{4idfx + 4icf}{d}\right) + (4idm + 4id)e^{\left(-\frac{dm \log\left(\frac{2if}{d}\right) + 2ide - 2icf}{d}\right)} \Gamma\left(m + 1, \frac{2idfx + 2icf}{d}\right) + 4}{16(a^2dfm + a^2df)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e))^2,x, algorithm="fricas")

[Out] 1/16*((I*d*m + I*d)*e^(-(d*m*log(4*I*f/d) + 4*I*d*e - 4*I*c*f)/d)*gamma(m + 1, (4*I*d*f*x + 4*I*c*f)/d) + (4*I*d*m + 4*I*d)*e^(-(d*m*log(2*I*f/d) + 2*I*d*e - 2*I*c*f)/d)*gamma(m + 1, (2*I*d*f*x + 2*I*c*f)/d) + 4*(d*f*x + c*f)*(d*x + c)^m)/(a^2*d*f*m + a^2*d*f)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^m}{(ia \tan(fx + e) + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate((d*x + c)^m/(I*a*tan(f*x + e) + a)^2, x)

maple [F] time = 0.91, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^m}{(a + ia \tan(fx + e))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^m/(a+I*a*tan(f*x+e))^2,x)

[Out] int((d*x+c)^m/(a+I*a*tan(f*x+e))^2,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{(dm + d) \int (dx + c)^m \cos(4fx + 4e) dx + 2(dm + d) \int (dx + c)^m \cos(2fx + 2e) dx - (idm + id) \int (dx + c)^m \sec^2(e + fx) dx}{4(a^2dm + a^2d)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e))^2,x, algorithm="maxima")

[Out] 1/4*((d*m + d)*integrate((d*x + c)^m*cos(4*f*x + 4*e), x) + 2*(d*m + d)*integrate((d*x + c)^m*cos(2*f*x + 2*e), x) - (I*d*m + I*d)*integrate((d*x + c)^m*sin(4*f*x + 4*e), x) - (2*I*d*m + 2*I*d)*integrate((d*x + c)^m*sin(2*f*x + 2*e), x) + e^(m*log(d*x + c) + log(d*x + c)))/(a^2*d*m + a^2*d)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^m}{(a + a \tan(e + fx) i)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^m/(a + a*tan(e + f*x)*1i)^2,x)

[Out] int((c + d*x)^m/(a + a*tan(e + f*x)*1i)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{\int \frac{(c+dx)^m}{\tan^2(e+fx)-2i \tan(e+fx)-1} dx}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**m/(a+I*a*tan(f*x+e))**2,x)

[Out] -Integral((c + d*x)**m/(tan(e + f*x)**2 - 2*I*tan(e + f*x) - 1), x)/a**2

$$3.38 \quad \int \frac{(c+dx)^m}{(a+ia \tan(e+fx))^3} dx$$

Optimal. Leaf size=251

$$\frac{3i2^{-m-4}e^{-2i\left(\frac{cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(m+1,\frac{2if(c+dx)}{d}\right)}{a^3f} + \frac{3i2^{-2m-5}e^{-4i\left(\frac{cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(m+1,\frac{4if(c+dx)}{d}\right)}{a^3f}$$

[Out] $1/8*(d*x+c)^{(1+m)}/a^3/d/(1+m)+3*I*2^{(-4-m)}*(d*x+c)^m*\text{GAMMA}(1+m,2*I*f*(d*x+c)/d)/a^3/\exp(2*I*(e-c*f/d))/f/((I*f*(d*x+c)/d)^m)+3*I*2^{(-5-2*m)}*(d*x+c)^m*\text{GAMMA}(1+m,4*I*f*(d*x+c)/d)/a^3/\exp(4*I*(e-c*f/d))/f/(((I*f*(d*x+c)/d)^m)+I*2^{(-4-m)}*3^{(-1-m)}*(d*x+c)^m*\text{GAMMA}(1+m,6*I*f*(d*x+c)/d)/a^3/\exp(6*I*(e-c*f/d))/f/((I*f*(d*x+c)/d)^m)$

Rubi [A] time = 0.24, antiderivative size = 251, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 2, integrand size = 23, $\frac{\text{number of rules}}{\text{integrand size}} = 0.087$, Rules used = {3729, 2181}

$$\frac{3i2^{-m-4}e^{-2i\left(\frac{cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\text{Gamma}\left(m+1,\frac{2if(c+dx)}{d}\right)}{a^3f} + \frac{3i2^{-2m-5}e^{-4i\left(\frac{cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\text{Gamma}\left(m+1,\frac{4if(c+dx)}{d}\right)}{a^3f}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^m/(a + I*a*Tan[e + f*x])^3,x]

[Out] $(c+d*x)^{(1+m)}/(8*a^3*d*(1+m)) + ((3*I)*2^{(-4-m)}*(c+d*x)^m*\text{Gamma}[1+m,((2*I)*f*(c+d*x))/d])/(a^3*E^{((2*I)*(e-(c*f)/d))*f*((I*f*(c+d*x))/d)^m}) + ((3*I)*2^{(-5-2*m)}*(c+d*x)^m*\text{Gamma}[1+m,((4*I)*f*(c+d*x))/d])/(a^3*E^{((4*I)*(e-(c*f)/d))*f*((I*f*(c+d*x))/d)^m}) + (I*2^{(-4-m)}*3^{(-1-m)}*(c+d*x)^m*\text{Gamma}[1+m,((6*I)*f*(c+d*x))/d])/(a^3*E^{((6*I)*(e-(c*f)/d))*f*((I*f*(c+d*x))/d)^m})$

Rule 2181

Int[(F_)^((g_)*((e_)+(f_)*(x_)))*((c_)+(d_)*(x_))^(m_), x_Symbol] :> -Simp[(F^(g*(e-(c*f)/d))*(c+d*x)^FracPart[m]*Gamma[m+1,(-(f*g*Log[F])/d)*(c+d*x])/(d*(-(f*g*Log[F])/d))^(IntPart[m]+1)*(-(f*g*Log[F])*(c+d*x)/d)^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !IntegerQ[m]

Rule 3729

Int[((c_)+(d_)*(x_))^(m_)*((a_)+(b_)*tan[(e_)+(f_)*(x_)])^(n_), x_Symbol] :> Int[ExpandIntegrand[(c+d*x)^m, (1/(2*a)+E^((2*a*(e+f*x))/b)/(2*a))^(n), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[a^2+b^2, 0] && ILtQ[n, 0]

Rubi steps

$$\begin{aligned} \int \frac{(c+dx)^m}{(a+ia \tan(e+fx))^3} dx &= \int \left(\frac{(c+dx)^m}{8a^3} + \frac{3e^{-2ie-2ifx}(c+dx)^m}{8a^3} + \frac{3e^{-4ie-4ifx}(c+dx)^m}{8a^3} + \frac{e^{-6ie-6ifx}(c+dx)^m}{8a^3} \right) dx \\ &= \frac{(c+dx)^{1+m}}{8a^3d(1+m)} + \frac{\int e^{-6ie-6ifx}(c+dx)^m dx}{8a^3} + \frac{3 \int e^{-2ie-2ifx}(c+dx)^m dx}{8a^3} + \frac{3 \int e^{-4ie-4ifx}(c+dx)^m dx}{8a^3} \\ &= \frac{(c+dx)^{1+m}}{8a^3d(1+m)} + \frac{3i2^{-4-m}e^{-2i\left(\frac{cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(1+m,\frac{2if(c+dx)}{d}\right)}{a^3f} + \frac{3i2^{-5-m}e^{-4i\left(\frac{cf}{d}\right)}(c+dx)^m\left(\frac{if(c+dx)}{d}\right)^{-m}\Gamma\left(1+m,\frac{4if(c+dx)}{d}\right)}{a^3f} \end{aligned}$$

Mathematica [A] time = 68.70, size = 269, normalized size = 1.07

$$e^{-3ie}2^{-2m-5}3^{-m-1}(c+dx)^m \sec^3(e+fx)(\cos(fx)+i\sin(fx))^3 \left(\frac{if(c+dx)}{d}\right)^{-m} \left(e^{6ie}f12^{m+1}(c+dx)\left(\frac{if(c+dx)}{d}\right)^m + id\right)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^m/(a + I*a*Tan[e + f*x])^3,x]

[Out] (2^(-5 - 2*m)*3^(-1 - m)*(c + d*x)^m*(12^(1 + m)*E^((6*I)*e)*f*(c + d*x)*((I*f*(c + d*x))/d)^m + I*2^(1 + m)*3^(2 + m)*d*E^((2*I)*(2*e + (c*f)/d))*(1 + m)*Gamma[1 + m, ((2*I)*f*(c + d*x))/d] + I*3^(2 + m)*d*E^((2*I)*e + ((4*I)*c*f)/d)*(1 + m)*Gamma[1 + m, ((4*I)*f*(c + d*x))/d] + I*2^(1 + m)*d*E^(((6*I)*c*f)/d)*(1 + m)*Gamma[1 + m, ((6*I)*f*(c + d*x))/d])*Sec[e + f*x]^3*(Cos[f*x] + I*Sin[f*x])^3)/(d*E^((3*I)*e)*f*(1 + m)*((I*f*(c + d*x))/d)^m*(a + I*a*Tan[e + f*x])^3)

fricas [A] time = 0.62, size = 192, normalized size = 0.76

$$(2idm + 2id)e^{\left(-\frac{dm \log\left(\frac{6if}{d}\right) + 6ide - 6icf}{d}\right)} \Gamma\left(m + 1, \frac{6idfx + 6icf}{d}\right) + (9idm + 9id)e^{\left(-\frac{dm \log\left(\frac{4if}{d}\right) + 4ide - 4icf}{d}\right)} \Gamma\left(m + 1, \frac{4idfx + 4icf}{d}\right)$$

$$96(a^3dfm + a^3df)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e))^3,x, algorithm="fricas")

[Out] 1/96*((2*I*d*m + 2*I*d)*e^(-(d*m*log(6*I*f/d) + 6*I*d*e - 6*I*c*f)/d)*gamma(m + 1, (6*I*d*f*x + 6*I*c*f)/d) + (9*I*d*m + 9*I*d)*e^(-(d*m*log(4*I*f/d) + 4*I*d*e - 4*I*c*f)/d)*gamma(m + 1, (4*I*d*f*x + 4*I*c*f)/d) + (18*I*d*m + 18*I*d)*e^(-(d*m*log(2*I*f/d) + 2*I*d*e - 2*I*c*f)/d)*gamma(m + 1, (2*I*d*f*x + 2*I*c*f)/d) + 12*(d*f*x + c*f)*(d*x + c)^m)/(a^3*d*f*m + a^3*d*f)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^m}{(ia \tan(fx + e) + a)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e))^3,x, algorithm="giac")

[Out] integrate((d*x + c)^m/(I*a*tan(f*x + e) + a)^3, x)

maple [F] time = 1.03, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^m}{(a + ia \tan(fx + e))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^m/(a+I*a*tan(f*x+e))^3,x)

[Out] int((d*x+c)^m/(a+I*a*tan(f*x+e))^3,x)

maxima [F] time = 0.00, size = 0, normalized size = 0.00

$$(dm + d) \int (dx + c)^m \cos(6fx + 6e) dx + 3(dm + d) \int (dx + c)^m \cos(4fx + 4e) dx + 3(dm + d) \int (dx + c)^m$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^m/(a+I*a*tan(f*x+e))^3,x, algorithm="maxima")

[Out] 1/8*((d*m + d)*integrate((d*x + c)^m*cos(6*f*x + 6*e), x) + 3*(d*m + d)*integrate((d*x + c)^m*cos(4*f*x + 4*e), x) + 3*(d*m + d)*integrate((d*x + c)^m*cos(2*f*x + 2*e), x) - (I*d*m + I*d)*integrate((d*x + c)^m*sin(6*f*x + 6*e), x) - (3*I*d*m + 3*I*d)*integrate((d*x + c)^m*sin(4*f*x + 4*e), x) - (3*I*d*m + 3*I*d)*integrate((d*x + c)^m*sin(2*f*x + 2*e), x) + e^(m*log(d*x + c) + log(d*x + c)))/(a^3*d*m + a^3*d)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^m}{(a + a \tan(e + fx) i)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^m/(a + a*tan(e + f*x)*1i)^3,x)

[Out] int((c + d*x)^m/(a + a*tan(e + f*x)*1i)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\frac{i \int \frac{(c+dx)^m}{\tan^3(e+fx)-3i \tan^2(e+fx)-3 \tan(e+fx)+i} dx}{a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**m/(a+I*a*tan(f*x+e))**3,x)

[Out] I*Integral((c + d*x)**m/(tan(e + f*x)**3 - 3*I*tan(e + f*x)**2 - 3*tan(e + f*x) + I), x)/a**3

3.39 $\int (c + dx)^3 (a + b \tan(e + fx)) dx$

Optimal. Leaf size=152

$$\frac{a(c + dx)^4}{4d} - \frac{3bd^2(c + dx)\text{Li}_3(-e^{2i(e+fx)})}{2f^3} + \frac{3ibd(c + dx)^2\text{Li}_2(-e^{2i(e+fx)})}{2f^2} - \frac{b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{ib(c + d}{4d}$$

[Out] $1/4*a*(d*x+c)^4/d+1/4*I*b*(d*x+c)^4/d-b*(d*x+c)^3*\ln(1+\exp(2*I*(f*x+e)))/f+3/2*I*b*d*(d*x+c)^2*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^2-3/2*b*d^2*(d*x+c)*\text{polylog}(3,-\exp(2*I*(f*x+e)))/f^3-3/4*I*b*d^3*\text{polylog}(4,-\exp(2*I*(f*x+e)))/f^4$

Rubi [A] time = 0.25, antiderivative size = 152, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 7, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.389$, Rules used = {3722, 3719, 2190, 2531, 6609, 2282, 6589}

$$\frac{a(c + dx)^4}{4d} - \frac{3bd^2(c + dx)\text{Li}_3(-e^{2i(e+fx)})}{2f^3} + \frac{3ibd(c + dx)^2\text{Li}_2(-e^{2i(e+fx)})}{2f^2} - \frac{b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{ib(c + d}{4d}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^3*(a + b*\text{Tan}[e + f*x]), x]$

[Out] $(a*(c + d*x)^4)/(4*d) + ((I/4)*b*(c + d*x)^4)/d - (b*(c + d*x)^3*\text{Log}[1 + E^((2*I)*(e + f*x))])/f + (((3*I)/2)*b*d*(c + d*x)^2*\text{PolyLog}[2, -E^((2*I)*(e + f*x))])/f^2 - (3*b*d^2*(c + d*x)*\text{PolyLog}[3, -E^((2*I)*(e + f*x))])/(2*f^3) - (((3*I)/4)*b*d^3*\text{PolyLog}[4, -E^((2*I)*(e + f*x))])/f^4$

Rule 2190

$\text{Int}[(F_1)^{((g_1)*(e_1) + (f_1)*(x_1))} * ((c_1) + (d_1)*(x_1))^{(m_1)} / ((a_1) + (b_1)*(F_1)^{((g_1)*(e_1) + (f_1)*(x_1))} * ((c_1) + (d_1)*(x_1))^{(n_1)}), x_Symbol] := \text{Simp} [((c + d*x)^m*\text{Log}[1 + (b*(F^(g*(e + f*x)))^n)/a]) / (b*f*g*n*\text{Log}[F]), x] - \text{Dist} [(d*m) / (b*f*g*n*\text{Log}[F]), \text{Int} [(c + d*x)^{(m-1)}*\text{Log}[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /;$ FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2282

$\text{Int}[u, x_Symbol] := \text{With} [\{v = \text{FunctionOfExponential}[u, x]\}, \text{Dist}[v/D[v, x], \text{Subst}[\text{Int}[\text{FunctionOfExponentialFunction}[u, x]/x, x], x, v], x] /;$ FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_)+(b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2531

$\text{Int}[\text{Log}[1 + (e_1)*((F_1)^{((c_1)*((a_1) + (b_1)*(x_1)))})^{(n_1)}] * ((f_1) + (g_1)*(x_1))^{(m_1)}, x_Symbol] := -\text{Simp} [((f + g*x)^m*\text{PolyLog}[2, -(e*(F^(c*(a + b*x)))^n)])/ (b*c*n*\text{Log}[F]), x] + \text{Dist} [(g*m) / (b*c*n*\text{Log}[F]), \text{Int} [(f + g*x)^{(m-1)}*\text{PolyLog}[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /;$ FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

$\text{Int}[(c_1) + (d_1)*(x_1))^{(m_1)} * \text{tan}[(e_1) + (f_1)*(x_1)], x_Symbol] := \text{Simp} [(I*(c + d*x)^{(m+1)}) / (d*(m+1)), x] - \text{Dist} [2*I, \text{Int} [(c + d*x)^m * E^(2*I*(e + f*x)) / (1 + E^(2*I*(e + f*x))), x], x] /;$ FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3722

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.)
, x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x],
x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6609

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)
)*(x_)))]^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p])/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned}
\int (c + dx)^3 (a + b \tan(e + fx)) dx &= \int (a(c + dx)^3 + b(c + dx)^3 \tan(e + fx)) dx \\
&= \frac{a(c + dx)^4}{4d} + b \int (c + dx)^3 \tan(e + fx) dx \\
&= \frac{a(c + dx)^4}{4d} + \frac{ib(c + dx)^4}{4d} - (2ib) \int \frac{e^{2i(e+fx)}(c + dx)^3}{1 + e^{2i(e+fx)}} dx \\
&= \frac{a(c + dx)^4}{4d} + \frac{ib(c + dx)^4}{4d} - \frac{b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{(3bd) \int (c + dx)^2 \log(1 + e^{2i(e+fx)}) dx}{2f^2} \\
&= \frac{a(c + dx)^4}{4d} + \frac{ib(c + dx)^4}{4d} - \frac{b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{3ibd(c + dx)^2 \text{Li}_2(-e^{2i(e+fx)})}{2f^2} \\
&= \frac{a(c + dx)^4}{4d} + \frac{ib(c + dx)^4}{4d} - \frac{b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{3ibd(c + dx)^2 \text{Li}_2(-e^{2i(e+fx)})}{2f^2} \\
&= \frac{a(c + dx)^4}{4d} + \frac{ib(c + dx)^4}{4d} - \frac{b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{3ibd(c + dx)^2 \text{Li}_2(-e^{2i(e+fx)})}{2f^2} \\
&= \frac{a(c + dx)^4}{4d} + \frac{ib(c + dx)^4}{4d} - \frac{b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{3ibd(c + dx)^2 \text{Li}_2(-e^{2i(e+fx)})}{2f^2}
\end{aligned}$$

Mathematica [A] time = 0.36, size = 255, normalized size = 1.68

$$\frac{1}{4} \left(4ac^3x + 6ac^2dx^2 + 4acd^2x^3 + ad^3x^4 - \frac{4bc^3 \log(\cos(e + fx))}{f} - \frac{12bc^2dx \log(1 + e^{2i(e+fx)})}{f} + 6ibc^2dx^2 - \frac{6bd^2(c + dx)^2 \text{Li}_2(-e^{2i(e+fx)})}{2f^2} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^3*(a + b*Tan[e + f*x]),x]
```

```
[Out] (4*a*c^3*x + 6*a*c^2*d*x^2 + (6*I)*b*c^2*d*x^2 + 4*a*c*d^2*x^3 + (4*I)*b*c*
d^2*x^3 + a*d^3*x^4 + I*b*d^3*x^4 - (12*b*c^2*d*x*Log[1 + E^((2*I)*(e + f*x
))])/f - (12*b*c*d^2*x^2*Log[1 + E^((2*I)*(e + f*x))])/f - (4*b*d^3*x^3*Log
[1 + E^((2*I)*(e + f*x))])/f - (4*b*c^3*Log[Cos[e + f*x]])/f + ((6*I)*b*d*(
c + d*x)^2*PolyLog[2, -E^((2*I)*(e + f*x))])/f^2 - (6*b*d^2*(c + d*x)*PolyL
og[3, -E^((2*I)*(e + f*x))])/f^3 - ((3*I)*b*d^3*PolyLog[4, -E^((2*I)*(e + f
*x))])/f^4)/4
```

fricas [C] time = 0.70, size = 498, normalized size = 3.28

$$2ad^3f^4x^4 + 8acd^2f^4x^3 + 12ac^2df^4x^2 + 8ac^3f^4x + 3ibd^3\text{polylog}\left(4, \frac{\tan(fx+e)^2 + 2i\tan(fx+e) - 1}{\tan(fx+e)^2 + 1}\right) - 3ibd^3\text{polylog}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3*(a+b*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/8*(2*a*d^3*f^4*x^4 + 8*a*c*d^2*f^4*x^3 + 12*a*c^2*d*f^4*x^2 + 8*a*c^3*f^4*x + 3*I*b*d^3*polylog(4, (tan(f*x + e)^2 + 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 3*I*b*d^3*polylog(4, (tan(f*x + e)^2 - 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) + (-6*I*b*d^3*f^2*x^2 - 12*I*b*c*d^2*f^2*x - 6*I*b*c^2*d*f^2)*dilog(2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) + (6*I*b*d^3*f^2*x^2 + 12*I*b*c*d^2*f^2*x + 6*I*b*c^2*d*f^2)*dilog(2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) - 4*(b*d^3*f^3*x^3 + 3*b*c*d^2*f^3*x^2 + 3*b*c^2*d*f^3*x + b*c^3*f^3)*log(-2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 4*(b*d^3*f^3*x^3 + 3*b*c*d^2*f^3*x^2 + 3*b*c^2*d*f^3*x + b*c^3*f^3)*log(-2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 6*(b*d^3*f*x + b*c*d^2*f)*polylog(3, (tan(f*x + e)^2 + 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 6*(b*d^3*f*x + b*c*d^2*f)*polylog(3, (tan(f*x + e)^2 - 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)))/f^4

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)^3 (b \tan(fx + e) + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3*(a+b*tan(f*x+e)),x, algorithm="giac")

[Out] integrate((d*x + c)^3*(b*tan(f*x + e) + a), x)

maple [B] time = 0.52, size = 481, normalized size = 3.16

$$\frac{3a^2c^2dx^2}{2} + acd^2x^3 - ibc^3x + \frac{ibd^3x^4}{4} + \frac{2bc^3 \ln(e^{i(fx+e)})}{f} - \frac{bc^3 \ln(e^{2i(fx+e)} + 1)}{f} + \frac{6ibc^2dex}{f} + \frac{3ibcd^2 \text{polylog}(2, -\exp(2I*(fx+e)))}{f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3*(a+b*tan(f*x+e)),x)

[Out] -I*b*c^3*x+3/2*a*c^2*d*x^2+I*b*c*d^2*x^3+a*c*d^2*x^3+1/4*I*b*d^3*x^4+2/f*b*c^3*ln(exp(I*(f*x+e)))-1/f*b*c^3*ln(exp(2*I*(f*x+e))+1)+6*I/f*b*c^2*d*e*x+3*I/f^2*b*c*d^2*polylog(2,-exp(2*I*(f*x+e)))*x-6*I/f^2*b*c*d^2*e^2*x+a*c^3*x+1/4*a*d^3*x^4-3/2/f^3*b*c*d^2*polylog(3,-exp(2*I*(f*x+e)))-2/f^4*b*d^3*e^3*ln(exp(I*(f*x+e)))-3/f*b*c*d^2*ln(exp(2*I*(f*x+e))+1)*x^2-3/f*b*c^2*d*ln(exp(2*I*(f*x+e))+1)*x-1/f*b*d^3*ln(exp(2*I*(f*x+e))+1)*x^3-6/f^2*b*c^2*d*e*ln(exp(I*(f*x+e)))+6/f^3*b*c*d^2*e^2*ln(exp(I*(f*x+e)))+3*I/f^2*b*c^2*d*e^2-4*I/f^3*b*c*d^2*e^3+2*I/f^3*b*d^3*e^3*x+3/2*I/f^2*b*d^3*polylog(2,-exp(2*I*(f*x+e)))*x^2+3/2*I/f^2*b*c^2*d*polylog(2,-exp(2*I*(f*x+e)))+3/2*I*b*c^2*d*x^2+3/2*I/f^4*b*d^3*e^4*d^3-3/2/f^3*b*d^3*polylog(3,-exp(2*I*(f*x+e)))*x-3/4*I*b*d^3*polylog(4,-exp(2*I*(f*x+e)))/f^4

maxima [B] time = 3.41, size = 665, normalized size = 4.38

$$12(fx + e)ac^3 + \frac{3(fx+e)^4ad^3}{f^3} - \frac{12(fx+e)^3ad^3e}{f^3} + \frac{18(fx+e)^2ad^3e^2}{f^3} - \frac{12(fx+e)ad^3e^3}{f^3} + \frac{12(fx+e)^3acd^2}{f^2} - \frac{36(fx+e)^2acd^2e}{f^2} + \frac{36(fx+e)acd^2e^2}{f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3*(a+b*tan(f*x+e)),x, algorithm="maxima")

[Out] 1/12*(12*(f*x + e)*a*c^3 + 3*(f*x + e)^4*a*d^3/f^3 - 12*(f*x + e)^3*a*d^3*e/f^3 + 18*(f*x + e)^2*a*d^3*e^2/f^3 - 12*(f*x + e)*a*d^3*e^3/f^3 + 12*(f*x + e)^3*a*c*d^2/f^2 - 36*(f*x + e)^2*a*c*d^2*e/f^2 + 36*(f*x + e)*a*c*d^2*e^2/f^2 + 18*(f*x + e)^2*a*c^2*d/f - 36*(f*x + e)*a*c^2*d*e/f + 12*b*c^3*log(sec(f*x + e)) - 12*b*d^3*e^3*log(sec(f*x + e))/f^3 + 36*b*c*d^2*e^2*log(sec(f*x + e))/f^2 - 36*b*c^2*d*e*log(sec(f*x + e))/f - (-3*I*(f*x + e)^4*b*d^3 + 12*I*b*d^3*polylog(4, -e^(2*I*f*x + 2*I*e)) + (12*I*b*d^3*e - 12*I*b*c*d^2*f)*(f*x + e)^3 + (-18*I*b*d^3*e^2 + 36*I*b*c*d^2*e*f - 18*I*b*c^2*d*f^2)*(f*x + e)^2 + (16*I*(f*x + e)^3*b*d^3 + (-36*I*b*d^3*e + 36*I*b*c*d^2*f)*(f*x + e)^2 + (36*I*b*d^3*e^2 - 72*I*b*c*d^2*e*f + 36*I*b*c^2*d*f^2)*(f*x + e))*arctan2(sin(2*f*x + 2*e), cos(2*f*x + 2*e) + 1) + (-24*I*(f*x + e)^2*b*d^3 - 18*I*b*d^3*e^2 + 36*I*b*c*d^2*e*f - 18*I*b*c^2*d*f^2 + (36*I*b*d^3*e - 36*I*b*c*d^2*f)*(f*x + e))*dilog(-e^(2*I*f*x + 2*I*e)) + 2*(4*(f*x + e)^3*b*d^3 - 9*(b*d^3*e - b*c*d^2*f)*(f*x + e)^2 + 9*(b*d^3*e^2 - 2*b*c*d^2*e*f + b*c^2*d*f^2)*(f*x + e))*log(cos(2*f*x + 2*e)^2 + sin(2*f*x + 2*e)^2 + 2*cos(2*f*x + 2*e) + 1) + 6*(4*(f*x + e)*b*d^3 - 3*b*d^3*e + 3*b*c*d^2*f)*polylog(3, -e^(2*I*f*x + 2*I*e)))/f^3)/f

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + b \tan(e + f x)) (c + d x)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))*(c + d*x)^3,x)

[Out] int((a + b*tan(e + f*x))*(c + d*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + f x)) (c + d x)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3*(a+b*tan(f*x+e)),x)

[Out] Integral((a + b*tan(e + f*x))*(c + d*x)**3, x)

3.40 $\int (c + dx)^2 (a + b \tan(e + fx)) dx$

Optimal. Leaf size=115

$$\frac{a(c + dx)^3}{3d} + \frac{ibd(c + dx)\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{ib(c + dx)^3}{3d} - \frac{bd^2\text{Li}_3(-e^{2i(e+fx)})}{2f^3}$$

[Out] $1/3*a*(d*x+c)^3/d+1/3*I*b*(d*x+c)^3/d-b*(d*x+c)^2*\ln(1+\exp(2*I*(f*x+e)))/f+I*b*d*(d*x+c)*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^2-1/2*b*d^2*\text{polylog}(3,-\exp(2*I*(f*x+e)))/f^3$

Rubi [A] time = 0.21, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {3722, 3719, 2190, 2531, 2282, 6589}

$$\frac{a(c + dx)^3}{3d} + \frac{ibd(c + dx)\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{ib(c + dx)^3}{3d} - \frac{bd^2\text{Li}_3(-e^{2i(e+fx)})}{2f^3}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2*(a + b*Tan[e + f*x]), x]

[Out] $(a*(c + d*x)^3)/(3*d) + ((I/3)*b*(c + d*x)^3)/d - (b*(c + d*x)^2*\text{Log}[1 + E^{((2*I)*(e + f*x))}])/f + (I*b*d*(c + d*x)*\text{PolyLog}[2, -E^{((2*I)*(e + f*x))}])/f^2 - (b*d^2*\text{PolyLog}[3, -E^{((2*I)*(e + f*x))}])/(2*f^3)$

Rule 2190

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m-1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2531

Int[Log[1 + (e_)*((F_)^(c_)*((a_) + (b_)*(x_)))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] := -Simp[(((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m-1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

Int[(((c_) + (d_)*(x_))^(m_))*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m+1))/(d*(m+1)), x] - Dist[2*I, Int[(c + d*x)^m*E^(2*I*(e + f*x))]/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3722

Int[(((c_) + (d_)*(x_))^(m_))*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x],

x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rule 6589

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned}
 \int (c + dx)^2(a + b \tan(e + fx)) dx &= \int (a(c + dx)^2 + b(c + dx)^2 \tan(e + fx)) dx \\
 &= \frac{a(c + dx)^3}{3d} + b \int (c + dx)^2 \tan(e + fx) dx \\
 &= \frac{a(c + dx)^3}{3d} + \frac{ib(c + dx)^3}{3d} - (2ib) \int \frac{e^{2i(e+fx)}(c + dx)^2}{1 + e^{2i(e+fx)}} dx \\
 &= \frac{a(c + dx)^3}{3d} + \frac{ib(c + dx)^3}{3d} - \frac{b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{(2bd) \int (c + dx) \log(1 + e^{2i(e+fx)}) dx}{f^2} \\
 &= \frac{a(c + dx)^3}{3d} + \frac{ib(c + dx)^3}{3d} - \frac{b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{ibd(c + dx) \text{Li}_2(-e^{2i(e+fx)})}{f^2} \\
 &= \frac{a(c + dx)^3}{3d} + \frac{ib(c + dx)^3}{3d} - \frac{b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{ibd(c + dx) \text{Li}_2(-e^{2i(e+fx)})}{f^2} \\
 &= \frac{a(c + dx)^3}{3d} + \frac{ib(c + dx)^3}{3d} - \frac{b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{ibd(c + dx) \text{Li}_2(-e^{2i(e+fx)})}{f^2}
 \end{aligned}$$

Mathematica [A] time = 0.13, size = 191, normalized size = 1.66

$$ac^2x + acdx^2 + \frac{1}{3}ad^2x^3 - \frac{bc^2 \log(\cos(e + fx))}{f} + \frac{ibcd \text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{2bcdx \log(1 + e^{2i(e+fx)})}{f} + ibcdx^2 - \frac{bd^2 \text{Li}_3(-e^{2i(e+fx)})}{2f^3}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2*(a + b*Tan[e + f*x]), x]

[Out] a*c^2*x + a*c*d*x^2 + I*b*c*d*x^2 + (a*d^2*x^3)/3 + (I/3)*b*d^2*x^3 - (2*b*c*d*x*Log[1 + E^((2*I)*(e + f*x))])/f - (b*d^2*x^2*Log[1 + E^((2*I)*(e + f*x))])/f - (b*c^2*Log[Cos[e + f*x]])/f + (I*b*c*d*PolyLog[2, -E^((2*I)*(e + f*x))])/f^2 + (I*b*d^2*x*PolyLog[2, -E^((2*I)*(e + f*x))])/f^2 - (b*d^2*PolyLog[3, -E^((2*I)*(e + f*x))])/f^3

fricas [C] time = 0.56, size = 315, normalized size = 2.74

$$4ad^2f^3x^3 + 12acdf^3x^2 + 12ac^2f^3x - 3bd^2 \text{polylog}\left(3, \frac{\tan(fx+e)^2 + 2i \tan(fx+e) - 1}{\tan(fx+e)^2 + 1}\right) - 3bd^2 \text{polylog}\left(3, \frac{\tan(fx+e)^2 - 2i \tan(fx+e) - 1}{\tan(fx+e)^2 + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2*(a+b*tan(f*x+e)), x, algorithm="fricas")

[Out] 1/12*(4*a*d^2*f^3*x^3 + 12*a*c*d*f^3*x^2 + 12*a*c^2*f^3*x - 3*b*d^2*polylog(3, (tan(f*x + e)^2 + 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 3*b*d^2*polylog(3, (tan(f*x + e)^2 - 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) + (-6*I*b*d^2*f*x - 6*I*b*c*d*f)*dilog(2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1))

$2 + 1) + 1) + (6*I*b*d^2*f*x + 6*I*b*c*d*f)*dilog(2*(-I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1) + 1) - 6*(b*d^2*f^2*x^2 + 2*b*c*d*f^2*x + b*c^2*f^2)*\log(-2*(I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)) - 6*(b*d^2*f^2*x^2 + 2*b*c*d*f^2*x + b*c^2*f^2)*\log(-2*(-I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)))/f^3$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)^2 (b \tan (fx + e) + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2*(a+b*tan(f*x+e)),x, algorithm="giac")

[Out] integrate((d*x + c)^2*(b*tan(f*x + e) + a), x)

maple [B] time = 0.43, size = 295, normalized size = 2.57

$$\frac{ibcd \operatorname{polylog}\left(2, -e^{2i(fx+e)}\right)}{f^2} + \frac{ib d^2 x^3}{3} + \frac{a d^2 x^3}{3} + ibcd x^2 + acd x^2 + a c^2 x - \frac{b c^2 \ln\left(e^{2i(fx+e)} + 1\right)}{f} + \frac{2 b c^2 \ln\left(e^{i(fx+e)}\right)}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2*(a+b*tan(f*x+e)),x)

[Out] $\frac{1}{3}I*b*d^2*x^3 + I/f^2*b*c*d*\operatorname{polylog}(2, -\exp(2*I*(f*x+e))) + \frac{1}{3}a*d^2*x^3 + I/f^2*b*d^2*\operatorname{polylog}(2, -\exp(2*I*(f*x+e)))*x + a*c*d*x^2 + a*c^2*x - 1/f*b*c^2*\ln(\exp(2*I*(f*x+e))+1) + 2/f*b*c^2*\ln(\exp(I*(f*x+e))) + 2/f^3*b*d^2*e^2*\ln(\exp(I*(f*x+e))) + I*b*c*d*x^2 - 2*I/f^2*b*d^2*e^2*x + 2*I/f^2*b*c*d*e^2 - 1/f*b*d^2*\ln(\exp(2*I*(f*x+e))+1)*x^2 - 4/3*I/f^3*b*d^2*e^3 - 1/2*b*d^2*\operatorname{polylog}(3, -\exp(2*I*(f*x+e)))/f^3 - 4/f^2*b*c*d*e*\ln(\exp(I*(f*x+e))) - I*b*c^2*x + 4*I/f*b*c*d*e*x - 2/f*b*c*d*\ln(\exp(2*I*(f*x+e))+1)*x$

maxima [B] time = 1.23, size = 369, normalized size = 3.21

$$\frac{6(fx + e)ac^2 + \frac{2(fx+e)^3 ad^2}{f^2} - \frac{6(fx+e)^2 ad^2 e}{f^2} + \frac{6(fx+e) ad^2 e^2}{f^2} + \frac{6(fx+e)^2 acd}{f} - \frac{12(fx+e) acde}{f} + 6bc^2 \log(\sec(fx + e))}{f^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2*(a+b*tan(f*x+e)),x, algorithm="maxima")

[Out] $\frac{1}{6}(6*(f*x + e)*a*c^2 + 2*(f*x + e)^3*a*d^2/f^2 - 6*(f*x + e)^2*a*d^2*e/f^2 + 6*(f*x + e)*a*d^2*e^2/f^2 + 6*(f*x + e)^2*a*c*d/f - 12*(f*x + e)*a*c*d*e/f + 6*b*c^2*\log(\sec(f*x + e)) + 6*b*d^2*e^2*\log(\sec(f*x + e))/f^2 - 12*b*c*d*e*\log(\sec(f*x + e))/f - (-2*I*(f*x + e)^3*b*d^2 + 3*b*d^2*\operatorname{polylog}(3, -e^{(2*I*f*x + 2*I*e)}) + (6*I*b*d^2*e - 6*I*b*c*d*f)*(f*x + e)^2 + (6*I*(f*x + e)^2*b*d^2 + (-12*I*b*d^2*e + 12*I*b*c*d*f)*(f*x + e))*\arctan2(\sin(2*f*x + 2*e), \cos(2*f*x + 2*e) + 1) + (-6*I*(f*x + e)*b*d^2 + 6*I*b*d^2*e - 6*I*b*c*d*f)*dilog(-e^{(2*I*f*x + 2*I*e)}) + 3*((f*x + e)^2*b*d^2 - 2*(b*d^2*e - b*c*d*f)*(f*x + e))*\log(\cos(2*f*x + 2*e)^2 + \sin(2*f*x + 2*e)^2 + 2*\cos(2*f*x + 2*e) + 1))/f^2)/f$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + b \tan (e + fx)) (c + dx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*tan(e + f*x))*(c + d*x)^2,x)
```

```
[Out] int((a + b*tan(e + f*x))*(c + d*x)^2, x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + fx))(c + dx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2*(a+b*tan(f*x+e)),x)
```

```
[Out] Integral((a + b*tan(e + f*x))*(c + d*x)**2, x)
```

3.41 $\int (c + dx)(a + b \tan(e + fx)) dx$

Optimal. Leaf size=84

$$\frac{a(c + dx)^2}{2d} - \frac{b(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{ib(c + dx)^2}{2d} + \frac{ibd \operatorname{Li}_2(-e^{2i(e+fx)})}{2f^2}$$

[Out] $1/2*a*(d*x+c)^2/d+1/2*I*b*(d*x+c)^2/d-b*(d*x+c)*\ln(1+\exp(2*I*(f*x+e)))/f+1/2*I*b*d*\operatorname{polylog}(2,-\exp(2*I*(f*x+e)))/f^2$

Rubi [A] time = 0.12, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.312$, Rules used = {3722, 3719, 2190, 2279, 2391}

$$\frac{a(c + dx)^2}{2d} - \frac{b(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{ib(c + dx)^2}{2d} + \frac{ibd \operatorname{Li}_2(-e^{2i(e+fx)})}{2f^2}$$

Antiderivative was successfully verified.

[In] `Int[(c + d*x)*(a + b*Tan[e + f*x]),x]`

[Out] $(a*(c + d*x)^2)/(2*d) + ((I/2)*b*(c + d*x)^2)/d - (b*(c + d*x)*\operatorname{Log}[1 + E^{((2*I)*(e + f*x))}])/f + ((I/2)*b*d*\operatorname{PolyLog}[2, -E^{((2*I)*(e + f*x))}])/f^2$

Rule 2190

`Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n]/a)/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n]/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]`

Rule 2279

`Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_))))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]`

Rule 2391

`Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]`

Rule 3719

`Int[(((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1)/(d*(m + 1)), x] - Dist[2*I, Int[(((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]`

Rule 3722

`Int[(((c_) + (d_)*(x_))^(m_)*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^(n_), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]`

Rubi steps

$$\begin{aligned}
\int (c + dx)(a + b \tan(e + fx)) dx &= \int (a(c + dx) + b(c + dx) \tan(e + fx)) dx \\
&= \frac{a(c + dx)^2}{2d} + b \int (c + dx) \tan(e + fx) dx \\
&= \frac{a(c + dx)^2}{2d} + \frac{ib(c + dx)^2}{2d} - (2ib) \int \frac{e^{2i(e+fx)}(c + dx)}{1 + e^{2i(e+fx)}} dx \\
&= \frac{a(c + dx)^2}{2d} + \frac{ib(c + dx)^2}{2d} - \frac{b(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{(bd) \int \log(1 + e^{2i(e+fx)})}{f} \\
&= \frac{a(c + dx)^2}{2d} + \frac{ib(c + dx)^2}{2d} - \frac{b(c + dx) \log(1 + e^{2i(e+fx)})}{f} - \frac{(ibd) \operatorname{Subst}\left(\int \frac{\log(1+x)}{x}\right)}{2f^2} \\
&= \frac{a(c + dx)^2}{2d} + \frac{ib(c + dx)^2}{2d} - \frac{b(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{ibd \operatorname{Li}_2(-e^{2i(e+fx)})}{2f^2}
\end{aligned}$$

Mathematica [A] time = 0.02, size = 87, normalized size = 1.04

$$acx + \frac{1}{2}adx^2 - \frac{bc \log(\cos(e + fx))}{f} + \frac{ibd \operatorname{Li}_2(-e^{2i(e+fx)})}{2f^2} - \frac{bdx \log(1 + e^{2i(e+fx)})}{f} + \frac{1}{2}ibdx^2$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)*(a + b*Tan[e + f*x]),x]

[Out] a*c*x + (a*d*x^2)/2 + (I/2)*b*d*x^2 - (b*d*x*Log[1 + E^((2*I)*(e + f*x))])/f - (b*c*Log[Cos[e + f*x]])/f + ((I/2)*b*d*PolyLog[2, -E^((2*I)*(e + f*x))])/f^2

fricas [B] time = 0.55, size = 160, normalized size = 1.90

$$\frac{2ad^2x^2 + 4acf^2x - ibd \operatorname{Li}_2\left(\frac{2(i \tan(fx+e)-1)}{\tan(fx+e)^2+1} + 1\right) + ibd \operatorname{Li}_2\left(\frac{2(-i \tan(fx+e)-1)}{\tan(fx+e)^2+1} + 1\right) - 2(bdfx + bcf) \log\left(-\frac{2(i \tan(fx+e)-1)}{\tan(fx+e)^2+1}\right)}{4f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e)),x, algorithm="fricas")

[Out] 1/4*(2*a*d*f^2*x^2 + 4*a*c*f^2*x - I*b*d*dilog(2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) + I*b*d*dilog(2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) - 2*(b*d*f*x + b*c*f)*log(-2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 2*(b*d*f*x + b*c*f)*log(-2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)))/f^2

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)(b \tan(fx + e) + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e)),x, algorithm="giac")

[Out] integrate((d*x + c)*(b*tan(f*x + e) + a), x)

maple [A] time = 0.39, size = 143, normalized size = 1.70

$$\frac{ibd x^2}{2} - ibcx + \frac{ad x^2}{2} + cax - \frac{bc \ln(e^{2i(fx+e)} + 1)}{f} + \frac{2bc \ln(e^{i(fx+e)})}{f} + \frac{2ibdex}{f} + \frac{ibd e^2}{f^2} - \frac{bd \ln(e^{2i(fx+e)} + 1)x}{f} + \frac{ibd \operatorname{poly}}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x+c)*(a+b*tan(f*x+e)),x)`

[Out] $\frac{1}{2}I*b*d*x^2 - I*b*c*x + \frac{1}{2}a*d*x^2 + c*a*x - \frac{1}{f*b*c} \ln(\exp(2*I*(f*x+e))+1) + \frac{2}{f*b*c} \ln(\exp(I*(f*x+e))) + \frac{2*I}{f*b*d} e*x + \frac{I}{f^2*b*d} e^2 - \frac{1}{f*b*d} \ln(\exp(2*I*(f*x+e))+1)*x + \frac{1}{2}I*b*d*\text{polylog}(2, -\exp(2*I*(f*x+e)))/f^2 - \frac{2}{f^2*b*d} e*\ln(\exp(I*(f*x+e)))$

maxima [A] time = 0.75, size = 130, normalized size = 1.55

$$\frac{(a + ib)df^2x^2 + 2(a + ib)cf^2x + ibd\text{Li}_2\left(-e^{(2ifx+2ie)}\right) - (2ibdfx + 2ibcf) \arctan\left(\sin(2fx + 2e), \cos(2fx + 2e)\right)}{2f^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)*(a+b*tan(f*x+e)),x, algorithm="maxima")`

[Out] $\frac{1}{2}*((a + I*b)*d*f^2*x^2 + 2*(a + I*b)*c*f^2*x + I*b*d*\text{dilog}(-e^{(2*I*f*x + 2*I*e)}) - (2*I*b*d*f*x + 2*I*b*c*f)*\arctan2(\sin(2*f*x + 2*e), \cos(2*f*x + 2*e) + 1) - (b*d*f*x + b*c*f)*\log(\cos(2*f*x + 2*e)^2 + \sin(2*f*x + 2*e)^2 + 2*\cos(2*f*x + 2*e) + 1))/f^2$

mupad [B] time = 3.22, size = 161, normalized size = 1.92

$$\frac{ax(2c + dx)}{2} - \frac{bd(\pi \ln(\cos(fx)) - \pi \ln(e^{fx2i} + 1) + \text{polylog}(2, -e^{-e2i}e^{-fx2i})1i - \pi \ln(e^{-e2i}e^{-fx2i} + 1))}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*tan(e + f*x))*(c + d*x),x)`

[Out] $(a*x*(2*c + d*x))/2 - (b*d*(\text{polylog}(2, -\exp(-e*2i)*\exp(-f*x*2i))*1i - \pi*\log(\exp(f*x*2i) + 1) - \log(\cos(e + f*x))*(2*e - \pi) - \pi*\log(\exp(-e*2i)*\exp(-f*x*2i) + 1) + 2*e*\log(\exp(-e*2i)*\exp(-f*x*2i) + 1) + \pi*\log(\cos(f*x)) + f^2*x^2*1i + 2*f*x*\log(\exp(-e*2i)*\exp(-f*x*2i) + 1) + e*f*x*2i))/(2*f^2) + (b*c*\log(\tan(e + f*x)^2 + 1))/(2*f)$

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + fx))(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)*(a+b*tan(f*x+e)),x)`

[Out] `Integral((a + b*tan(e + f*x))*(c + d*x), x)`

$$3.42 \quad \int \frac{a+b \tan(e+fx)}{c+dx} dx$$

Optimal. Leaf size=21

$$\text{Int}\left(\frac{a+b \tan(e+fx)}{c+dx}, x\right)$$

[Out] Unintegrable((a+b*tan(f*x+e))/(d*x+c), x)

Rubi [A] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a+b \tan(e+fx)}{c+dx} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*Tan[e + f*x])/(c + d*x), x]

[Out] Defer[Int] [(a + b*Tan[e + f*x])/(c + d*x), x]

Rubi steps

$$\int \frac{a+b \tan(e+fx)}{c+dx} dx = \int \frac{a+b \tan(e+fx)}{c+dx} dx$$

Mathematica [A] time = 2.13, size = 0, normalized size = 0.00

$$\int \frac{a+b \tan(e+fx)}{c+dx} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*Tan[e + f*x])/(c + d*x), x]

[Out] Integrate[(a + b*Tan[e + f*x])/(c + d*x), x]

fricas [A] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{b \tan(fx+e)+a}{dx+c}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c), x, algorithm="fricas")

[Out] integral((b*tan(f*x + e) + a)/(d*x + c), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{b \tan(fx+e)+a}{dx+c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c), x, algorithm="giac")

[Out] integrate((b*tan(f*x + e) + a)/(d*x + c), x)

maple [A] time = 0.76, size = 0, normalized size = 0.00

$$\int \frac{a + b \tan(fx + e)}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*tan(f*x+e))/(d*x+c), x)

[Out] int((a+b*tan(f*x+e))/(d*x+c), x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\frac{2bd \int \frac{\sin(2fx+2e)}{(dx+c)(\cos(2fx+2e)^2 + \sin(2fx+2e)^2 + 2\cos(2fx+2e)+1)} dx + a \log(dx+c)}{d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c), x, algorithm="maxima")

[Out] (2*b*d*integrate(sin(2*f*x + 2*e)/((d*x + c)*cos(2*f*x + 2*e)^2 + (d*x + c)*sin(2*f*x + 2*e)^2 + d*x + 2*(d*x + c)*cos(2*f*x + 2*e) + c), x) + a*log(d*x + c))/d

mupad [A] time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{a + b \tan(e + fx)}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))/(c + d*x), x)

[Out] int((a + b*tan(e + f*x))/(c + d*x), x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{a + b \tan(e + fx)}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c), x)

[Out] Integral((a + b*tan(e + f*x))/(c + d*x), x)

$$3.43 \quad \int \frac{a+b \tan(e+fx)}{(c+dx)^2} dx$$

Optimal. Leaf size=21

$$\text{Int}\left(\frac{a+b \tan(e+fx)}{(c+dx)^2}, x\right)$$

[Out] Unintegrable((a+b*tan(f*x+e))/(d*x+c)^2,x)

Rubi [A] time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{a+b \tan(e+fx)}{(c+dx)^2} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*Tan[e + f*x])/(c + d*x)^2,x]

[Out] Defer[Int] [(a + b*Tan[e + f*x])/(c + d*x)^2, x]

Rubi steps

$$\int \frac{a+b \tan(e+fx)}{(c+dx)^2} dx = \int \frac{a+b \tan(e+fx)}{(c+dx)^2} dx$$

Mathematica [A] time = 6.14, size = 0, normalized size = 0.00

$$\int \frac{a+b \tan(e+fx)}{(c+dx)^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*Tan[e + f*x])/(c + d*x)^2,x]

[Out] Integrate[(a + b*Tan[e + f*x])/(c + d*x)^2, x]

fricas [A] time = 0.53, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{b \tan(fx + e) + a}{d^2x^2 + 2cdx + c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c)^2,x, algorithm="fricas")

[Out] integral((b*tan(f*x + e) + a)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{b \tan(fx + e) + a}{(dx + c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c)^2,x, algorithm="giac")

[Out] integrate((b*tan(f*x + e) + a)/(d*x + c)^2, x)

maple [A] time = 0.78, size = 0, normalized size = 0.00

$$\int \frac{a + b \tan(fx + e)}{(dx + c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*tan(f*x+e))/(d*x+c)^2,x)

[Out] int((a+b*tan(f*x+e))/(d*x+c)^2,x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$\frac{2(bd^2x + bcd) \int \frac{\sin(2fx+2e)}{(dx+c)^2(\cos(2fx+2e)^2 + \sin(2fx+2e)^2 + 2\cos(2fx+2e)+1)} dx - a}{d^2x + cd}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c)^2,x, algorithm="maxima")

[Out] (2*(b*d^2*x + b*c*d)*integrate(sin(2*f*x + 2*e)/(d^2*x^2 + 2*c*d*x + (d^2*x^2 + 2*c*d*x + c^2)*cos(2*f*x + 2*e)^2 + (d^2*x^2 + 2*c*d*x + c^2)*sin(2*f*x + 2*e)^2 + c^2 + 2*(d^2*x^2 + 2*c*d*x + c^2)*cos(2*f*x + 2*e)), x) - a)/(d^2*x + c*d)

mupad [A] time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{a + b \tan(e + fx)}{(c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))/(c + d*x)^2,x)

[Out] int((a + b*tan(e + f*x))/(c + d*x)^2, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{a + b \tan(e + fx)}{(c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))/(d*x+c)**2,x)

[Out] Integral((a + b*tan(e + f*x))/(c + d*x)**2, x)

3.44 $\int (c + dx)^3 (a + b \tan(e + fx))^2 dx$

Optimal. Leaf size=300

$$\frac{a^2(c + dx)^4}{4d} - \frac{3abd^2(c + dx)\text{Li}_3(-e^{2i(e+fx)})}{f^3} + \frac{3iabd(c + dx)^2\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{2ab(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{iab(c + dx)^4}{4d}$$

[Out] $-I*b^2*(d*x+c)^3/f+1/4*a^2*(d*x+c)^4/d+1/2*I*a*b*(d*x+c)^4/d-1/4*b^2*(d*x+c)^4/d+3*b^2*d*(d*x+c)^2*\ln(1+\exp(2*I*(f*x+e)))/f^2-2*a*b*(d*x+c)^3*\ln(1+\exp(2*I*(f*x+e)))/f-3*I*b^2*d^2*(d*x+c)*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^3+3*I*a*b*d*(d*x+c)^2*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^2+3/2*b^2*d^3*\text{polylog}(3,-\exp(2*I*(f*x+e)))/f^4-3*a*b*d^2*(d*x+c)*\text{polylog}(3,-\exp(2*I*(f*x+e)))/f^3-3/2*I*a*b*d^3*\text{polylog}(4,-\exp(2*I*(f*x+e)))/f^4+b^2*(d*x+c)^3*\tan(f*x+e)/f$

Rubi [A] time = 0.52, antiderivative size = 300, normalized size of antiderivative = 1.00, number of steps used = 15, number of rules used = 9, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.450$, Rules used = {3722, 3719, 2190, 2531, 6609, 2282, 6589, 3720, 32}

$$\frac{a^2(c + dx)^4}{4d} - \frac{3abd^2(c + dx)\text{Li}_3(-e^{2i(e+fx)})}{f^3} + \frac{3iabd(c + dx)^2\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{2ab(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{iab(c + dx)^4}{4d}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^3*(a + b*\text{Tan}[e + f*x])^2, x]$

[Out] $((-I)*b^2*(c + d*x)^3)/f + (a^2*(c + d*x)^4)/(4*d) + ((I/2)*a*b*(c + d*x)^4)/d - (b^2*(c + d*x)^4)/(4*d) + (3*b^2*d*(c + d*x)^2*\text{Log}[1 + E^((2*I)*(e + f*x))])/f^2 - (2*a*b*(c + d*x)^3*\text{Log}[1 + E^((2*I)*(e + f*x))])/f - ((3*I)*b^2*d^2*(c + d*x)*\text{PolyLog}[2, -E^((2*I)*(e + f*x))])/f^3 + ((3*I)*a*b*d*(c + d*x)^2*\text{PolyLog}[2, -E^((2*I)*(e + f*x))])/f^2 + (3*b^2*d^3*\text{PolyLog}[3, -E^((2*I)*(e + f*x))])/(2*f^4) - (3*a*b*d^2*(c + d*x)*\text{PolyLog}[3, -E^((2*I)*(e + f*x))])/f^3 - (((3*I)/2)*a*b*d^3*\text{PolyLog}[4, -E^((2*I)*(e + f*x))])/f^4 + (b^2*(c + d*x)^3*\text{Tan}[e + f*x])/f$

Rule 32

$\text{Int}[(a_. + (b_.)*(x_.))^(m_.), x_Symbol] \rightarrow \text{Simp}[(a + b*x)^(m + 1)/(b*(m + 1)), x] /;$ $\text{FreeQ}\{a, b, m, x\} \ \&\& \ \text{NeQ}[m, -1]$

Rule 2190

$\text{Int}[(F_)^(g_.)*((e_. + (f_.)*(x_.)))^(n_.)*((c_. + (d_.)*(x_.))^(m_.))/((a_. + (b_.)*(F_)^(g_.)*((e_. + (f_.)*(x_.))))^(n_.), x_Symbol] \rightarrow \text{Simp}[(c + d*x)^m*\text{Log}[1 + (b*(F^(g*(e + f*x)))^n)/a]/(b*f*g*n*\text{Log}[F]), x] - \text{Dist}[(d*m)/(b*f*g*n*\text{Log}[F]), \text{Int}[(c + d*x)^(m - 1)*\text{Log}[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /;$ $\text{FreeQ}\{F, a, b, c, d, e, f, g, n, x\} \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2282

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{FunctionOfExponential}[u, x], \text{Dist}[v/D[v, x], \text{Subst}[\text{Int}[\text{FunctionOfExponentialFunction}[u, x]/x, x], x, v], x]\} /;$ $\text{FunctionOfExponentialQ}[u, x] \ \&\& \ !\text{MatchQ}[u, (w_.)*((a_.)*(v_)^(n_.))^(m_.) /;$ $\text{FreeQ}\{a, m, n, x\} \ \&\& \ \text{IntegerQ}[m*n] \ \&\& \ !\text{MatchQ}[u, E^((c_.)*((a_.) + (b_.)*x))* (F_) [v_] /;$ $\text{FreeQ}\{a, b, c, x\} \ \&\& \ \text{InverseFunctionQ}[F[x]]$

Rule 2531

$\text{Int}[\text{Log}[1 + (e_.)*((F_)^(c_.)*((a_.) + (b_.)*(x_.)))]^(n_.)*((f_.) + (g_.)*(x_.))^(m_.), x_Symbol] \rightarrow -\text{Simp}[(f + g*x)^m*\text{PolyLog}[2, -(e*(F^(c*(a + b*x))))^n]/(b*c*n*\text{Log}[F]), x] + \text{Dist}[(g*m)/(b*c*n*\text{Log}[F]), \text{Int}[(f + g*x)^(m -$

1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

Int[((c_.) + (d_.)*(x_))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] := Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

Rule 3722

Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rule 6589

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6609

Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rubi steps

$$\begin{aligned}
\int (c + dx)^3 (a + b \tan(e + fx))^2 dx &= \int (a^2(c + dx)^3 + 2ab(c + dx)^3 \tan(e + fx) + b^2(c + dx)^3 \tan^2(e + fx)) dx \\
&= \frac{a^2(c + dx)^4}{4d} + (2ab) \int (c + dx)^3 \tan(e + fx) dx + b^2 \int (c + dx)^3 \tan^2(e + fx) dx \\
&= \frac{a^2(c + dx)^4}{4d} + \frac{iab(c + dx)^4}{2d} + \frac{b^2(c + dx)^3 \tan(e + fx)}{f} - (4iab) \int \frac{e^{2i(e+fx)}(c + dx)^3}{1 + e^{2i(e+fx)}} dx \\
&= -\frac{ib^2(c + dx)^3}{f} + \frac{a^2(c + dx)^4}{4d} + \frac{iab(c + dx)^4}{2d} - \frac{b^2(c + dx)^4}{4d} - \frac{2ab(c + dx)^3 \tan(e + fx)}{f} \\
&= -\frac{ib^2(c + dx)^3}{f} + \frac{a^2(c + dx)^4}{4d} + \frac{iab(c + dx)^4}{2d} - \frac{b^2(c + dx)^4}{4d} + \frac{3b^2d(c + dx)^2 \tan(e + fx)}{f} \\
&= -\frac{ib^2(c + dx)^3}{f} + \frac{a^2(c + dx)^4}{4d} + \frac{iab(c + dx)^4}{2d} - \frac{b^2(c + dx)^4}{4d} + \frac{3b^2d(c + dx)^2 \tan^2(e + fx)}{f} \\
&= -\frac{ib^2(c + dx)^3}{f} + \frac{a^2(c + dx)^4}{4d} + \frac{iab(c + dx)^4}{2d} - \frac{b^2(c + dx)^4}{4d} + \frac{3b^2d(c + dx)^2 \tan^3(e + fx)}{f} \\
&= -\frac{ib^2(c + dx)^3}{f} + \frac{a^2(c + dx)^4}{4d} + \frac{iab(c + dx)^4}{2d} - \frac{b^2(c + dx)^4}{4d} + \frac{3b^2d(c + dx)^2 \tan^4(e + fx)}{f}
\end{aligned}$$

Mathematica [B] time = 8.04, size = 1326, normalized size = 4.42

result too large to display

Warning: Unable to verify antiderivative.

[In] Integrate[(c + d*x)^3*(a + b*Tan[e + f*x])^2,x]

[Out] ((I/4)*b^2*d^3*(2*f^2*x^2*(2*f*x - (3*I)*(1 + E^((2*I)*e))*Log[1 + E^((-2*I)*(e + f*x))]) + 6*(1 + E^((2*I)*e))*f*x*PolyLog[2, -E^((-2*I)*(e + f*x))] - (3*I)*(1 + E^((2*I)*e))*PolyLog[3, -E^((-2*I)*(e + f*x))]*Sec[e])/(E^(I*e)*f^4) - ((I/2)*a*b*c*d^2*(2*f^2*x^2*(2*f*x - (3*I)*(1 + E^((2*I)*e))*Log[1 + E^((-2*I)*(e + f*x))]) + 6*(1 + E^((2*I)*e))*f*x*PolyLog[2, -E^((-2*I)*(e + f*x))] - (3*I)*(1 + E^((2*I)*e))*PolyLog[3, -E^((-2*I)*(e + f*x))]*Sec[e])/(E^(I*e)*f^3) - (I/4)*a*b*d^3*E^(I*e)*((2*x^4)/E^((2*I)*e) - ((4*I)*(1 + E^((-2*I)*e))*x^3*Log[1 + E^((-2*I)*(e + f*x))])/f + (3*(1 + E^((2*I)*e))*(2*f^2*x^2*PolyLog[2, -E^((-2*I)*(e + f*x))] - (2*I)*f*x*PolyLog[3, -E^((-2*I)*(e + f*x))]) - PolyLog[4, -E^((-2*I)*(e + f*x))]))/(E^((2*I)*e)*f^4) *Sec[e] + (3*b^2*c^2*d*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f^2*(Cos[e]^2 + Sin[e]^2)) - (2*a*b*c^3*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f*(Cos[e]^2 + Sin[e]^2)) + (3*b^2*c*d^2*Csc[e]*((f^2*x^2)/E^(I*ArcTan[Cot[e]]) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]]) - Pi*Log[1 + E^((-2*I)*f*x]) - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^((2*I)*(f*x - ArcTan[Cot[e]])])) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]])) + I*PolyLog[2, E^((2*I)*(f*x - ArcTan[Cot[e]])])))/Sqrt[1 + Cot[e]^2])*Sec[e])/(f^3*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2))) - (3*a*b*c^2*d*Csc[e]*((f^2*x^2)/E^(I*ArcTan[Cot[e]]) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]]) - Pi*Log[1 + E^((-2*I)*f*x]) - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^((2*I)*(f*x - ArcTan[Cot[e]])])) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]])) + I*PolyLog[2, E^((2*I)*(f*x - ArcTan[Cot[e]])])))/Sqrt[1 + Cot[e]^2])*Sec[e])/(f^2*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2))) + (Sec[e]*Sec[e + f*x]*(4*a^2*c^3*f*x*Cos[f*x] - 4*b^2*c^3*f*x*Cos[f*x] + 6*a^2*c^2*d*f*x^2*Cos[f*x] - 6*b^2*c^2*d*f*x^2*Cos[f*x] + 4*a^2*c*d^2*f*x^3*Cos[f*x] - 4*b^2*c*d^2*f*x^3*Cos[f*x] + a^2*d^3*f*x^4*Cos[f*x] - b^2*d^3*f*x^4*Cos[f*x] + 4*a^2*c^3*f*x*Cos[2*e + f*x] - 4*b^2*c^3*f*x*Cos[2*e + f*x] + 6*a^2*c^2*d*f*x^2*Cos[2*e + f*x] - 6*b^2*c^2*d*f*x

$$\begin{aligned} &^2 \cos[2e + fx] + 4a^2cd^2f^3 \cos[2e + fx] - 4b^2cd^2f^3 \cos[2e + fx] + a^2d^3f^4 \cos[2e + fx] - b^2d^3f^4 \cos[2e + fx] \\ &+ 8b^2c^3 \sin[fx] + 24b^2c^2d^2fx \sin[fx] - 8abc^3fx \sin[fx] + 24b^2cd^2x^2 \sin[fx] - 12abc^2d^2fx^2 \sin[fx] + 8b^2d^3x^3 \sin[fx] \\ &- 8abc^3d^2fx^3 \sin[fx] - 2abcd^3fx^4 \sin[fx] + 8abc^3fx^4 \sin[2e + fx] + 12abc^2d^2fx^2 \sin[2e + fx] + 8abcd^2fx^3 \sin[2e + fx] \\ &+ 2abcd^3fx^4 \sin[2e + fx] \end{aligned} \Big) / (8f)$$

fricas [C] time = 0.66, size = 757, normalized size = 2.52

$$(a^2 - b^2)d^3f^4x^4 + 4(a^2 - b^2)cd^2f^4x^3 + 6(a^2 - b^2)c^2df^4x^2 + 4(a^2 - b^2)c^3f^4x + 3abd^3 \operatorname{polylog}\left(4, \frac{\tan(fx+e)^2 + \tan(fx+e)}{\tan(fx+e)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((dx+c)^3*(a+b*tan(fx+e))^2,x, algorithm="fricas")

[Out] $\frac{1}{4}((a^2 - b^2)d^3f^4x^4 + 4(a^2 - b^2)cd^2f^4x^3 + 6(a^2 - b^2)c^2df^4x^2 + 4(a^2 - b^2)c^3f^4x + 3Iabcd^3 \operatorname{polylog}(4, (\tan(fx + e)^2 + 2I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1)) - 3Iabcd^3 \operatorname{polylog}(4, (\tan(fx + e)^2 - 2I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1)) + (-6Iabcd^3f^2x^2 - 6Iabcd^2d^2f^2 + 6Ib^2cd^2f - 6I(2abcd^2f^2 - b^2d^3f) * x) * \operatorname{dilog}(2(I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1) + 1) + (6Iabcd^3f^2x^2 + 6Iabcd^2d^2f^2 - 6Ib^2cd^2f + 6I(2abcd^2f^2 - b^2d^3f) * x) * \operatorname{dilog}(2(-I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1) + 1) - 2(2abcd^3f^3x^3 + 2abcd^3f^3 - 3b^2c^2d^2f^2 + 3(2abcd^2f^3 - b^2d^3f^2) * x^2 + 6(abc^2d^2f^3 - b^2cd^2f^2) * x) * \log(-2(I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1)) - 2(2abcd^3f^3x^3 + 2abcd^3f^3 - 3b^2c^2d^2f^2 + 3(2abcd^2f^3 - b^2d^3f^2) * x^2 + 6(abc^2d^2f^3 - b^2cd^2f^2) * x) * \log(-2(-I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1)) - 3(2abcd^3fx + 2abcd^2f - b^2d^3) * \operatorname{polylog}(3, (\tan(fx + e)^2 + 2I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1)) - 3(2abcd^3fx + 2abcd^2f - b^2d^3) * \operatorname{polylog}(3, (\tan(fx + e)^2 - 2I \tan(fx + e) - 1)/(\tan(fx + e)^2 + 1)) + 4(b^2d^3f^3x^3 + 3b^2cd^2f^3x^2 + 3b^2c^2d^2f^3x + b^2c^3f^3) * \tan(fx + e)) / f^4$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)^3 (b \tan(fx + e) + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((dx+c)^3*(a+b*tan(fx+e))^2,x, algorithm="giac")

[Out] integrate((dx + c)^3*(b*tan(fx + e) + a)^2, x)

maple [B] time = 0.82, size = 919, normalized size = 3.06

$$\frac{6b^2c d^2 \ln\left(e^{2i(fx+e)} + 1\right)x}{f^2} + \frac{12b^2c d^2 e \ln\left(e^{i(fx+e)}\right)}{f^3} - \frac{4ba d^3 e^3 \ln\left(e^{i(fx+e)}\right)}{f^4} - \frac{3ba d^3 \operatorname{polylog}\left(3, -e^{2i(fx+e)}\right)x}{f^3} - 3b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((dx+c)^3*(a+b*tan(fx+e))^2,x)

[Out] $a^2c^3x - b^2c^3x + a^2cd^2x^3 + 12I/f * abc^2d^2e * x + 6I/f^2 * abc^2d^2 * \operatorname{polylog}(2, -\exp(2I * (fx + e))) * x - 12I/f^2 * abc^2d^2e^2 * x + 2Ib^2 * (d^3x^3 + 3c^2d^2x^2 + 3c^2d^2 * x + c^3) / f / (\exp(2I * (fx + e)) + 1) - b^2cd^2x^3 + 3/2 * a^2c^2d^2 * x$

$$\begin{aligned} & -2-3/2*b^2*c^2*d*x^2-12/f^2*b*a*c^2*d*e*\ln(\exp(I*(f*x+e)))+12/f^3*b*a*c*d^2 \\ & *e^2*\ln(\exp(I*(f*x+e)))-12*I/f^2*b^2*c*d^2*e*x+4*I/f^3*b*a*d^3*e^3*x-8*I/f^ \\ & 3*b*a*c*d^2*e^3+3*I/f^2*b*a*c^2*d*polylog(2,-\exp(2*I*(f*x+e)))+3*I/f^2*b*a* \\ & d^3*polylog(2,-\exp(2*I*(f*x+e)))*x^2+6*I/f^2*b*a*c^2*d*e^2-6/f*b*a*c*d^2*\ln \\ & (\exp(2*I*(f*x+e))+1)*x^2-6/f*b*\ln(\exp(2*I*(f*x+e))+1)*a*c^2*d*x-2/f*b*a*d^3 \\ & *\ln(\exp(2*I*(f*x+e))+1)*x^3-2*I*a*b*c^3*x+1/2*I*a*b*d^3*x^4+1/4*a^2*d^3*x^4 \\ & -1/4*b^2*d^3*x^4-3/f^3*b*a*d^3*polylog(3,-\exp(2*I*(f*x+e)))*x+6/f^2*b^2*c*d \\ & ^2*\ln(\exp(2*I*(f*x+e))+1)*x+12/f^3*b^2*c*d^2*e*\ln(\exp(I*(f*x+e)))-4/f^4*b*a \\ & *d^3*e^3*\ln(\exp(I*(f*x+e)))-3/f^3*b*a*c*d^2*polylog(3,-\exp(2*I*(f*x+e)))+3/ \\ & f^2*b^2*d^3*\ln(\exp(2*I*(f*x+e))+1)*x^2+4/f*b*a*c^3*\ln(\exp(I*(f*x+e)))-6/f^2 \\ & *b^2*c^2*d*\ln(\exp(I*(f*x+e)))+3/f^2*b^2*c^2*d*\ln(\exp(2*I*(f*x+e))+1)-2/f*b* \\ & a*c^3*\ln(\exp(2*I*(f*x+e))+1)-6/f^4*b^2*d^3*e^2*\ln(\exp(I*(f*x+e)))-2*I/f*b^2 \\ & *d^3*x^3+4*I/f^4*b^2*d^3*e^3-3*I/f^3*b^2*c*d^2*polylog(2,-\exp(2*I*(f*x+e))) \\ & -3*I/f^3*b^2*d^3*polylog(2,-\exp(2*I*(f*x+e)))*x+3*I/f^4*b*a*d^3*e^4-6*I/f*b \\ & ^2*c*d^2*x^2-6*I/f^3*b^2*c*d^2*e^2+6*I/f^3*b^2*d^3*e^2*x+3/2*b^2*d^3*polylo \\ & g(3,-\exp(2*I*(f*x+e)))/f^4+3*I*a*b*c^2*d*x^2+2*I*a*b*c*d^2*x^3-3/2*I*a*b*d^ \\ & 3*polylog(4,-\exp(2*I*(f*x+e)))/f^4 \end{aligned}$$

maxima [B] time = 2.79, size = 2521, normalized size = 8.40

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3*(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out]
$$\begin{aligned} & 1/4*(4*(f*x + e)*a^2*c^3 + (f*x + e)^4*a^2*d^3/f^3 - 4*(f*x + e)^3*a^2*d^3* \\ & e/f^3 + 6*(f*x + e)^2*a^2*d^3*e^2/f^3 - 4*(f*x + e)*a^2*d^3*e^3/f^3 + 4*(f* \\ & x + e)^3*a^2*c*d^2/f^2 - 12*(f*x + e)^2*a^2*c*d^2*e/f^2 + 12*(f*x + e)*a^2* \\ & c*d^2*e^2/f^2 + 6*(f*x + e)^2*a^2*c^2*d/f - 12*(f*x + e)*a^2*c^2*d*e/f + 8* \\ & a*b*c^3*\log(\sec(f*x + e)) - 8*a*b*d^3*e^3*\log(\sec(f*x + e))/f^3 + 24*a*b*c* \\ & d^2*e^2*\log(\sec(f*x + e))/f^2 - 24*a*b*c^2*d*e*\log(\sec(f*x + e))/f + 4*(3*(\\ & 2*a*b + I*b^2)*(f*x + e)^4*d^3 - 24*b^2*d^3*e^3 + 72*b^2*c*d^2*e^2*f - 72*b \\ & ^2*c^2*d*e*f^2 + 24*b^2*c^3*f^3 - 12*((2*a*b + I*b^2)*d^3*e - (2*a*b + I*b^ \\ & 2)*c*d^2*f)*(f*x + e)^3 + 18*((2*a*b + I*b^2)*d^3*e^2 - 2*(2*a*b + I*b^2)*c \\ & *d^2*e*f + (2*a*b + I*b^2)*c^2*d*f^2)*(f*x + e)^2 - (12*I*b^2*d^3*e^3 - 36* \\ & I*b^2*c*d^2*e^2*f + 36*I*b^2*c^2*d*e*f^2 - 12*I*b^2*c^3*f^3)*(f*x + e) - (3 \\ & 2*(f*x + e)^3*a*b*d^3 - 36*b^2*d^3*e^2 + 72*b^2*c*d^2*e*f - 36*b^2*c^2*d*f^ \\ & 2 - 36*(2*a*b*d^3*e - 2*a*b*c*d^2*f + b^2*d^3)*(f*x + e)^2 + 72*(a*b*d^3*e^ \\ & 2 + a*b*c^2*d*f^2 + b^2*d^3*e - (2*a*b*c*d^2*e + b^2*c*d^2)*f)*(f*x + e) + \\ & 4*(8*(f*x + e)^3*a*b*d^3 - 9*b^2*d^3*e^2 + 18*b^2*c*d^2*e*f - 9*b^2*c^2*d*f \\ & ^2 - 9*(2*a*b*d^3*e - 2*a*b*c*d^2*f + b^2*d^3)*(f*x + e)^2 + 18*(a*b*d^3*e^ \\ & 2 + a*b*c^2*d*f^2 + b^2*d^3*e - (2*a*b*c*d^2*e + b^2*c*d^2)*f)*(f*x + e)*c \\ & os(2*f*x + 2*e) + (32*I*(f*x + e)^3*a*b*d^3 - 36*I*b^2*d^3*e^2 + 72*I*b^2*c \\ & *d^2*e*f - 36*I*b^2*c^2*d*f^2 + (-72*I*a*b*d^3*e + 72*I*a*b*c*d^2*f - 36*I* \\ & b^2*d^3)*(f*x + e)^2 + (72*I*a*b*d^3*e^2 + 72*I*a*b*c^2*d*f^2 + 72*I*b^2*d^ \\ & 3*e + (-144*I*a*b*c*d^2*e - 72*I*b^2*c*d^2)*f)*(f*x + e))*\sin(2*f*x + 2*e) \\ & *\arctan2(\sin(2*f*x + 2*e), \cos(2*f*x + 2*e) + 1) + (3*(2*a*b + I*b^2)*(f*x \\ & + e)^4*d^3 - 12*(2*b^2*d^3 + (2*a*b + I*b^2)*d^3*e - (2*a*b + I*b^2)*c*d^2* \\ & f)*(f*x + e)^3 + 18*(4*b^2*d^3*e + (2*a*b + I*b^2)*d^3*e^2 + (2*a*b + I*b^2 \\ &)*c^2*d*f^2 - 2*(2*b^2*c*d^2 + (2*a*b + I*b^2)*c*d^2*e)*f)*(f*x + e)^2 - (1 \\ & 2*I*b^2*d^3*e^3 - 12*I*b^2*c^3*f^3 + 72*b^2*d^3*e^2 - 36*(-I*b^2*c^2*d*e - \\ & 2*b^2*c^2*d)*f^2 + (-36*I*b^2*c*d^2*e^2 - 144*b^2*c*d^2*e)*f)*(f*x + e))*c \\ & os(2*f*x + 2*e) + (48*(f*x + e)^2*a*b*d^3 + 36*a*b*d^3*e^2 + 36*a*b*c^2*d*f^ \\ & 2 + 36*b^2*d^3*e - 36*(2*a*b*d^3*e - 2*a*b*c*d^2*f + b^2*d^3)*(f*x + e) - 3 \\ & 6*(2*a*b*c*d^2*e + b^2*c*d^2)*f + 12*(4*(f*x + e)^2*a*b*d^3 + 3*a*b*d^3*e^2 \\ & + 3*a*b*c^2*d*f^2 + 3*b^2*d^3*e - 3*(2*a*b*d^3*e - 2*a*b*c*d^2*f + b^2*d^3 \\ &)*(f*x + e) - 3*(2*a*b*c*d^2*e + b^2*c*d^2)*f)*\cos(2*f*x + 2*e) - (-48*I*(f \\ & *x + e)^2*a*b*d^3 - 36*I*a*b*d^3*e^2 - 36*I*a*b*c^2*d*f^2 - 36*I*b^2*d^3*e \\ & + (72*I*a*b*d^3*e - 72*I*a*b*c*d^2*f + 36*I*b^2*d^3)*(f*x + e) + (72*I*a*b* \\ & c*d^2*e + 36*I*b^2*c*d^2)*f)*\sin(2*f*x + 2*e))*\operatorname{dilog}(-e^(2*I*f*x + 2*I*e)) \end{aligned}$$

$$\begin{aligned}
& - (-16*I*(f*x + e)^3*a*b*d^3 + 18*I*b^2*d^3*e^2 - 36*I*b^2*c*d^2*e*f + 18*I \\
& *b^2*c^2*d*f^2 + (36*I*a*b*d^3*e - 36*I*a*b*c*d^2*f + 18*I*b^2*d^3)*(f*x + \\
& e)^2 + (-36*I*a*b*d^3*e^2 - 36*I*a*b*c^2*d*f^2 - 36*I*b^2*d^3*e + (72*I*a*b \\
& *c*d^2*e + 36*I*b^2*c*d^2)*f)*(f*x + e) + (-16*I*(f*x + e)^3*a*b*d^3 + 18*I \\
& *b^2*d^3*e^2 - 36*I*b^2*c*d^2*e*f + 18*I*b^2*c^2*d*f^2 + (36*I*a*b*d^3*e - \\
& 36*I*a*b*c*d^2*f + 18*I*b^2*d^3)*(f*x + e)^2 + (-36*I*a*b*d^3*e^2 - 36*I*a \\
& b*c^2*d*f^2 - 36*I*b^2*d^3*e + (72*I*a*b*c*d^2*e + 36*I*b^2*c*d^2)*f)*(f*x \\
& + e))*\cos(2*f*x + 2*e) + 2*(8*(f*x + e)^3*a*b*d^3 - 9*b^2*d^3*e^2 + 18*b^2 \\
& *c*d^2*e*f - 9*b^2*c^2*d*f^2 - 9*(2*a*b*d^3*e - 2*a*b*c*d^2*f + b^2*d^3)*(f* \\
& x + e)^2 + 18*(a*b*d^3*e^2 + a*b*c^2*d*f^2 + b^2*d^3*e - (2*a*b*c*d^2*e + b \\
& ^2*c*d^2)*f)*(f*x + e))*\sin(2*f*x + 2*e))*\log(\cos(2*f*x + 2*e)^2 + \sin(2*f* \\
& x + 2*e)^2 + 2*\cos(2*f*x + 2*e) + 1) - (24*a*b*d^3*\cos(2*f*x + 2*e) + 24*I* \\
& a*b*d^3*\sin(2*f*x + 2*e) + 24*a*b*d^3)*\text{polylog}(4, -e^{(2*I*f*x + 2*I*e)}) - (\\
& -48*I*(f*x + e)*a*b*d^3 + 36*I*a*b*d^3*e - 36*I*a*b*c*d^2*f + 18*I*b^2*d^3 \\
& + (-48*I*(f*x + e)*a*b*d^3 + 36*I*a*b*d^3*e - 36*I*a*b*c*d^2*f + 18*I*b^2*d \\
& ^3)*\cos(2*f*x + 2*e) + 6*(8*(f*x + e)*a*b*d^3 - 6*a*b*d^3*e + 6*a*b*c*d^2*f \\
& - 3*b^2*d^3)*\sin(2*f*x + 2*e))*\text{polylog}(3, -e^{(2*I*f*x + 2*I*e)}) - ((-6*I*a \\
& *b + 3*b^2)*(f*x + e)^4*d^3 + (24*I*b^2*d^3 + (24*I*a*b - 12*b^2)*d^3*e + (\\
& -24*I*a*b + 12*b^2)*c*d^2*f)*(f*x + e)^3 + (-72*I*b^2*d^3*e + (-36*I*a*b + \\
& 18*b^2)*d^3*e^2 + (-36*I*a*b + 18*b^2)*c^2*d*f^2 + (72*I*b^2*c*d^2 + (72*I* \\
& a*b - 36*b^2)*c*d^2*e)*f)*(f*x + e)^2 - (12*b^2*d^3*e^3 - 12*b^2*c^3*f^3 - \\
& 72*I*b^2*d^3*e^2 + (36*b^2*c^2*d*e - 72*I*b^2*c^2*d)*f^2 - 36*(b^2*c*d^2*e^ \\
& 2 - 4*I*b^2*c*d^2*e)*f)*(f*x + e))*\sin(2*f*x + 2*e))/(-12*I*f^3*\cos(2*f*x + \\
& 2*e) + 12*f^3*\sin(2*f*x + 2*e) - 12*I*f^3))/f
\end{aligned}$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + b \tan(e + f x))^2 (c + d x)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^2*(c + d*x)^3,x)

[Out] int((a + b*tan(e + f*x))^2*(c + d*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + f x))^2 (c + d x)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3*(a+b*tan(f*x+e))**2,x)

[Out] Integral((a + b*tan(e + f*x))**2*(c + d*x)**3, x)

3.45 $\int (c + dx)^2 (a + b \tan(e + fx))^2 dx$

Optimal. Leaf size=229

$$\frac{a^2(c + dx)^3}{3d} + \frac{2iabd(c + dx)\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{2ab(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{2iab(c + dx)^3}{3d} - \frac{abd^2\text{Li}_3(-e^{2i(e+fx)})}{f^3} +$$

[Out] $-I*b^2*(d*x+c)^2/f+1/3*a^2*(d*x+c)^3/d+2/3*I*a*b*(d*x+c)^3/d-1/3*b^2*(d*x+c)^3/d+2*b^2*d*(d*x+c)*\ln(1+\exp(2*I*(f*x+e)))/f^2-2*a*b*(d*x+c)^2*\ln(1+\exp(2*I*(f*x+e)))/f-I*b^2*d^2*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^3+2*I*a*b*d*(d*x+c)*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^2-a*b*d^2*\text{polylog}(3,-\exp(2*I*(f*x+e)))/f^3+b^2*(d*x+c)^2*\tan(f*x+e)/f$

Rubi [A] time = 0.41, antiderivative size = 229, normalized size of antiderivative = 1.00, number of steps used = 13, number of rules used = 10, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3722, 3719, 2190, 2531, 2282, 6589, 3720, 2279, 2391, 32}

$$\frac{a^2(c + dx)^3}{3d} + \frac{2iabd(c + dx)\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{2ab(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{2iab(c + dx)^3}{3d} - \frac{abd^2\text{Li}_3(-e^{2i(e+fx)})}{f^3} +$$

Antiderivative was successfully verified.

[In] $\text{Int}[(c + d*x)^2*(a + b*\text{Tan}[e + f*x])^2, x]$

[Out] $((-I)*b^2*(c + d*x)^2)/f + (a^2*(c + d*x)^3)/(3*d) + (((2*I)/3)*a*b*(c + d*x)^3)/d - (b^2*(c + d*x)^3)/(3*d) + (2*b^2*d*(c + d*x)*\text{Log}[1 + E^((2*I)*(e + f*x))])/f^2 - (2*a*b*(c + d*x)^2*\text{Log}[1 + E^((2*I)*(e + f*x))])/f - (I*b^2*d^2*\text{PolyLog}[2, -E^((2*I)*(e + f*x))])/f^3 + ((2*I)*a*b*d*(c + d*x)*\text{PolyLog}[2, -E^((2*I)*(e + f*x))])/f^2 - (a*b*d^2*\text{PolyLog}[3, -E^((2*I)*(e + f*x))])/f^3 + (b^2*(c + d*x)^2*\text{Tan}[e + f*x])/f$

Rule 32

$\text{Int}[(a_. + (b_.)*(x_.))^{(m_.)}, x_Symbol] \text{ :> } \text{Simp}[(a + b*x)^{(m + 1)}/(b*(m + 1)), x] \text{ /; } \text{FreeQ}\{a, b, m\}, x\} \ \&\& \ \text{NeQ}\{m, -1\}$

Rule 2190

$\text{Int}[(F_)^{((g_.)*((e_.) + (f_.)*(x_.)))^{(n_.)*((c_.) + (d_.)*(x_.))^{(m_.)}}/((a_.) + (b_.)*((F_)^{((g_.)*((e_.) + (f_.)*(x_.)))^{(n_.)}}), x_Symbol] \text{ :> } \text{Simp}[(c + d*x)^m*\text{Log}[1 + (b*(F^{(g*(e + f*x)))^n)/a]]/(b*f*g^n*\text{Log}[F]), x] - \text{Dist}[(d*m)/(b*f*g^n*\text{Log}[F]), \text{Int}[(c + d*x)^{(m - 1)}*\text{Log}[1 + (b*(F^{(g*(e + f*x)))^n)/a], x], x] \text{ /; } \text{FreeQ}\{F, a, b, c, d, e, f, g, n\}, x\} \ \&\& \ \text{IGtQ}\{m, 0\}$

Rule 2279

$\text{Int}[\text{Log}[(a_.) + (b_.)*((F_)^{((e_.)*((c_.) + (d_.)*(x_.)))^{(n_.)}}], x_Symbol] \text{ :> } \text{Dist}[1/(d*e^n*\text{Log}[F]), \text{Subst}[\text{Int}[\text{Log}[a + b*x]/x, x], x, (F^{(e*(c + d*x))})^n], x] \text{ /; } \text{FreeQ}\{F, a, b, c, d, e, n\}, x\} \ \&\& \ \text{GtQ}\{a, 0\}$

Rule 2282

$\text{Int}[u_, x_Symbol] \text{ :> } \text{With}\{v = \text{FunctionOfExponential}[u, x]\}, \text{Dist}[v/D[v, x], \text{Subst}[\text{Int}[\text{FunctionOfExponentialFunction}[u, x]/x, x], x, v], x] \text{ /; } \text{FunctionOfExponentialQ}[u, x] \ \&\& \ \text{!MatchQ}[u, (w_.)*((a_.)*(v_)^{(n_.)})^{(m_.)} \text{ /; } \text{FreeQ}\{a, m, n\}, x\} \ \&\& \ \text{IntegerQ}\{m*n\} \ \&\& \ \text{!MatchQ}[u, E^((c_.)*((a_.) + (b_.)*x))* (F_) [v_] \text{ /; } \text{FreeQ}\{a, b, c\}, x\} \ \&\& \ \text{InverseFunctionQ}[F[x]]]$

Rule 2391

Int[Log[(c_.)*((d_) + (e_.)*(x_)^(n_.))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 2531

Int[Log[1 + (e_.)*(F_)^((c_.)*((a_.) + (b_.)*(x_)))^(n_.)]*((f_.) + (g_.)*(x_)^(m_.), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

Int[((c_.) + (d_.)*(x_)^(m_.))*tan[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

Int[((c_.) + (d_.)*(x_)^(m_.))*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

Rule 3722

Int[((c_.) + (d_.)*(x_)^(m_.))*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rule 6589

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_)^(p_.))]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned}
\int (c + dx)^2 (a + b \tan(e + fx))^2 dx &= \int (a^2(c + dx)^2 + 2ab(c + dx)^2 \tan(e + fx) + b^2(c + dx)^2 \tan^2(e + fx)) dx \\
&= \frac{a^2(c + dx)^3}{3d} + (2ab) \int (c + dx)^2 \tan(e + fx) dx + b^2 \int (c + dx)^2 \tan^2(e + fx) dx \\
&= \frac{a^2(c + dx)^3}{3d} + \frac{2iab(c + dx)^3}{3d} + \frac{b^2(c + dx)^2 \tan(e + fx)}{f} - (4iab) \int \frac{e^{2i(e+fx)}(c + dx)^2}{1 + e^{2i(e+fx)}} dx \\
&= -\frac{ib^2(c + dx)^2}{f} + \frac{a^2(c + dx)^3}{3d} + \frac{2iab(c + dx)^3}{3d} - \frac{b^2(c + dx)^3}{3d} - \frac{2ab(c + dx)^2 \tan(e + fx)}{f} \\
&= -\frac{ib^2(c + dx)^2}{f} + \frac{a^2(c + dx)^3}{3d} + \frac{2iab(c + dx)^3}{3d} - \frac{b^2(c + dx)^3}{3d} + \frac{2b^2d(c + dx) \tan(e + fx)}{f} \\
&= -\frac{ib^2(c + dx)^2}{f} + \frac{a^2(c + dx)^3}{3d} + \frac{2iab(c + dx)^3}{3d} - \frac{b^2(c + dx)^3}{3d} + \frac{2b^2d(c + dx) \tan(e + fx)}{f} \\
&= -\frac{ib^2(c + dx)^2}{f} + \frac{a^2(c + dx)^3}{3d} + \frac{2iab(c + dx)^3}{3d} - \frac{b^2(c + dx)^3}{3d} + \frac{2b^2d(c + dx) \tan(e + fx)}{f}
\end{aligned}$$

Mathematica [B] time = 7.18, size = 649, normalized size = 2.83

$$\frac{1}{3} x \sec(e) (3c^2 + 3cdx + d^2x^2) (a^2 \cos(e) + 2ab \sin(e) - b^2 \cos(e)) - \frac{2abc^2 \sec(e)(fx \sin(e) + \cos(e) \log(\cos(e) \cos(fx)))}{f (\sin^2(e) + \cos^2(e))}$$

Warning: Unable to verify antiderivative.

[In] Integrate[(c + d*x)^2*(a + b*Tan[e + f*x])^2,x]

[Out] ((-1/6*I)*a*b*d^2*(2*f^2*x^2*(2*f*x - (3*I)*(1 + E^((2*I)*e))*Log[1 + E^((-2*I)*(e + f*x))]) + 6*(1 + E^((2*I)*e))*f*x*PolyLog[2, -E^((-2*I)*(e + f*x))] - (3*I)*(1 + E^((2*I)*e))*PolyLog[3, -E^((-2*I)*(e + f*x))])*Sec[e]/(E^(I*e)*f^3) + (x*(3*c^2 + 3*c*d*x + d^2*x^2)*Sec[e]*(a^2*Cos[e] - b^2*Cos[e] + 2*a*b*Sin[e]))/3 + (2*b^2*c*d*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f^2*(Cos[e]^2 + Sin[e]^2)) - (2*a*b*c^2*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f*(Cos[e]^2 + Sin[e]^2)) + (b^2*d^2*Csc[e]*((f^2*x^2)/E^(I*ArcTan[Cot[e]]) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]]) - Pi*Log[1 + E^((-2*I)*f*x]) - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^((2*I)*(f*x - ArcTan[Cot[e]])]) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]]]) + I*PolyLog[2, E^((2*I)*(f*x - ArcTan[Cot[e]])])))/Sqrt[1 + Cot[e]^2])*Sec[e]/(f^3*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2))) - (2*a*b*c*d*Csc[e]*((f^2*x^2)/E^(I*ArcTan[Cot[e]]) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]]) - Pi*Log[1 + E^((-2*I)*f*x]) - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^((2*I)*(f*x - ArcTan[Cot[e]])]) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]]]) + I*PolyLog[2, E^((2*I)*(f*x - ArcTan[Cot[e]])])))/Sqrt[1 + Cot[e]^2])*Sec[e]/(f^2*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2))) + (Sec[e]*Sec[e + f*x]*(b^2*c^2*Sin[f*x] + 2*b^2*c*d*x*Sin[f*x] + b^2*d^2*x^2*Sin[f*x]))/f

fricas [C] time = 0.50, size = 448, normalized size = 1.96

$$2(a^2 - b^2)d^2f^3x^3 + 6(a^2 - b^2)cdf^3x^2 + 6(a^2 - b^2)c^2f^3x - 3abd^2 \operatorname{polylog}\left(3, \frac{\tan(fx+e)^2 + 2i \tan(fx+e) - 1}{\tan(fx+e)^2 + 1}\right) - 3abd^2 \operatorname{polylog}\left(3, \frac{\tan(fx+e)^2 + 2i \tan(fx+e) - 1}{\tan(fx+e)^2 + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2*(a+b*tan(f*x+e))^2,x, algorithm="fricas")

[Out] $\frac{1}{6}*(2*(a^2 - b^2)*d^2*f^3*x^3 + 6*(a^2 - b^2)*c*d*f^3*x^2 + 6*(a^2 - b^2)*c^2*f^3*x - 3*a*b*d^2*polylog(3, (\tan(f*x + e))^2 + 2*I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)) - 3*a*b*d^2*polylog(3, (\tan(f*x + e))^2 - 2*I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)) + (-6*I*a*b*d^2*f*x - 6*I*a*b*c*d*f + 3*I*b^2*d^2)*dilog(2*(I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1) + 1) + (6*I*a*b*d^2*f*x + 6*I*a*b*c*d*f - 3*I*b^2*d^2)*dilog(2*(-I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1) + 1) - 6*(a*b*d^2*f^2*x^2 + a*b*c^2*f^2 - b^2*c*d*f + (2*a*b*c*d*f^2 - b^2*d^2*f)*x)*\log(-2*(I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)) - 6*(a*b*d^2*f^2*x^2 + a*b*c^2*f^2 - b^2*c*d*f + (2*a*b*c*d*f^2 - b^2*d^2*f)*x)*\log(-2*(-I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)) + 6*(b^2*d^2*f^2*x^2 + 2*b^2*c*d*f^2*x + b^2*c^2*f^2)*\tan(f*x + e))/f^3$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)^2 (b \tan(fx + e) + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2*(a+b*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate((d*x + c)^2*(b*tan(f*x + e) + a)^2, x)

maple [B] time = 0.68, size = 542, normalized size = 2.37

$$\frac{ib^2d^2 \operatorname{polylog}\left(2, -e^{2i(fx+e)}\right)}{f^3} - \frac{abd^2 \operatorname{polylog}\left(3, -e^{2i(fx+e)}\right)}{f^3} - b^2cdx^2 + a^2cdx^2 + \frac{8ibacdex}{f} + \frac{4bac^2 \ln\left(e^{i(fx+e)}\right)}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2*(a+b*tan(f*x+e))^2,x)

[Out] $-2*I*a*b*c^2*x + 2*I*b^2*(d^2*x^2 + 2*c*d*x + c^2)/f / (\exp(2*I*(f*x+e)) + 1) - b^2*c*d*x^2 + 4/f^3*b*a*d^2*e^2*\ln(\exp(I*(f*x+e))) + a^2*c*d*x^2 + 8*I/f*b*a*c*d*e*x - 8/f^2*b*a*c*d*e*\ln(\exp(I*(f*x+e))) - 4/f*b*\ln(\exp(2*I*(f*x+e)) + 1)*a*c*d*x + 2*I/f^2*b*a*c*d*polylog(2, -\exp(2*I*(f*x+e))) + 4*I/f^2*b*a*c*d*e^2 - 4*I/f^2*b*a*d^2*e^2*x + 2*I/f^2*b*a*d^2*polylog(2, -\exp(2*I*(f*x+e))) * x - 2*I/f*b^2*d^2*x^2 - 2*I/f^3*b^2*d^2*e^2 - 2/f*b*a*c^2*\ln(\exp(2*I*(f*x+e)) + 1) + 4/f*b*a*c^2*\ln(\exp(I*(f*x+e))) + 2/f^2*b^2*c*d*\ln(\exp(2*I*(f*x+e)) + 1) - 4/f^2*b^2*c*d*\ln(\exp(I*(f*x+e))) + 2/f^2*b^2*d^2*\ln(\exp(2*I*(f*x+e)) + 1)*x + 2/3*I*a*b*d^2*x^3 - I*b^2*d^2*polylog(2, -\exp(2*I*(f*x+e)))/f^3 + 4/f^3*b^2*d^2*e*\ln(\exp(I*(f*x+e))) - 2/f*b*a*d^2*\ln(\exp(2*I*(f*x+e)) + 1)*x^2 - b^2*c^2*x + 1/3*a^2*d^2*x^3 - 1/3*b^2*d^2*x^3 + a^2*c^2*x + 2*I*a*b*c*d*x^2 - 4*I/f^2*b^2*d^2*e*x - 8/3*I/f^3*b*a*d^2*e^3 - a*b*d^2*polylog(3, -\exp(2*I*(f*x+e)))/f^3$

maxima [B] time = 1.29, size = 1269, normalized size = 5.54

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2*(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out] $\frac{1}{3}*(3*(f*x + e)*a^2*c^2 + (f*x + e)^3*a^2*d^2/f^2 - 3*(f*x + e)^2*a^2*d^2*e/f^2 + 3*(f*x + e)*a^2*d^2*e^2/f^2 + 3*(f*x + e)^2*a^2*c*d/f - 6*(f*x + e)*a^2*c*d*e/f + 6*a*b*c^2*\log(\sec(f*x + e)) + 6*a*b*d^2*e^2*\log(\sec(f*x + e))/f^2 - 12*a*b*c*d*e*\log(\sec(f*x + e))/f + 3*((2*a*b + I*b^2)*(f*x + e)^3*d^2 + 6*b^2*d^2*e^2 - 12*b^2*c*d*e*f + 6*b^2*c^2*f^2 - 3*((2*a*b + I*b^2)*d^2*e - (2*a*b + I*b^2)*c*d*f)*(f*x + e)^2 - (-3*I*b^2*d^2*e^2 + 6*I*b^2*c*d$

```

e*f - 3*I*b^2*c^2*f^2)*(f*x + e) - (6*(f*x + e)^2*a*b*d^2 + 6*b^2*d^2*e - 6
*b^2*c*d*f - 6*(2*a*b*d^2*e - 2*a*b*c*d*f + b^2*d^2)*(f*x + e) + 6*((f*x +
e)^2*a*b*d^2 + b^2*d^2*e - b^2*c*d*f - (2*a*b*d^2*e - 2*a*b*c*d*f + b^2*d^2
)*(f*x + e))*cos(2*f*x + 2*e) + (6*I*(f*x + e)^2*a*b*d^2 + 6*I*b^2*d^2*e -
6*I*b^2*c*d*f + (-12*I*a*b*d^2*e + 12*I*a*b*c*d*f - 6*I*b^2*d^2)*(f*x + e))
*sin(2*f*x + 2*e))*arctan2(sin(2*f*x + 2*e), cos(2*f*x + 2*e) + 1) + ((2*a*
b + I*b^2)*(f*x + e)^3*d^2 - 3*(2*b^2*d^2 + (2*a*b + I*b^2)*d^2*e - (2*a*b
+ I*b^2)*c*d*f)*(f*x + e)^2 - (-3*I*b^2*d^2*e^2 - 3*I*b^2*c^2*f^2 - 12*b^2*
d^2*e - 6*(-I*b^2*c*d*e - 2*b^2*c*d)*f)*(f*x + e))*cos(2*f*x + 2*e) + (6*(f
*x + e)*a*b*d^2 - 6*a*b*d^2*e + 6*a*b*c*d*f - 3*b^2*d^2 + 3*(2*(f*x + e)*a*
b*d^2 - 2*a*b*d^2*e + 2*a*b*c*d*f - b^2*d^2)*cos(2*f*x + 2*e) - (-6*I*(f*x
+ e)*a*b*d^2 + 6*I*a*b*d^2*e - 6*I*a*b*c*d*f + 3*I*b^2*d^2)*sin(2*f*x + 2*e
))*dilog(-e^(2*I*f*x + 2*I*e)) - (-3*I*(f*x + e)^2*a*b*d^2 - 3*I*b^2*d^2*e
+ 3*I*b^2*c*d*f + (6*I*a*b*d^2*e - 6*I*a*b*c*d*f + 3*I*b^2*d^2)*(f*x + e) +
(-3*I*(f*x + e)^2*a*b*d^2 - 3*I*b^2*d^2*e + 3*I*b^2*c*d*f + (6*I*a*b*d^2*e
- 6*I*a*b*c*d*f + 3*I*b^2*d^2)*(f*x + e))*cos(2*f*x + 2*e) + 3*((f*x + e)^
2*a*b*d^2 + b^2*d^2*e - b^2*c*d*f - (2*a*b*d^2*e - 2*a*b*c*d*f + b^2*d^2)*(
f*x + e))*sin(2*f*x + 2*e))*log(cos(2*f*x + 2*e)^2 + sin(2*f*x + 2*e)^2 + 2
*cos(2*f*x + 2*e) + 1) - (-3*I*a*b*d^2*cos(2*f*x + 2*e) + 3*a*b*d^2*sin(2*f
*x + 2*e) - 3*I*a*b*d^2)*polylog(3, -e^(2*I*f*x + 2*I*e)) - ((-2*I*a*b + b^
2)*(f*x + e)^3*d^2 + (6*I*b^2*d^2 + (6*I*a*b - 3*b^2)*d^2*e + (-6*I*a*b + 3
*b^2)*c*d*f)*(f*x + e)^2 + (3*b^2*d^2*e^2 + 3*b^2*c^2*f^2 - 12*I*b^2*d^2*e
- (6*b^2*c*d*e - 12*I*b^2*c*d)*f)*(f*x + e))*sin(2*f*x + 2*e))/(-3*I*f^2*co
s(2*f*x + 2*e) + 3*f^2*sin(2*f*x + 2*e) - 3*I*f^2))/f

```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + b \tan(e + f x))^2 (c + d x)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^2*(c + d*x)^2,x)

[Out] int((a + b*tan(e + f*x))^2*(c + d*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + f x))^2 (c + d x)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2*(a+b*tan(f*x+e))**2,x)

[Out] Integral((a + b*tan(e + f*x))**2*(c + d*x)**2, x)

3.46 $\int (c + dx)(a + b \tan(e + fx))^2 dx$

Optimal. Leaf size=136

$$\frac{a^2(c + dx)^2}{2d} - \frac{2ab(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{iab(c + dx)^2}{d} + \frac{iabd \operatorname{Li}_2(-e^{2i(e+fx)})}{f^2} + \frac{b^2(c + dx) \tan(e + fx)}{f} - b^2cx + \dots$$

[Out] $-b^2cx - 1/2b^2dx^2 + 1/2a^2(dx+c)^2/d + Iab(dx+c)^2/d - 2ab(dx+c) \ln(1+\exp(2I*(fx+e)))/f + b^2d \ln(\cos(fx+e))/f^2 + Iabdx \operatorname{polylog}(2, -\exp(2I*(fx+e)))/f^2 + b^2(dx+c) \tan(fx+e)/f$

Rubi [A] time = 0.19, antiderivative size = 136, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 7, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.389$, Rules used = {3722, 3719, 2190, 2279, 2391, 3720, 3475}

$$\frac{a^2(c + dx)^2}{2d} - \frac{2ab(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{iab(c + dx)^2}{d} + \frac{iabd \operatorname{Li}_2(-e^{2i(e+fx)})}{f^2} + \frac{b^2(c + dx) \tan(e + fx)}{f} - b^2cx + \dots$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)*(a + b*Tan[e + f*x])^2, x]

[Out] $-(b^2cx) - (b^2dx^2)/2 + (a^2(c + dx)^2)/(2d) + (Iab(dx+c)^2)/d - (2ab(dx+c) \operatorname{Log}[1 + E^((2I)(e + fx))])/f + (b^2d \operatorname{Log}[\operatorname{Cos}[e + fx]])/f^2 + (Iabd \operatorname{PolyLog}[2, -E^((2I)(e + fx))])/f^2 + (b^2(dx+c) \operatorname{Tan}[e + fx])/f$

Rule 2190

Int[(((F_)^(g_)*(e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^(g_)*(e_) + (f_)*(x_)))^(n_), x_Symbol] := Simp[((c + d*x)^m * Log[1 + (b*(F^(g*(e + f*x)))^n)/a]) / (b*f*g*n * Log[F]), x] - Dist[(d*m) / (b*f*g*n * Log[F]), Int[(c + d*x)^(m-1) * Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_)*((F_)^(e_)*((c_) + (d_)*(x_)))^(n_)], x_Symbol] := Dist[1/(d*e*n * Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

Int[Log[(c_) * ((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 3475

Int[tan[(c_) + (d_)*(x_)], x_Symbol] := -Simp[Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]

Rule 3719

Int[((c_) + (d_)*(x_))^(m_)*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m+1))/(d*(m+1)), x] - Dist[2*I, Int[((c + d*x)^m * E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol]
:> Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rule 3722

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol]
:> Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rubi steps

$$\begin{aligned} \int (c + dx)(a + b \tan(e + fx))^2 dx &= \int (a^2(c + dx) + 2ab(c + dx) \tan(e + fx) + b^2(c + dx) \tan^2(e + fx)) dx \\ &= \frac{a^2(c + dx)^2}{2d} + (2ab) \int (c + dx) \tan(e + fx) dx + b^2 \int (c + dx) \tan^2(e + fx) dx \\ &= \frac{a^2(c + dx)^2}{2d} + \frac{iab(c + dx)^2}{d} + \frac{b^2(c + dx) \tan(e + fx)}{f} - (4iab) \int \frac{e^{2i(e+fx)}(c + dx)}{1 + e^{2i(e+fx)}} dx \\ &= -b^2cx - \frac{1}{2}b^2dx^2 + \frac{a^2(c + dx)^2}{2d} + \frac{iab(c + dx)^2}{d} - \frac{2ab(c + dx) \log(1 + e^{2i(e+fx)})}{f} \\ &= -b^2cx - \frac{1}{2}b^2dx^2 + \frac{a^2(c + dx)^2}{2d} + \frac{iab(c + dx)^2}{d} - \frac{2ab(c + dx) \log(1 + e^{2i(e+fx)})}{f} \\ &= -b^2cx - \frac{1}{2}b^2dx^2 + \frac{a^2(c + dx)^2}{2d} + \frac{iab(c + dx)^2}{d} - \frac{2ab(c + dx) \log(1 + e^{2i(e+fx)})}{f} \end{aligned}$$

Mathematica [A] time = 2.32, size = 200, normalized size = 1.47

$$\frac{\cos(e + fx)(a + b \tan(e + fx))^2 (\cos(e + fx) - ((e + fx)(a^2(-2cf + de - dfx) - 2iabd(e + fx) + b^2(2cf - de + d^2x^2))))}{2d^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)*(a + b*Tan[e + f*x])^2,x]
```

```
[Out] (Cos[e + f*x]*(Cos[e + f*x]*(-(e + f*x)*((-2*I)*a*b*d*(e + f*x) + a^2*(d*e - 2*c*f - d*f*x) + b^2*(-(d*e) + 2*c*f + d*f*x)))) - 4*a*b*d*(e + f*x)*Log[1 + E^((2*I)*(e + f*x))] + 2*b*(b*d + 2*a*d*e - 2*a*c*f)*Log[Cos[e + f*x]] + (2*I)*a*b*d*Cos[e + f*x]*PolyLog[2, -E^((2*I)*(e + f*x))] + 2*b^2*f*(c + d*x)*Sin[e + f*x]*(a + b*Tan[e + f*x])^2)/(2*f^2*(a*Cos[e + f*x] + b*Sine + f*x))^2)
```

fricas [A] time = 0.54, size = 219, normalized size = 1.61

$$\frac{(a^2 - b^2)df^2x^2 + 2(a^2 - b^2)cf^2x - iabd\text{Li}_2\left(\frac{2(i \tan(fx+e)-1)}{\tan(fx+e)^2+1} + 1\right) + iabd\text{Li}_2\left(\frac{2(-i \tan(fx+e)-1)}{\tan(fx+e)^2+1} + 1\right) - (2abdfx + 2ab^2x^2)}{2d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*(a+b*tan(f*x+e))^2,x, algorithm="fricas")
```

```
[Out] 1/2*((a^2 - b^2)*d*f^2*x^2 + 2*(a^2 - b^2)*c*f^2*x - I*a*b*d*dilog(2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) + I*a*b*d*dilog(2*(-I*tan(f*x + e)
```


$-1)/(\tan(f*x + e)^2 + 1) + 1) - (2*a*b*d*f*x + 2*a*b*c*f - b^2*d)*\log(-2*(I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)) - (2*a*b*d*f*x + 2*a*b*c*f - b^2*d)*\log(-2*(-I*\tan(f*x + e) - 1)/(\tan(f*x + e)^2 + 1)) + 2*(b^2*d*f*x + b^2*c*f)*\tan(f*x + e))/f^2$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)(b \tan(fx + e) + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate((d*x + c)*(b*tan(f*x + e) + a)^2, x)

maple [A] time = 0.64, size = 238, normalized size = 1.75

$$-2iabcx + \frac{2ibade^2}{f^2} + \frac{a^2dx^2}{2} - \frac{b^2dx^2}{2} + a^2cx - b^2cx + iabd x^2 - \frac{2b^2d \ln(e^{i(fx+e)})}{f^2} + \frac{b^2d \ln(e^{2i(fx+e)} + 1)}{f^2} - \frac{2bac \ln(e^{2i(fx+e)})}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)*(a+b*tan(f*x+e))^2,x)

[Out] $-2*I*a*b*c*x + 2*I/f^2*b*a*d*e^2 + 1/2*a^2*d*x^2 - 1/2*b^2*d*x^2 + a^2*c*x - b^2*c*x + 2*I*b^2*(d*x+c)/f/(exp(2*I*(f*x+e))+1) - 2/f^2*b^2*d*\ln(exp(I*(f*x+e)))+1/f^2*b^2*d*\ln(exp(2*I*(f*x+e))+1) - 2/f*b*a*c*\ln(exp(2*I*(f*x+e))+1) + 4/f*b*a*c*\ln(exp(I*(f*x+e)))-4/f^2*b*a*d*e*\ln(exp(I*(f*x+e)))+I*a*b*d*x^2 + 4*I/f*b*a*d*e*x + I*a*b*d*polylog(2, -exp(2*I*(f*x+e)))/f^2 - 2/f*b*\ln(exp(2*I*(f*x+e))+1)*a*d*x$

maxima [B] time = 0.82, size = 529, normalized size = 3.89

$$2(fx + e)a^2c + \frac{(fx+e)^2 a^2 d}{f} - \frac{2(fx+e)a^2 de}{f} + 4abc \log(\sec(fx + e)) - \frac{4abde \log(\sec(fx+e))}{f} + \frac{2((2ab+ib^2)(fx+e)^2 d - 4b^2 d)}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out] $1/2*(2*(f*x + e)*a^2*c + (f*x + e)^2*a^2*d/f - 2*(f*x + e)*a^2*d*e/f + 4*a*b*c*\log(\sec(f*x + e)) - 4*a*b*d*e*\log(\sec(f*x + e))/f + 2*((2*a*b + I*b^2)*(f*x + e)^2*d - 4*b^2*d*e + 4*b^2*c*f - (2*I*b^2*d*e - 2*I*b^2*c*f)*(f*x + e) - (4*(f*x + e)*a*b*d - 2*b^2*d + 2*(2*(f*x + e)*a*b*d - b^2*d)*\cos(2*f*x + 2*e) + (4*I*(f*x + e)*a*b*d - 2*I*b^2*d)*\sin(2*f*x + 2*e))*\arctan2(\sin(2*f*x + 2*e), \cos(2*f*x + 2*e) + 1) + ((2*a*b + I*b^2)*(f*x + e)^2*d - (2*I*b^2*d*e - 2*I*b^2*c*f + 4*b^2*d)*(f*x + e))*\cos(2*f*x + 2*e) + (2*a*b*d*\cos(2*f*x + 2*e) + 2*I*a*b*d*\sin(2*f*x + 2*e) + 2*a*b*d)*\operatorname{dilog}(-e^{(2*I*f*x + 2*I*e)}) - (-2*I*(f*x + e)*a*b*d + I*b^2*d + (-2*I*(f*x + e)*a*b*d + I*b^2*d)*\cos(2*f*x + 2*e) + (2*(f*x + e)*a*b*d - b^2*d)*\sin(2*f*x + 2*e))*\log(\cos(2*f*x + 2*e)^2 + \sin(2*f*x + 2*e)^2 + 2*\cos(2*f*x + 2*e) + 1) - ((-2*I*a*b + b^2)*(f*x + e)^2*d - (2*b^2*d*e - 2*b^2*c*f - 4*I*b^2*d)*(f*x + e))*\sin(2*f*x + 2*e))/(-2*I*f*\cos(2*f*x + 2*e) + 2*f*\sin(2*f*x + 2*e) - 2*I*f)/f$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int (a + b \tan(e + fx))^2 (c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a + b*tan(e + f*x))^2*(c + d*x),x)`

[Out] `int((a + b*tan(e + f*x))^2*(c + d*x), x)`

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + fx))^2 (c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x+c)*(a+b*tan(f*x+e))**2,x)`

[Out] `Integral((a + b*tan(e + f*x))**2*(c + d*x), x)`

$$3.47 \quad \int \frac{(a+b \tan(e+fx))^2}{c+dx} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{(a+b \tan(e+fx))^2}{c+dx}, x\right)$$

[Out] Unintegrable((a+b*tan(f*x+e))^2/(d*x+c), x)

Rubi [A] time = 0.05, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a+b \tan(e+fx))^2}{c+dx} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*Tan[e + f*x])^2/(c + d*x), x]

[Out] Defer[Int][(a + b*Tan[e + f*x])^2/(c + d*x), x]

Rubi steps

$$\int \frac{(a+b \tan(e+fx))^2}{c+dx} dx = \int \frac{(a+b \tan(e+fx))^2}{c+dx} dx$$

Mathematica [A] time = 20.27, size = 0, normalized size = 0.00

$$\int \frac{(a+b \tan(e+fx))^2}{c+dx} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*Tan[e + f*x])^2/(c + d*x), x]

[Out] Integrate[(a + b*Tan[e + f*x])^2/(c + d*x), x]

fricas [A] time = 0.62, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{b^2 \tan(fx+e)^2 + 2ab \tan(fx+e) + a^2}{dx+c}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^2/(d*x+c), x, algorithm="fricas")

[Out] integral((b^2*tan(f*x + e)^2 + 2*a*b*tan(f*x + e) + a^2)/(d*x + c), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(b \tan(fx+e) + a)^2}{dx+c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^2/(d*x+c), x, algorithm="giac")

[Out] integrate((b*tan(f*x + e) + a)^2/(d*x + c), x)

maple [A] time = 2.70, size = 0, normalized size = 0.00

$$\int \frac{(a + b \tan(fx + e))^2}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*tan(f*x+e))^2/(d*x+c),x)

[Out] int((a+b*tan(f*x+e))^2/(d*x+c),x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$((a^2 - b^2)dfx + (a^2 - b^2)cf) \cos(2fx + 2e)^2 \log(dx + c) + 2b^2d \sin(2fx + 2e) + ((a^2 - b^2)dfx + (a^2 - b^2)cf)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^2/(d*x+c),x, algorithm="maxima")

[Out] (((a^2 - b^2)*d*f*x + (a^2 - b^2)*c*f)*cos(2*f*x + 2*e)^2*log(d*x + c) + 2*b^2*d*sin(2*f*x + 2*e) + ((a^2 - b^2)*d*f*x + (a^2 - b^2)*c*f)*log(d*x + c)*sin(2*f*x + 2*e)^2 + 2*((a^2 - b^2)*d*f*x + (a^2 - b^2)*c*f)*cos(2*f*x + 2*e)*log(d*x + c) + (d^2*f*x + c*d*f + (d^2*f*x + c*d*f)*cos(2*f*x + 2*e)^2 + (d^2*f*x + c*d*f)*sin(2*f*x + 2*e)^2 + 2*(d^2*f*x + c*d*f)*cos(2*f*x + 2*e))*integrate(2*(2*a*b*d*f*x + 2*a*b*c*f + b^2*d)*sin(2*f*x + 2*e)/(d^2*f*x^2 + 2*c*d*f*x + c^2*f + (d^2*f*x^2 + 2*c*d*f*x + c^2*f)*cos(2*f*x + 2*e)^2 + (d^2*f*x^2 + 2*c*d*f*x + c^2*f)*sin(2*f*x + 2*e)^2 + 2*(d^2*f*x^2 + 2*c*d*f*x + c^2*f)*cos(2*f*x + 2*e)), x) + ((a^2 - b^2)*d*f*x + (a^2 - b^2)*c*f)*log(d*x + c)/(d^2*f*x + c*d*f + (d^2*f*x + c*d*f)*cos(2*f*x + 2*e)^2 + (d^2*f*x + c*d*f)*sin(2*f*x + 2*e)^2 + 2*(d^2*f*x + c*d*f)*cos(2*f*x + 2*e))

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{(a + b \tan(e + fx))^2}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^2/(c + d*x),x)

[Out] int((a + b*tan(e + f*x))^2/(c + d*x), x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + b \tan(e + fx))^2}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))**2/(d*x+c),x)

[Out] Integral((a + b*tan(e + f*x))**2/(c + d*x), x)

$$3.48 \quad \int \frac{(a+b \tan(e+fx))^2}{(c+dx)^2} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{(a+b \tan(e+fx))^2}{(c+dx)^2}, x\right)$$

[Out] Unintegrable((a+b*tan(f*x+e))^2/(d*x+c)^2, x)

Rubi [A] time = 0.05, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a+b \tan(e+fx))^2}{(c+dx)^2} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*Tan[e + f*x])^2/(c + d*x)^2, x]

[Out] Defer[Int][(a + b*Tan[e + f*x])^2/(c + d*x)^2, x]

Rubi steps

$$\int \frac{(a+b \tan(e+fx))^2}{(c+dx)^2} dx = \int \frac{(a+b \tan(e+fx))^2}{(c+dx)^2} dx$$

Mathematica [A] time = 15.69, size = 0, normalized size = 0.00

$$\int \frac{(a+b \tan(e+fx))^2}{(c+dx)^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*Tan[e + f*x])^2/(c + d*x)^2, x]

[Out] Integrate[(a + b*Tan[e + f*x])^2/(c + d*x)^2, x]

fricas [A] time = 0.48, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{b^2 \tan^2(fx + e) + 2ab \tan(fx + e) + a^2}{d^2 x^2 + 2cdx + c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^2/(d*x+c)^2, x, algorithm="fricas")

[Out] integral((b^2*tan(f*x + e)^2 + 2*a*b*tan(f*x + e) + a^2)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(b \tan(fx + e) + a)^2}{(dx + c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^2/(d*x+c)^2, x, algorithm="giac")

[Out] integrate((b*tan(f*x + e) + a)^2/(d*x + c)^2, x)

maple [A] time = 3.31, size = 0, normalized size = 0.00

$$\int \frac{(a + b \tan(fx + e))^2}{(dx + c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*tan(f*x+e))^2/(d*x+c)^2,x)

[Out] int((a+b*tan(f*x+e))^2/(d*x+c)^2,x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

$$(a^2 - b^2)dfx - 2b^2d \sin(2fx + 2e) + (a^2 - b^2)cf + ((a^2 - b^2)dfx + (a^2 - b^2)cf) \cos(2fx + 2e)^2 + ((a^2 - b^2)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^2/(d*x+c)^2,x, algorithm="maxima")

[Out] -((a^2 - b^2)*d*f*x - 2*b^2*d*sin(2*f*x + 2*e) + (a^2 - b^2)*c*f + ((a^2 - b^2)*d*f*x + (a^2 - b^2)*c*f)*cos(2*f*x + 2*e)^2 + ((a^2 - b^2)*d*f*x + (a^2 - b^2)*c*f)*sin(2*f*x + 2*e)^2 + 2*((a^2 - b^2)*d*f*x + (a^2 - b^2)*c*f)*cos(2*f*x + 2*e) - (d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f + (d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f)*cos(2*f*x + 2*e)^2 + (d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f)*sin(2*f*x + 2*e)^2 + 2*(d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f)*cos(2*f*x + 2*e)) *integrate(4*(a*b*d*f*x + a*b*c*f + b^2*d)*sin(2*f*x + 2*e)/(d^3*f*x^3 + 3*c*d^2*f*x^2 + 3*c^2*d*f*x + c^3*f)*cos(2*f*x + 2*e)^2 + (d^3*f*x^3 + 3*c*d^2*f*x^2 + 3*c^2*d*f*x + c^3*f)*sin(2*f*x + 2*e)^2 + 2*(d^3*f*x^3 + 3*c*d^2*f*x^2 + 3*c^2*d*f*x + c^3*f)*cos(2*f*x + 2*e)), x)/(d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f + (d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f)*cos(2*f*x + 2*e)^2 + (d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f)*sin(2*f*x + 2*e)^2 + 2*(d^3*f*x^2 + 2*c*d^2*f*x + c^2*d*f)*cos(2*f*x + 2*e))

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{(a + b \tan(e + fx))^2}{(c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^2/(c + d*x)^2,x)

[Out] int((a + b*tan(e + f*x))^2/(c + d*x)^2, x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + b \tan(e + fx))^2}{(c + dx)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))**2/(d*x+c)**2,x)

[Out] Integral((a + b*tan(e + f*x))**2/(c + d*x)**2, x)

3.49 $\int (c + dx)^3 (a + b \tan(e + fx))^3 dx$

Optimal. Leaf size=612

$$\frac{a^3(c + dx)^4}{4d} - \frac{9a^2bd^2(c + dx)\text{Li}_3(-e^{2i(e+fx)})}{2f^3} + \frac{9ia^2bd(c + dx)^2\text{Li}_2(-e^{2i(e+fx)})}{2f^2} - \frac{3a^2b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f}$$

[Out] $\frac{3}{2}I*b^3*d^3*\text{polylog}(2, -\exp(2*I*(f*x+e)))/f^4 - 3*I*a*b^2*(d*x+c)^3/f + 1/2*b^3*(d*x+c)^3/f + 1/4*a^3*(d*x+c)^4/d - 3/2*I*b^3*d*(d*x+c)^2*\text{polylog}(2, -\exp(2*I*(f*x+e)))/f^2 - 3/4*a*b^2*(d*x+c)^4/d + 3/4*I*b^3*d^3*\text{polylog}(4, -\exp(2*I*(f*x+e)))/f^4 - 3*b^3*d^2*(d*x+c)*\ln(1+\exp(2*I*(f*x+e)))/f^3 + 9*a*b^2*d*(d*x+c)^2*\ln(1+\exp(2*I*(f*x+e)))/f^2 - 3*a^2*b*(d*x+c)^3*\ln(1+\exp(2*I*(f*x+e)))/f + b^3*(d*x+c)^3*\ln(1+\exp(2*I*(f*x+e)))/f - 1/4*I*b^3*(d*x+c)^4/d - 9/4*I*a^2*b*d^3*\text{polylog}(4, -\exp(2*I*(f*x+e)))/f^4 + 9/2*I*a^2*b*d*(d*x+c)^2*\text{polylog}(2, -\exp(2*I*(f*x+e)))/f^2 + 3/4*I*a^2*b*(d*x+c)^4/d + 9/2*a*b^2*d^3*\text{polylog}(3, -\exp(2*I*(f*x+e)))/f^4 - 9/2*a^2*b*d^2*(d*x+c)*\text{polylog}(3, -\exp(2*I*(f*x+e)))/f^3 + 3/2*b^3*d^2*(d*x+c)*\text{polylog}(3, -\exp(2*I*(f*x+e)))/f^3 + 3/2*I*b^3*d*(d*x+c)^2/f^2 - 9*I*a*b^2*d^2*(d*x+c)*\text{polylog}(2, -\exp(2*I*(f*x+e)))/f^3 - 3/2*b^3*d*(d*x+c)^2*\tan(f*x+e)/f^2 + 3*a*b^2*(d*x+c)^3*\tan(f*x+e)/f + 1/2*b^3*(d*x+c)^3*\tan(f*x+e)^2/f$

Rubi [A] time = 0.98, antiderivative size = 612, normalized size of antiderivative = 1.00, number of steps used = 28, number of rules used = 11, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.550$, Rules used = {3722, 3719, 2190, 2531, 6609, 2282, 6589, 3720, 32, 2279, 2391}

$$-\frac{9a^2bd^2(c + dx)\text{Li}_3(-e^{2i(e+fx)})}{2f^3} + \frac{9ia^2bd(c + dx)^2\text{Li}_2(-e^{2i(e+fx)})}{2f^2} - \frac{3a^2b(c + dx)^3 \log(1 + e^{2i(e+fx)})}{f} + \frac{3ia^2b(c + dx)^4}{4d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3*(a + b*Tan[e + f*x])^3,x]

[Out] $((3I/2)*b^3*d*(c + d*x)^2)/f^2 - ((3I)*a*b^2*(c + d*x)^3)/f + (b^3*(c + d*x)^3)/(2*f) + (a^3*(c + d*x)^4)/(4*d) + ((3I/4)*a^2*b*(c + d*x)^4)/d - (3*a*b^2*(c + d*x)^4)/(4*d) - ((I/4)*b^3*(c + d*x)^4)/d - (3*b^3*d^2*(c + d*x)*\text{Log}[1 + E^((2I)*(e + f*x))])/f^3 + (9*a*b^2*d*(c + d*x)^2*\text{Log}[1 + E^((2I)*(e + f*x))])/f^2 - (3*a^2*b*(c + d*x)^3*\text{Log}[1 + E^((2I)*(e + f*x))])/f + (b^3*(c + d*x)^3*\text{Log}[1 + E^((2I)*(e + f*x))])/f + ((3I/2)*b^3*d^3*\text{PolyLog}[2, -E^((2I)*(e + f*x))])/f^4 - ((9I)*a*b^2*d^2*(c + d*x)*\text{PolyLog}[2, -E^((2I)*(e + f*x))])/f^3 + (((9I)/2)*a^2*b*d*(c + d*x)^2*\text{PolyLog}[2, -E^((2I)*(e + f*x))])/f^2 - (((3I)/2)*b^3*d*(c + d*x)^2*\text{PolyLog}[2, -E^((2I)*(e + f*x))])/f^2 + (9*a*b^2*d^3*\text{PolyLog}[3, -E^((2I)*(e + f*x))])/(2*f^4) - (9*a^2*b*d^2*(c + d*x)*\text{PolyLog}[3, -E^((2I)*(e + f*x))])/(2*f^3) + (3*b^3*d^2*(c + d*x)*\text{PolyLog}[3, -E^((2I)*(e + f*x))])/(2*f^3) - (((9I)/4)*a^2*b*d^3*\text{PolyLog}[4, -E^((2I)*(e + f*x))])/f^4 + (((3I)/4)*b^3*d^3*\text{PolyLog}[4, -E^((2I)*(e + f*x))])/f^4 - (3*b^3*d*(c + d*x)^2*\text{Tan}[e + f*x])/(2*f^2) + (3*a*b^2*(c + d*x)^3*\text{Tan}[e + f*x])/f + (b^3*(c + d*x)^3*\text{Tan}[e + f*x]^2)/(2*f)$

Rule 32

Int[((a_.) + (b_.)*(x_.))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rule 2190

Int[(((F_)^(g_.)*((e_.) + (f_.)*(x_.)))^(n_.)*((c_.) + (d_.)*(x_.))^(m_.))/((a_.) + (b_.)*((F_)^(g_.)*((e_.) + (f_.)*(x_.)))^(n_.), x_Symbol] := Simp[((c + d*x)^m*\text{Log}[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*\text{Log}[F]), x] - Dist[(d*m)/(b*f*g*n*\text{Log}[F]), Int[(c + d*x)^(m - 1)*\text{Log}[1 + (b*(F^(g*(e + f*x)))^n)]]

))ⁿ)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_)))^{n_})], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))ⁿ], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^{n_})^{m_}] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))* (F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2391

Int[Log[(c_)*((d_) + (e_)*(x_)^{n_})]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*xⁿ)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 2531

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^{n_})]*((f_) + (g_)*(x_)^{m_}), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)))ⁿ)]/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^{m-1}*PolyLog[2, -(e*(F^(c*(a + b*x)))ⁿ]], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3719

Int[((c_) + (d_)*(x_)^{m_})*tan[(e_) + (f_)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^{m+1})/(d*(m+1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

Int[((c_) + (d_)*(x_)^{m_})*((b_)*tan[(e_) + (f_)*(x_)])^{n_}, x_Symbol] := Simp[(b*(c + d*x)^m*((b*Tan[e + f*x])ⁿ⁻¹)/(f*(n-1)), x] + (-Dist[(b*d*m)/(f*(n-1)), Int[(c + d*x)^{m-1}*((b*Tan[e + f*x])ⁿ⁻¹), x], x] - Dist[b², Int[(c + d*x)^m*((b*Tan[e + f*x])ⁿ⁻²), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

Rule 3722

Int[((c_) + (d_)*(x_)^{m_})*((a_) + (b_)*tan[(e_) + (f_)*(x_)])^{n_}, x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])ⁿ], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rule 6589

Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_)^{p_})]/((d_) + (e_)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6609


```
Int[((e_.) + (f_.)*(x_.))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_.)))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^
(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned}
\int (c + dx)^3 (a + b \tan(e + fx))^3 dx &= \int (a^3(c + dx)^3 + 3a^2b(c + dx)^3 \tan(e + fx) + 3ab^2(c + dx)^3 \tan^2(e + fx) \\
&+ b^3(c + dx)^3 \tan^3(e + fx)) dx \\
&= \frac{a^3(c + dx)^4}{4d} + (3a^2b) \int (c + dx)^3 \tan(e + fx) dx + (3ab^2) \int (c + dx)^3 \tan^2(e + fx) dx \\
&+ b^3 \int (c + dx)^3 \tan^3(e + fx) dx \\
&= \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d} + \frac{3ab^2(c + dx)^3 \tan(e + fx)}{f} + \frac{b^3(c + dx)^3 \tan^2(e + fx)}{2f} \\
&+ \frac{3iab^2(c + dx)^3}{f} + \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d} - \frac{3ab^2(c + dx)^4}{4d} - \frac{ib^3(c + dx)^3 \tan(e + fx)}{f} \\
&= \frac{3ib^3d(c + dx)^2}{2f^2} - \frac{3iab^2(c + dx)^3}{f} + \frac{b^3(c + dx)^3}{2f} + \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d} \\
&= \frac{3ib^3d(c + dx)^2}{2f^2} - \frac{3iab^2(c + dx)^3}{f} + \frac{b^3(c + dx)^3}{2f} + \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d} \\
&= \frac{3ib^3d(c + dx)^2}{2f^2} - \frac{3iab^2(c + dx)^3}{f} + \frac{b^3(c + dx)^3}{2f} + \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d} \\
&= \frac{3ib^3d(c + dx)^2}{2f^2} - \frac{3iab^2(c + dx)^3}{f} + \frac{b^3(c + dx)^3}{2f} + \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d} \\
&= \frac{3ib^3d(c + dx)^2}{2f^2} - \frac{3iab^2(c + dx)^3}{f} + \frac{b^3(c + dx)^3}{2f} + \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d} \\
&= \frac{3ib^3d(c + dx)^2}{2f^2} - \frac{3iab^2(c + dx)^3}{f} + \frac{b^3(c + dx)^3}{2f} + \frac{a^3(c + dx)^4}{4d} + \frac{3ia^2b(c + dx)^4}{4d}
\end{aligned}$$

Mathematica [B] time = 8.48, size = 2572, normalized size = 4.20

Result too large to show

Warning: Unable to verify antiderivative.

```
[In] Integrate[(c + d*x)^3*(a + b*Tan[e + f*x])^3,x]
```

```
[Out] (((3*I)/4)*a*b^2*d^3*(2*f^2*x^2*(2*f*x - (3*I)*(1 + E^((2*I)*e))*Log[1 + E^
((-2*I)*(e + f*x))]) + 6*(1 + E^((2*I)*e))*f*x*PolyLog[2, -E^((-2*I)*(e + f
*x))]) - (3*I)*(1 + E^((2*I)*e))*PolyLog[3, -E^((-2*I)*(e + f*x))])*Sec[e])/
(E^(I*e)*f^4) - (((3*I)/4)*a^2*b*c*d^2*(2*f^2*x^2*(2*f*x - (3*I)*(1 + E^((2
*I)*e))*Log[1 + E^((-2*I)*(e + f*x))]) + 6*(1 + E^((2*I)*e))*f*x*PolyLog[2,
-E^((-2*I)*(e + f*x))]) - (3*I)*(1 + E^((2*I)*e))*PolyLog[3, -E^((-2*I)*(e
+ f*x))])*Sec[e])/(E^(I*e)*f^3) + ((I/4)*b^3*c*d^2*(2*f^2*x^2*(2*f*x - (3*I
)*(1 + E^((2*I)*e))*Log[1 + E^((-2*I)*(e + f*x))]) + 6*(1 + E^((2*I)*e))*f*
x*PolyLog[2, -E^((-2*I)*(e + f*x))]) - (3*I)*(1 + E^((2*I)*e))*PolyLog[3, -E
^((-2*I)*(e + f*x))])*Sec[e])/(E^(I*e)*f^3) - ((3*I)/8)*a^2*b*d^3*E^(I*e)*
(2*x^4)/E^((2*I)*e) - ((4*I)*(1 + E^((-2*I)*e))*x^3*Log[1 + E^((-2*I)*(e +
f*x))])/f + (3*(1 + E^((2*I)*e))*(2*f^2*x^2*PolyLog[2, -E^((-2*I)*(e + f*x)
)]) - (2*I)*f*x*PolyLog[3, -E^((-2*I)*(e + f*x))]) - PolyLog[4, -E^((-2*I)*(e
+ f*x))])/E^((2*I)*e)*f^4)*Sec[e] + (I/8)*b^3*d^3*E^(I*e)*((2*x^4)/E^((
2*I)*e) - ((4*I)*(1 + E^((-2*I)*e))*x^3*Log[1 + E^((-2*I)*(e + f*x))])/f +
(3*(1 + E^((2*I)*e))*(2*f^2*x^2*PolyLog[2, -E^((-2*I)*(e + f*x))]) - (2*I)*f
```

```

**PolyLog[3, -E^((-2*I)*(e + f*x))] - PolyLog[4, -E^((-2*I)*(e + f*x)))]/
(E^((2*I)*e)*f^4))*Sec[e] + ((b^3*c^3 + 3*b^3*c^2*d*x + 3*b^3*c*d^2*x^2 + b
^3*d^3*x^3)*Sec[e + f*x]^2)/(2*f) - (3*b^3*c*d^2*Sec[e]*(Cos[e]*Log[Cos[e]*
Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f^3*(Cos[e]^2 + Sin[e]^2)) + (9
*a*b^2*c^2*d*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Si
n[e]))/(f^2*(Cos[e]^2 + Sin[e]^2)) - (3*a^2*b*c^3*Sec[e]*(Cos[e]*Log[Cos[e]
*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f*(Cos[e]^2 + Sin[e]^2)) + (b^
3*c^3*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/
(f*(Cos[e]^2 + Sin[e]^2)) - (3*b^3*d^3*Csc[e]*((f^2*x^2)/E^(I*ArcTan[Cot[e]
])) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]])) - Pi*Log[1 + E^((-2*I)*f*x)] -
2*(f*x - ArcTan[Cot[e]])*Log[1 - E^((2*I)*(f*x - ArcTan[Cot[e]]))]) + Pi*Lo
g[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]]]) + I*PolyLog[2
, E^((2*I)*(f*x - ArcTan[Cot[e]])))]/Sqrt[1 + Cot[e]^2])*Sec[e]/(2*f^4*Sq
rt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2)]) + (9*a*b^2*c*d^2*Csc[e]*((f^2*x^2)/E^(I
*ArcTan[Cot[e]])) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]])) - Pi*Log[1 + E^
(-2*I)*f*x)] - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^((2*I)*(f*x - ArcTan[Cot[
e]]))]) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]]]
+ I*PolyLog[2, E^((2*I)*(f*x - ArcTan[Cot[e]])))]/Sqrt[1 + Cot[e]^2])*Sec
[e]/(f^3*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2)]) - (9*a^2*b*c^2*d*Csc[e]*((f
^2*x^2)/E^(I*ArcTan[Cot[e]])) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]])) - Pi
*Log[1 + E^((-2*I)*f*x)] - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^((2*I)*(f*x -
ArcTan[Cot[e]]))]) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcT
an[Cot[e]]]]) + I*PolyLog[2, E^((2*I)*(f*x - ArcTan[Cot[e]])))]/Sqrt[1 + Co
t[e]^2])*Sec[e]/(2*f^2*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2)]) + (3*b^3*c^2*
d*Csc[e]*((f^2*x^2)/E^(I*ArcTan[Cot[e]])) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[C
ot[e]])) - Pi*Log[1 + E^((-2*I)*f*x)] - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^
(2*I)*(f*x - ArcTan[Cot[e]]))]) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Si
n[f*x - ArcTan[Cot[e]]]]) + I*PolyLog[2, E^((2*I)*(f*x - ArcTan[Cot[e]])))]
/Sqrt[1 + Cot[e]^2])*Sec[e]/(2*f^2*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2)]) +
(3*x^2*(a^3*c^2*d + (3*I)*a^2*b*c^2*d - 3*a*b^2*c^2*d - I*b^3*c^2*d + a^3*
c^2*d*cos[2*e] - (3*I)*a^2*b*c^2*d*cos[2*e] - 3*a*b^2*c^2*d*cos[2*e] + I*b^
3*c^2*d*cos[2*e] + I*a^3*c^2*d*sin[2*e] + 3*a^2*b*c^2*d*sin[2*e] - (3*I)*a*
b^2*c^2*d*sin[2*e] - b^3*c^2*d*sin[2*e]))/(2*(1 + Cos[2*e] + I*Sin[2*e])) +
(x^3*(a^3*c*d^2 + (3*I)*a^2*b*c*d^2 - 3*a*b^2*c*d^2 - I*b^3*c*d^2 + a^3*c*
d^2*cos[2*e] - (3*I)*a^2*b*c*d^2*cos[2*e] - 3*a*b^2*c*d^2*cos[2*e] + I*b^3*
c*d^2*cos[2*e] + I*a^3*c*d^2*sin[2*e] + 3*a^2*b*c*d^2*sin[2*e] - (3*I)*a*b^
2*c*d^2*sin[2*e] - b^3*c*d^2*sin[2*e]))/(1 + Cos[2*e] + I*Sin[2*e]) + (x^4*
(a^3*d^3 + (3*I)*a^2*b*d^3 - 3*a*b^2*d^3 - I*b^3*d^3 + a^3*d^3*cos[2*e] -
(3*I)*a^2*b*d^3*cos[2*e] - 3*a*b^2*d^3*cos[2*e] + I*b^3*d^3*cos[2*e] + I*a^3
*d^3*sin[2*e] + 3*a^2*b*d^3*sin[2*e] - (3*I)*a*b^2*d^3*sin[2*e] - b^3*d^3*S
in[2*e]))/(4*(1 + Cos[2*e] + I*Sin[2*e])) + x*(a^3*c^3 - 3*a*b^2*c^3 + ((3*
I)*a^2*b*c^3)/(1 + Cos[2*e] + I*Sin[2*e]) + ((-3*I)*a^2*b*c^3*cos[2*e] + 3*
a^2*b*c^3*sin[2*e]))/(1 + Cos[2*e] + I*Sin[2*e]) + ((2*I)*b^3*c^3*cos[2*e] -
2*b^3*c^3*sin[2*e])/((1 + Cos[2*e] + I*Sin[2*e])*(1 - Cos[2*e] + Cos[4*e]
- I*Sin[2*e] + I*Sin[4*e])) + ((-2*I)*b^3*c^3*cos[4*e] + 2*b^3*c^3*sin[4*e]
)/((1 + Cos[2*e] + I*Sin[2*e])*(1 - Cos[2*e] + Cos[4*e] - I*Sin[2*e] + I*Si
n[4*e])) - (I*b^3*c^3)/(1 + Cos[6*e] + I*Sin[6*e]) + (I*b^3*c^3*cos[6*e] -
b^3*c^3*sin[6*e])/((1 + Cos[6*e] + I*Sin[6*e])) + (3*Sec[e]*Sec[e + f*x]*(-
b^3*c^2*d*sin[f*x]) + 2*a*b^2*c^3*f*sin[f*x] - 2*b^3*c*d^2*x*sin[f*x] + 6*a
*b^2*c^2*d*f*x*sin[f*x] - b^3*d^3*x^2*sin[f*x] + 6*a*b^2*c*d^2*f*x^2*sin[f*
x] + 2*a*b^2*d^3*f*x^3*sin[f*x]))/(2*f^2)

```

fricas [C] time = 0.54, size = 1175, normalized size = 1.92

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3*(a+b*tan(f*x+e))^3,x, algorithm="fricas")

[Out] 1/8*(2*(a^3 - 3*a*b^2)*d^3*f^4*x^4 + 3*I*(3*a^2*b - b^3)*d^3*polylog(4, (ta

```

n(f*x + e)^2 + 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 3*I*(3*a^2*b -
b^3)*d^3*polylog(4, (tan(f*x + e)^2 - 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^
2 + 1)) + 4*(b^3*d^3*f^3 + 2*(a^3 - 3*a*b^2)*c*d^2*f^4)*x^3 + 12*(b^3*c*d^2
*f^3 + (a^3 - 3*a*b^2)*c^2*d*f^4)*x^2 + 4*(b^3*d^3*f^3*x^3 + 3*b^3*c*d^2*f^
3*x^2 + 3*b^3*c^2*d*f^3*x + b^3*c^3*f^3)*tan(f*x + e)^2 + 4*(3*b^3*c^2*d*f^
3 + 2*(a^3 - 3*a*b^2)*c^3*f^4)*x + (-6*I*(3*a^2*b - b^3)*d^3*f^2*x^2 + 36*I
*a*b^2*c*d^2*f - 6*I*b^3*d^3 - 6*I*(3*a^2*b - b^3)*c^2*d*f^2 + 12*I*(3*a*b^
2*d^3*f - (3*a^2*b - b^3)*c*d^2*f^2)*x)*dilog(2*(I*tan(f*x + e) - 1)/(tan(f
*x + e)^2 + 1) + 1) + (6*I*(3*a^2*b - b^3)*d^3*f^2*x^2 - 36*I*a*b^2*c*d^2*f
+ 6*I*b^3*d^3 + 6*I*(3*a^2*b - b^3)*c^2*d*f^2 - 12*I*(3*a*b^2*d^3*f - (3*a
^2*b - b^3)*c*d^2*f^2)*x)*dilog(2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1
) + 1) - 4*((3*a^2*b - b^3)*d^3*f^3*x^3 - 9*a*b^2*c^2*d*f^2 + 3*b^3*c*d^2*f
+ (3*a^2*b - b^3)*c^3*f^3 - 3*(3*a*b^2*d^3*f^2 - (3*a^2*b - b^3)*c*d^2*f^3
)*x^2 - 3*(6*a*b^2*c*d^2*f^2 - b^3*d^3*f - (3*a^2*b - b^3)*c^2*d*f^3)*x)*lo
g(-2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 4*((3*a^2*b - b^3)*d^3*f^
3*x^3 - 9*a*b^2*c^2*d*f^2 + 3*b^3*c*d^2*f + (3*a^2*b - b^3)*c^3*f^3 - 3*(3*
a*b^2*d^3*f^2 - (3*a^2*b - b^3)*c*d^2*f^3)*x^2 - 3*(6*a*b^2*c*d^2*f^2 - b^3
*d^3*f - (3*a^2*b - b^3)*c^2*d*f^3)*x)*log(-2*(-I*tan(f*x + e) - 1)/(tan(f*
x + e)^2 + 1)) + 6*(3*a*b^2*d^3 - (3*a^2*b - b^3)*d^3*f*x - (3*a^2*b - b^3)
*c*d^2*f)*polylog(3, (tan(f*x + e)^2 + 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^
2 + 1)) + 6*(3*a*b^2*d^3 - (3*a^2*b - b^3)*d^3*f*x - (3*a^2*b - b^3)*c*d^2*
f)*polylog(3, (tan(f*x + e)^2 - 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1))
+ 12*(2*a*b^2*d^3*f^3*x^3 + 2*a*b^2*c^3*f^3 - b^3*c^2*d*f^2 + (6*a*b^2*c*d
^2*f^3 - b^3*d^3*f^2)*x^2 + 2*(3*a*b^2*c^2*d*f^3 - b^3*c*d^2*f^2)*x)*tan(f*
x + e))/f^4

```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)^3 (b \tan(fx + e) + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3*(a+b*tan(f*x+e))^3,x, algorithm="giac")

[Out] integrate((d*x + c)^3*(b*tan(f*x + e) + a)^3, x)

maple [B] time = 1.01, size = 1882, normalized size = 3.08

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3*(a+b*tan(f*x+e))^3,x)

[Out] $-18*I/f^2*b*a^2*c*d^2*e^2*x+18*I/f*b*a^2*c^2*d*e*x-36*I/f^2*b^2*a*c*d^2*e*x$
 $+9*I/f^2*b*polylog(2, -exp(2*I*(f*x+e)))*a^2*c*d^2*x+b^2*(-6*I*b*c*d^2*x+6*I$
 $*a*d^3*f*x^3*exp(2*I*(f*x+e))+2*b*d^3*f*x^3*exp(2*I*(f*x+e))-3*I*b*c^2*d+18$
 $*I*a*c^2*d*f*x*exp(2*I*(f*x+e))+6*I*a*c^3*f*exp(2*I*(f*x+e))+6*b*c*d^2*f*x^$
 $2*exp(2*I*(f*x+e))-3*I*b*c^2*d*exp(2*I*(f*x+e))+6*I*a*d^3*f*x^3+18*I*a*c^2*$
 $d*f*x+6*b*c^2*d*f*x*exp(2*I*(f*x+e))-3*I*b*d^3*x^2*exp(2*I*(f*x+e))+18*I*a*$
 $c*d^2*f*x^2*exp(2*I*(f*x+e))-3*I*d^3*x^2*b+2*b*c^3*f*exp(2*I*(f*x+e))+6*I*a$
 $*c^3*f-6*I*b*c*d^2*x*exp(2*I*(f*x+e))+18*I*a*c*d^2*f*x^2)/f^2/(exp(2*I*(f*x$
 $+e))+1)^2+a^3*c*d^2*x^3+1/f*b^3*c^3*ln(exp(2*I*(f*x+e))+1)-2/f*b^3*c^3*ln(e$
 $xp(I*(f*x+e)))-1/4*I*b^3*d^3*x^4+3/2*I*b^3*d^3*polylog(2, -exp(2*I*(f*x+e)))$
 $/f^4+3/4*I*b^3*d^3*polylog(4, -exp(2*I*(f*x+e)))/f^4-3/4*a*b^2*d^3*x^4+3/2*a$
 $^3*c^2*d*x^2-3*b^2*a*c^3*x+I*b^3*c^3*x-9/2/f^3*b*a^2*c*d^2*polylog(3, -exp(2$
 $*I*(f*x+e))+1/f*b^3*d^3*ln(exp(2*I*(f*x+e))+1)*x^3-6/f^3*b^3*c*d^2*e^2*ln($
 $exp(I*(f*x+e)))-6/f^4*b*a^2*d^3*e^3*ln(exp(I*(f*x+e)))-18/f^4*b^2*a*d^3*e^2$
 $*ln(exp(I*(f*x+e)))-18/f^2*b^2*a*c^2*d*ln(exp(I*(f*x+e)))+9/f^2*b^2*a*d^3*ln$
 $(exp(2*I*(f*x+e))+1)*x^2-3/2*I*b^3*c^2*d*x^2-I*b^3*c*d^2*x^3+3/4*I*a^2*b*d$
 $^3*x^4-9/f*b*ln(exp(2*I*(f*x+e))+1)*a^2*c^2*d*x+18/f^2*b^2*ln(exp(2*I*(f*x+$

```
e)))+1)*a*c*d^2*x-9/f*b*ln(exp(2*I*(f*x+e)))+1)*a^2*c*d^2*x^2+9/2*a*b^2*d^3*p
olylog(3,-exp(2*I*(f*x+e)))/f^4-18/f^2*b*a^2*c^2*d*e*ln(exp(I*(f*x+e)))+36/
f^3*b^2*a*c*d^2*e*ln(exp(I*(f*x+e)))-18*I/f*b^2*a*c*d^2*x^2-3/f*b*a^2*c^3*1
n(exp(2*I*(f*x+e))+1)+6/f^3*b^3*c*d^2*ln(exp(I*(f*x+e)))-3/f^3*b^3*c*d^2*ln
(exp(2*I*(f*x+e))+1)+3/2/f^3*b^3*c*d^2*polylog(3,-exp(2*I*(f*x+e)))+3*I/f^2
*b^3*d^3*x^2-3/2*I/f^4*b^3*d^3*e^4+3*I/f^4*b^3*d^3*e^2+3/2/f^3*b^3*d^3*poly
log(3,-exp(2*I*(f*x+e)))*x-3/f^3*b^3*d^3*ln(exp(2*I*(f*x+e))+1)*x+2/f^4*b^3
*d^3*e^3*ln(exp(I*(f*x+e)))-6/f^4*b^3*d^3*e*ln(exp(I*(f*x+e)))+6/f*b*a^2*c^
3*ln(exp(I*(f*x+e)))+3/f*b^3*ln(exp(2*I*(f*x+e))+1)*c*d^2*x^2+3/f*b^3*ln(ex
p(2*I*(f*x+e))+1)*c^2*d*x-9/2/f^3*b*a^2*d^3*polylog(3,-exp(2*I*(f*x+e)))*x+
9/f^2*b^2*a*c^2*d*ln(exp(2*I*(f*x+e))+1)+6/f^2*b^3*c^2*d*e*ln(exp(I*(f*x+e)
))-3/2*I/f^2*b^3*c^2*d*polylog(2,-exp(2*I*(f*x+e)))-3/2*I/f^2*b^3*d^3*polyl
og(2,-exp(2*I*(f*x+e)))*x^2+12*I/f^4*b^2*a*d^3*e^3-3*I/f^2*b^3*c^2*d*e^2-6*
I/f*b^2*d^3*a*x^3-2*I/f^3*b^3*d^3*e^3*x+6*I/f^3*b^3*d^3*e*x+9/2*I/f^4*b*a^2
*d^3*e^4+4*I/f^3*b^3*c*d^2*e^3-3/f*b*a^2*d^3*ln(exp(2*I*(f*x+e))+1)*x^3+18/
f^3*b*a^2*c*d^2*e^2*ln(exp(I*(f*x+e)))+6*I/f^2*b^3*c*d^2*e^2*x-9*I/f^3*b^2*
a*d^3*polylog(2,-exp(2*I*(f*x+e)))*x-9*I/f^3*b^2*a*c*d^2*polylog(2,-exp(2*I
*(f*x+e)))+9/2*I/f^2*b*a^2*c^2*d*polylog(2,-exp(2*I*(f*x+e)))-3*I/f^2*b^3*p
olylog(2,-exp(2*I*(f*x+e)))*c*d^2*x+9/2*I/f^2*b*a^2*d^3*polylog(2,-exp(2*I*
(f*x+e)))*x^2-6*I/f*b^3*c^2*d*e*x+18*I/f^3*b^2*a*d^3*e^2*x-18*I/f^3*b^2*a*c
*d^2*e^2+9*I/f^2*b*a^2*c^2*d*e^2+6*I/f^3*b*a^2*d^3*e^3*x-12*I/f^3*b*a^2*c*d
^2*e^3+1/4*a^3*d^3*x^4+a^3*c^3*x-3*a*b^2*c*d^2*x^3-9/2*a*b^2*c^2*d*x^2-3*I*
a^2*b*c^3*x+3*I*a^2*b*c*d^2*x^3+9/2*I*a^2*b*c^2*d*x^2-9/4*I*a^2*b*d^3*polyl
og(4,-exp(2*I*(f*x+e)))/f^4
```

maxima [B] time = 23.83, size = 6819, normalized size = 11.14

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*(a+b*tan(f*x+e))^3,x, algorithm="maxima")
```

```
[Out] 1/4*(4*(f*x + e)*a^3*c^3 + (f*x + e)^4*a^3*d^3/f^3 - 4*(f*x + e)^3*a^3*d^3*
e/f^3 + 6*(f*x + e)^2*a^3*d^3*e^2/f^3 - 4*(f*x + e)*a^3*d^3*e^3/f^3 + 4*(f*
x + e)^3*a^3*c*d^2/f^2 - 12*(f*x + e)^2*a^3*c*d^2*e/f^2 + 12*(f*x + e)*a^3*
c*d^2*e^2/f^2 + 6*(f*x + e)^2*a^3*c^2*d/f - 12*(f*x + e)*a^3*c^2*d*e/f + 12
*a^2*b*c^3*log(sec(f*x + e)) - 12*a^2*b*d^3*e^3*log(sec(f*x + e))/f^3 + 36*
a^2*b*c*d^2*e^2*log(sec(f*x + e))/f^2 - 36*a^2*b*c^2*d*e*log(sec(f*x + e))/
f - 4*(72*a*b^2*d^3*e^3 - 72*a*b^2*c^3*f^3 - (9*a^2*b + 9*I*a*b^2 - 3*b^3)*
(f*x + e)^4*d^3 + 36*b^3*d^3*e^2 + ((36*a^2*b + 36*I*a*b^2 - 12*b^3)*d^3*e
- (36*a^2*b + 36*I*a*b^2 - 12*b^3)*c*d^2*f)*(f*x + e)^3 - ((54*a^2*b + 54*I
*a*b^2 - 18*b^3)*d^3*e^2 - (108*a^2*b + 108*I*a*b^2 - 36*b^3)*c*d^2*e*f + (
54*a^2*b + 54*I*a*b^2 - 18*b^3)*c^2*d*f^2)*(f*x + e)^2 + 36*(6*a*b^2*c^2*d*
e + b^3*c^2*d)*f^2 - ((-36*I*a*b^2 + 12*b^3)*d^3*e^3 + (108*I*a*b^2 - 36*b^
3)*c*d^2*e^2*f + (-108*I*a*b^2 + 36*b^3)*c^2*d*e*f^2 + (36*I*a*b^2 - 12*b^3
)*c^3*f^3)*(f*x + e) - 72*(3*a*b^2*c*d^2*e^2 + b^3*c*d^2*e)*f + (12*b^3*d^3
*e^3 - 12*b^3*c^3*f^3 - 108*a*b^2*d^3*e^2 + 16*(3*a^2*b - b^3)*(f*x + e)^3*
d^3 - 36*b^3*d^3*e - 36*(3*a*b^2*d^3 + (3*a^2*b - b^3)*d^3*e - (3*a^2*b - b
^3)*c*d^2*f)*(f*x + e)^2 + 36*(b^3*c^2*d*e - 3*a*b^2*c^2*d)*f^2 + 36*(6*a*b
^2*d^3*e + b^3*d^3 + (3*a^2*b - b^3)*d^3*e^2 + (3*a^2*b - b^3)*c^2*d*f^2 -
2*(3*a*b^2*c*d^2 + (3*a^2*b - b^3)*c*d^2*e)*f*(f*x + e) - 36*(b^3*c*d^2*e^
2 - 6*a*b^2*c*d^2*e - b^3*c*d^2)*f + 4*(3*b^3*d^3*e^3 - 3*b^3*c^3*f^3 - 27*
a*b^2*d^3*e^2 + 4*(3*a^2*b - b^3)*(f*x + e)^3*d^3 - 9*b^3*d^3*e - 9*(3*a*b^
2*d^3 + (3*a^2*b - b^3)*d^3*e - (3*a^2*b - b^3)*c*d^2*f)*(f*x + e)^2 + 9*(b
^3*c^2*d*e - 3*a*b^2*c^2*d)*f^2 + 9*(6*a*b^2*d^3*e + b^3*d^3 + (3*a^2*b - b
^3)*d^3*e^2 + (3*a^2*b - b^3)*c^2*d*f^2 - 2*(3*a*b^2*c*d^2 + (3*a^2*b - b^3
)*c*d^2*e)*f*(f*x + e) - 9*(b^3*c*d^2*e^2 - 6*a*b^2*c*d^2*e - b^3*c*d^2)*f
)*cos(4*f*x + 4*e) + 8*(3*b^3*d^3*e^3 - 3*b^3*c^3*f^3 - 27*a*b^2*d^3*e^2 +
4*(3*a^2*b - b^3)*(f*x + e)^3*d^3 - 9*b^3*d^3*e - 9*(3*a*b^2*d^3 + (3*a^2*b
- b^3)*d^3*e - (3*a^2*b - b^3)*c*d^2*f)*(f*x + e)^2 + 9*(b^3*c^2*d*e - 3*a
```

$$\begin{aligned}
& *b^2*c^2*d)*f^2 + 9*(6*a*b^2*d^3*e + b^3*d^3 + (3*a^2*b - b^3)*d^3*e^2 + (3 \\
& *a^2*b - b^3)*c^2*d*f^2 - 2*(3*a*b^2*c*d^2 + (3*a^2*b - b^3)*c*d^2*e)*f)*(f \\
& *x + e) - 9*(b^3*c*d^2*e^2 - 6*a*b^2*c*d^2*e - b^3*c*d^2)*f)*\cos(2*f*x + 2* \\
& e) - (-12*I*b^3*d^3*e^3 + 12*I*b^3*c^3*f^3 + 108*I*a*b^2*d^3*e^2 + (-48*I*a \\
& ^2*b + 16*I*b^3)*(f*x + e)^3*d^3 + 36*I*b^3*d^3*e + (108*I*a*b^2*d^3 + (108 \\
& *I*a^2*b - 36*I*b^3)*d^3*e + (-108*I*a^2*b + 36*I*b^3)*c*d^2*f)*(f*x + e)^2 \\
& + (-36*I*b^3*c^2*d*e + 108*I*a*b^2*c^2*d)*f^2 + (-216*I*a*b^2*d^3*e - 36*I \\
& *b^3*d^3 + (-108*I*a^2*b + 36*I*b^3)*d^3*e^2 + (-108*I*a^2*b + 36*I*b^3)*c^ \\
& 2*d*f^2 + (216*I*a*b^2*c*d^2 + (216*I*a^2*b - 72*I*b^3)*c*d^2*e)*f)*(f*x + \\
& e) + (36*I*b^3*c*d^2*e^2 - 216*I*a*b^2*c*d^2*e - 36*I*b^3*c*d^2)*f)*\sin(4*f \\
& *x + 4*e) - (-24*I*b^3*d^3*e^3 + 24*I*b^3*c^3*f^3 + 216*I*a*b^2*d^3*e^2 + (\\
& -96*I*a^2*b + 32*I*b^3)*(f*x + e)^3*d^3 + 72*I*b^3*d^3*e + (216*I*a*b^2*d^3 \\
& + (216*I*a^2*b - 72*I*b^3)*d^3*e + (-216*I*a^2*b + 72*I*b^3)*c*d^2*f)*(f*x \\
& + e)^2 + (-72*I*b^3*c^2*d*e + 216*I*a*b^2*c^2*d)*f^2 + (-432*I*a*b^2*d^3*e \\
& - 72*I*b^3*d^3 + (-216*I*a^2*b + 72*I*b^3)*d^3*e^2 + (-216*I*a^2*b + 72*I \\
& *b^3)*c^2*d*f^2 + (432*I*a*b^2*c*d^2 + (432*I*a^2*b - 144*I*b^3)*c*d^2*e)*f) \\
& *(f*x + e) + (72*I*b^3*c*d^2*e^2 - 432*I*a*b^2*c*d^2*e - 72*I*b^3*c*d^2)*f) \\
& *\sin(2*f*x + 2*e))*\arctan2(\sin(2*f*x + 2*e), \cos(2*f*x + 2*e) + 1) - ((9*a^ \\
& 2*b + 9*I*a*b^2 - 3*b^3)*(f*x + e)^4*d^3 - (72*a*b^2*d^3 + (36*a^2*b + 36*I \\
& *a*b^2 - 12*b^3)*d^3*e - (36*a^2*b + 36*I*a*b^2 - 12*b^3)*c*d^2*f)*(f*x + e \\
&)^3 + (216*a*b^2*d^3*e + 36*b^3*d^3 + (54*a^2*b + 54*I*a*b^2 - 18*b^3)*d^3* \\
& e^2 + (54*a^2*b + 54*I*a*b^2 - 18*b^3)*c^2*d*f^2 - (216*a*b^2*c*d^2 + (108* \\
& a^2*b + 108*I*a*b^2 - 36*b^3)*c*d^2*e)*f)*(f*x + e)^2 - (216*a*b^2*d^3*e^2 \\
& + 72*b^3*d^3*e - (-36*I*a*b^2 + 12*b^3)*d^3*e^3 - (36*I*a*b^2 - 12*b^3)*c^3 \\
& *f^3 + (216*a*b^2*c^2*d - (-108*I*a*b^2 + 36*b^3)*c^2*d*e)*f^2 - (432*a*b^2 \\
& *c*d^2*e + 72*b^3*c*d^2 + (108*I*a*b^2 - 36*b^3)*c*d^2*e^2)*f)*(f*x + e))*c \\
& \os(4*f*x + 4*e) - ((18*a^2*b + 18*I*a*b^2 - 6*b^3)*(f*x + e)^4*d^3 - 36*b^3 \\
& *d^3*e^2 - 24*(3*a*b^2 - I*b^3)*d^3*e^3 + 24*(3*a*b^2 - I*b^3)*c^3*f^3 - ((\\
& 72*a^2*b + 72*I*a*b^2 - 24*b^3)*d^3*e - (72*a^2*b + 72*I*a*b^2 - 24*b^3)*c* \\
& d^2*f + 24*(3*a*b^2 + I*b^3)*d^3)*(f*x + e)^3 + (36*b^3*d^3 + (108*a^2*b + \\
& 108*I*a*b^2 - 36*b^3)*d^3*e^2 + (108*a^2*b + 108*I*a*b^2 - 36*b^3)*c^2*d*f^ \\
& 2 + 72*(3*a*b^2 + I*b^3)*d^3*e - ((216*a^2*b + 216*I*a*b^2 - 72*b^3)*c*d^2* \\
& e + 72*(3*a*b^2 + I*b^3)*c*d^2)*f)*(f*x + e)^2 - 36*(b^3*c^2*d + 2*(3*a*b^2 \\
& - I*b^3)*c^2*d*e)*f^2 - (72*b^3*d^3*e - (-72*I*a*b^2 + 24*b^3)*d^3*e^3 - (\\
& 72*I*a*b^2 - 24*b^3)*c^3*f^3 + 72*(3*a*b^2 + I*b^3)*d^3*e^2 - ((-216*I*a*b^ \\
& 2 + 72*b^3)*c^2*d*e - 72*(3*a*b^2 + I*b^3)*c^2*d)*f^2 - (72*b^3*c*d^2 + (21 \\
& 6*I*a*b^2 - 72*b^3)*c*d^2*e^2 + 144*(3*a*b^2 + I*b^3)*c*d^2*e)*f)*(f*x + e) \\
& + 72*(b^3*c*d^2*e + (3*a*b^2 - I*b^3)*c*d^2*e^2)*f)*\cos(2*f*x + 2*e) - (10 \\
& 8*a*b^2*d^3*e + 24*(3*a^2*b - b^3)*(f*x + e)^2*d^3 + 18*b^3*d^3 + 18*(3*a^2 \\
& *b - b^3)*d^3*e^2 + 18*(3*a^2*b - b^3)*c^2*d*f^2 - 36*(3*a*b^2*d^3 + (3*a^2 \\
& *b - b^3)*d^3*e - (3*a^2*b - b^3)*c*d^2*f)*(f*x + e) - 36*(3*a*b^2*c*d^2 + \\
& (3*a^2*b - b^3)*c*d^2*e)*f + 6*(18*a*b^2*d^3*e + 4*(3*a^2*b - b^3)*(f*x + e \\
&)^2*d^3 + 3*b^3*d^3 + 3*(3*a^2*b - b^3)*d^3*e^2 + 3*(3*a^2*b - b^3)*c^2*d*f \\
& ^2 - 6*(3*a*b^2*d^3 + (3*a^2*b - b^3)*d^3*e - (3*a^2*b - b^3)*c*d^2*f)*(f*x \\
& + e) - 6*(3*a*b^2*c*d^2 + (3*a^2*b - b^3)*c*d^2*e)*f)*\cos(4*f*x + 4*e) + 1 \\
& 2*(18*a*b^2*d^3*e + 4*(3*a^2*b - b^3)*(f*x + e)^2*d^3 + 3*b^3*d^3 + 3*(3*a^ \\
& 2*b - b^3)*d^3*e^2 + 3*(3*a^2*b - b^3)*c^2*d*f^2 - 6*(3*a*b^2*d^3 + (3*a^2* \\
& b - b^3)*d^3*e - (3*a^2*b - b^3)*c*d^2*f)*(f*x + e) - 6*(3*a*b^2*c*d^2 + (3 \\
& *a^2*b - b^3)*c*d^2*e)*f)*\cos(2*f*x + 2*e) + (108*I*a*b^2*d^3*e + (72*I*a^2 \\
& *b - 24*I*b^3)*(f*x + e)^2*d^3 + 18*I*b^3*d^3 + (54*I*a^2*b - 18*I*b^3)*d^3 \\
& *e^2 + (54*I*a^2*b - 18*I*b^3)*c^2*d*f^2 + (-108*I*a*b^2*d^3 + (-108*I*a^2* \\
& b + 36*I*b^3)*d^3*e + (108*I*a^2*b - 36*I*b^3)*c*d^2*f)*(f*x + e) + (-108*I \\
& *a*b^2*c*d^2 + (-108*I*a^2*b + 36*I*b^3)*c*d^2*e)*f)*\sin(4*f*x + 4*e) + (21 \\
& 6*I*a*b^2*d^3*e + (144*I*a^2*b - 48*I*b^3)*(f*x + e)^2*d^3 + 36*I*b^3*d^3 + \\
& (108*I*a^2*b - 36*I*b^3)*d^3*e^2 + (108*I*a^2*b - 36*I*b^3)*c^2*d*f^2 + (- \\
& 216*I*a*b^2*d^3 + (-216*I*a^2*b + 72*I*b^3)*d^3*e + (216*I*a^2*b - 72*I*b^3 \\
&)*c*d^2*f)*(f*x + e) + (-216*I*a*b^2*c*d^2 + (-216*I*a^2*b + 72*I*b^3)*c*d^ \\
& 2*e)*f)*\sin(2*f*x + 2*e))*\operatorname{dilog}(-e^{(2*I*f*x + 2*I*e)}) - (6*I*b^3*d^3*e^3 - \\
& 6*I*b^3*c^3*f^3 - 54*I*a*b^2*d^3*e^2 + (24*I*a^2*b - 8*I*b^3)*(f*x + e)^3*d
\end{aligned}$$

$$\begin{aligned}
&^3 - 18I*b^3*d^3*e + (-54I*a*b^2*d^3 + (-54I*a^2*b + 18I*b^3)*d^3*e + (\\
&54I*a^2*b - 18I*b^3)*c*d^2*f)*(f*x + e)^2 + (18I*b^3*c^2*d*e - 54I*a*b^ \\
&2*c^2*d)*f^2 + (108I*a*b^2*d^3*e + 18I*b^3*d^3 + (54I*a^2*b - 18I*b^3)* \\
&d^3*e^2 + (54I*a^2*b - 18I*b^3)*c^2*d*f^2 + (-108I*a*b^2*c*d^2 + (-108I \\
&a^2*b + 36I*b^3)*c*d^2*e)*f)*(f*x + e) + (-18I*b^3*c*d^2*e^2 + 108I*a*b \\
&^2*c*d^2*e + 18I*b^3*c*d^2)*f + (6I*b^3*d^3*e^3 - 6I*b^3*c^3*f^3 - 54I* \\
&a*b^2*d^3*e^2 + (24I*a^2*b - 8I*b^3)*(f*x + e)^3*d^3 - 18I*b^3*d^3*e + (\\
&-54I*a*b^2*d^3 + (-54I*a^2*b + 18I*b^3)*d^3*e + (54I*a^2*b - 18I*b^3)* \\
&c*d^2*f)*(f*x + e)^2 + (18I*b^3*c^2*d*e - 54I*a*b^2*c^2*d)*f^2 + (108I*a \\
&b^2*d^3*e + 18I*b^3*d^3 + (54I*a^2*b - 18I*b^3)*d^3*e^2 + (54I*a^2*b - \\
&18I*b^3)*c^2*d*f^2 + (-108I*a*b^2*c*d^2 + (-108I*a^2*b + 36I*b^3)*c*d^ \\
&2*e)*f)*(f*x + e) + (-18I*b^3*c*d^2*e^2 + 108I*a*b^2*c*d^2*e + 18I*b^3*c \\
&d^2)*f)*\cos(4*f*x + 4*e) + (12I*b^3*d^3*e^3 - 12I*b^3*c^3*f^3 - 108I*a* \\
&b^2*d^3*e^2 + (48I*a^2*b - 16I*b^3)*(f*x + e)^3*d^3 - 36I*b^3*d^3*e + (- \\
&108I*a*b^2*d^3 + (-108I*a^2*b + 36I*b^3)*d^3*e + (108I*a^2*b - 36I*b^3 \\
&))*c*d^2*f)*(f*x + e)^2 + (36I*b^3*c^2*d*e - 108I*a*b^2*c^2*d)*f^2 + (216* \\
&I*a*b^2*d^3*e + 36I*b^3*d^3 + (108I*a^2*b - 36I*b^3)*d^3*e^2 + (108I*a^ \\
&2*b - 36I*b^3)*c^2*d*f^2 + (-216I*a*b^2*c*d^2 + (-216I*a^2*b + 72I*b^3) \\
&)*c*d^2*e)*f)*(f*x + e) + (-36I*b^3*c*d^2*e^2 + 216I*a*b^2*c*d^2*e + 36I* \\
&b^3*c*d^2)*f)*\cos(2*f*x + 2*e) - 2*(3*b^3*d^3*e^3 - 3*b^3*c^3*f^3 - 27*a*b^ \\
&2*d^3*e^2 + 4*(3*a^2*b - b^3)*(f*x + e)^3*d^3 - 9*b^3*d^3*e - 9*(3*a*b^2*d^ \\
&3 + (3*a^2*b - b^3)*d^3*e - (3*a^2*b - b^3)*c*d^2*f)*(f*x + e)^2 + 9*(b^3*c \\
&^2*d*e - 3*a*b^2*c^2*d)*f^2 + 9*(6*a*b^2*d^3*e + b^3*d^3 + (3*a^2*b - b^3)* \\
&d^3*e^2 + (3*a^2*b - b^3)*c^2*d*f^2 - 2*(3*a*b^2*c*d^2 + (3*a^2*b - b^3)*c* \\
&d^2*e)*f)*(f*x + e) - 9*(b^3*c*d^2*e^2 - 6*a*b^2*c*d^2*e - b^3*c*d^2)*f)*\si \\
&n(4*f*x + 4*e) - 4*(3*b^3*d^3*e^3 - 3*b^3*c^3*f^3 - 27*a*b^2*d^3*e^2 + 4*(3 \\
&a^2*b - b^3)*(f*x + e)^3*d^3 - 9*b^3*d^3*e - 9*(3*a*b^2*d^3 + (3*a^2*b - b \\
&^3)*d^3*e - (3*a^2*b - b^3)*c*d^2*f)*(f*x + e)^2 + 9*(b^3*c^2*d*e - 3*a*b^2 \\
&)*c^2*d)*f^2 + 9*(6*a*b^2*d^3*e + b^3*d^3 + (3*a^2*b - b^3)*d^3*e^2 + (3*a^2 \\
&)*b - b^3)*c^2*d*f^2 - 2*(3*a*b^2*c*d^2 + (3*a^2*b - b^3)*c*d^2*e)*f)*(f*x + \\
&e) - 9*(b^3*c*d^2*e^2 - 6*a*b^2*c*d^2*e - b^3*c*d^2)*f)*\sin(2*f*x + 2*e))* \\
&\log(\cos(2*f*x + 2*e)^2 + \sin(2*f*x + 2*e)^2 + 2*\cos(2*f*x + 2*e) + 1) + (12 \\
&)*(3*a^2*b - b^3)*d^3*\cos(4*f*x + 4*e) + 24*(3*a^2*b - b^3)*d^3*\cos(2*f*x + \\
&2*e) - (-36I*a^2*b + 12I*b^3)*d^3*\sin(4*f*x + 4*e) - (-72I*a^2*b + 24I* \\
&b^3)*d^3*\sin(2*f*x + 2*e) + 12*(3*a^2*b - b^3)*d^3)*\text{polylog}(4, -e^{(2I*f*x \\
&+ 2I*e)}) - (-54I*a*b^2*d^3 + (72I*a^2*b - 24I*b^3)*(f*x + e)*d^3 + (-54 \\
&I*a^2*b + 18I*b^3)*d^3*e + (54I*a^2*b - 18I*b^3)*c*d^2*f + (-54I*a*b^2 \\
&d^3 + (72I*a^2*b - 24I*b^3)*(f*x + e)*d^3 + (-54I*a^2*b + 18I*b^3)*d^3 \\
&*e + (54I*a^2*b - 18I*b^3)*c*d^2*f)*\cos(4*f*x + 4*e) + (-108I*a*b^2*d^3 \\
&+ (144I*a^2*b - 48I*b^3)*(f*x + e)*d^3 + (-108I*a^2*b + 36I*b^3)*d^3*e \\
&+ (108I*a^2*b - 36I*b^3)*c*d^2*f)*\cos(2*f*x + 2*e) + 6*(9*a*b^2*d^3 - 4*(\\
&3*a^2*b - b^3)*(f*x + e)*d^3 + 3*(3*a^2*b - b^3)*d^3*e - 3*(3*a^2*b - b^3)* \\
&c*d^2*f)*\sin(4*f*x + 4*e) + 12*(9*a*b^2*d^3 - 4*(3*a^2*b - b^3)*(f*x + e)*d \\
&^3 + 3*(3*a^2*b - b^3)*d^3*e - 3*(3*a^2*b - b^3)*c*d^2*f)*\sin(2*f*x + 2*e)) \\
&)*\text{polylog}(3, -e^{(2I*f*x + 2I*e)}) - ((9I*a^2*b - 9*a*b^2 - 3I*b^3)*(f*x + \\
&e)^4*d^3 + (-72I*a*b^2*d^3 + (-36I*a^2*b + 36*a*b^2 + 12I*b^3)*d^3*e + \\
&(36I*a^2*b - 36*a*b^2 - 12I*b^3)*c*d^2*f)*(f*x + e)^3 + (216I*a*b^2*d^3* \\
&e + 36I*b^3*d^3 + (54I*a^2*b - 54*a*b^2 - 18I*b^3)*d^3*e^2 + (54I*a^2*b \\
&- 54*a*b^2 - 18I*b^3)*c^2*d*f^2 + (-216I*a*b^2*c*d^2 + (-108I*a^2*b + 1 \\
&08*a*b^2 + 36I*b^3)*c*d^2*e)*f)*(f*x + e)^2 + (-216I*a*b^2*d^3*e^2 - 72I \\
&)*b^3*d^3*e + 12*(3*a*b^2 + I*b^3)*d^3*e^3 - 12*(3*a*b^2 + I*b^3)*c^3*f^3 + \\
&(-216I*a*b^2*c^2*d + 36*(3*a*b^2 + I*b^3)*c^2*d*e)*f^2 + (432I*a*b^2*c*d^ \\
&2*e + 72I*b^3*c*d^2 - 36*(3*a*b^2 + I*b^3)*c*d^2*e^2)*f)*(f*x + e))*\sin(4* \\
&f*x + 4*e) - ((18I*a^2*b - 18*a*b^2 - 6I*b^3)*(f*x + e)^4*d^3 - 36I*b^3* \\
&d^3*e^2 + (-72I*a*b^2 - 24*b^3)*d^3*e^3 + (72I*a*b^2 + 24*b^3)*c^3*f^3 + \\
&((-72I*a^2*b + 72*a*b^2 + 24I*b^3)*d^3*e + (72I*a^2*b - 72*a*b^2 - 24I* \\
&b^3)*c*d^2*f + (-72I*a*b^2 + 24*b^3)*d^3)*(f*x + e)^3 + (36I*b^3*d^3 + (1 \\
&08I*a^2*b - 108*a*b^2 - 36I*b^3)*d^3*e^2 + (108I*a^2*b - 108*a*b^2 - 36* \\
&I*b^3)*c^2*d*f^2 + (216I*a*b^2 - 72*b^3)*d^3*e + ((-216I*a^2*b + 216*a*b^
\end{aligned}$$

$2 + 72I*b^3)*c*d^2*e + (-216I*a*b^2 + 72*b^3)*c*d^2)*f)*(f*x + e)^2 + (-36I*b^3*c^2*d + (-216I*a*b^2 - 72*b^3)*c^2*d*e)*f^2 + (-72I*b^3*d^3*e + 24*(3*a*b^2 + I*b^3)*d^3*e^3 - 24*(3*a*b^2 + I*b^3)*c^3*f^3 + (-216I*a*b^2 + 72*b^3)*d^3*e^2 + (72*(3*a*b^2 + I*b^3)*c^2*d*e + (-216I*a*b^2 + 72*b^3)*c^2*d)*f^2 + (72I*b^3*c*d^2 - 72*(3*a*b^2 + I*b^3)*c*d^2*e^2 + (432I*a*b^2 - 144*b^3)*c*d^2*e)*f)*(f*x + e) + (72I*b^3*c*d^2*e + (216I*a*b^2 + 72*b^3)*c*d^2*e^2)*f)*\sin(2*f*x + 2*e))/(-12I*f^3*\cos(4*f*x + 4*e) - 24I*f^3*\cos(2*f*x + 2*e) + 12*f^3*\sin(4*f*x + 4*e) + 24*f^3*\sin(2*f*x + 2*e) - 12*I*f^3))/f$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + b \tan(e + f x))^3 (c + d x)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^3*(c + d*x)^3,x)

[Out] int((a + b*tan(e + f*x))^3*(c + d*x)^3, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + f x))^3 (c + d x)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3*(a+b*tan(f*x+e))**3,x)

[Out] Integral((a + b*tan(e + f*x))**3*(c + d*x)**3, x)

3.50 $\int (c + dx)^2 (a + b \tan(e + fx))^3 dx$

Optimal. Leaf size=436

$$\frac{a^3(c + dx)^3}{3d} + \frac{3ia^2bd(c + dx)\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{3a^2b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{ia^2b(c + dx)^3}{d} - \frac{3a^2bd^2\text{Li}_3(-e^{2i(e+fx)})}{2f^3}$$

[Out] $b^3c*d*x/f + 1/2*b^3*d^2*x^2/f - 3*I*a*b^2*d^2*polylog(2, -exp(2*I*(f*x+e)))/f^3 + 1/3*a^3*(d*x+c)^3/d - 3*I*a*b^2*(d*x+c)^2/f - a*b^2*(d*x+c)^3/d - 1/3*I*b^3*(d*x+c)^3/d + 6*a*b^2*d*(d*x+c)*ln(1+exp(2*I*(f*x+e)))/f^2 - 3*a^2*b*(d*x+c)^2*ln(1+exp(2*I*(f*x+e)))/f + b^3*(d*x+c)^2*ln(1+exp(2*I*(f*x+e)))/f - b^3*d^2*ln(cos(f*x+e))/f^3 + 3*I*a^2*b*d*(d*x+c)*polylog(2, -exp(2*I*(f*x+e)))/f^2 + I*a^2*b*(d*x+c)^3/d - I*b^3*d*(d*x+c)*polylog(2, -exp(2*I*(f*x+e)))/f^2 - 3/2*a^2*b*d^2*polylog(3, -exp(2*I*(f*x+e)))/f^3 + 1/2*b^3*d^2*polylog(3, -exp(2*I*(f*x+e)))/f^3 - b^3*d*(d*x+c)*tan(f*x+e)/f^2 + 3*a*b^2*(d*x+c)^2*tan(f*x+e)/f + 1/2*b^3*(d*x+c)^2*tan(f*x+e)^2/f$

Rubi [A] time = 0.72, antiderivative size = 436, normalized size of antiderivative = 1.00, number of steps used = 22, number of rules used = 11, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.550$, Rules used = {3722, 3719, 2190, 2531, 2282, 6589, 3720, 2279, 2391, 32, 3475}

$$\frac{3ia^2bd(c + dx)\text{Li}_2(-e^{2i(e+fx)})}{f^2} - \frac{3a^2b(c + dx)^2 \log(1 + e^{2i(e+fx)})}{f} + \frac{ia^2b(c + dx)^3}{d} - \frac{3a^2bd^2\text{Li}_3(-e^{2i(e+fx)})}{2f^3} + \frac{a^3(c + dx)^3}{3d}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2*(a + b*Tan[e + f*x])^3,x]

[Out] $(b^3c*d*x)/f + (b^3*d^2*x^2)/(2*f) - ((3*I)*a*b^2*(c + d*x)^2)/f + (a^3*(c + d*x)^3)/(3*d) + (I*a^2*b*(c + d*x)^3)/d - (a*b^2*(c + d*x)^3)/d - ((I/3)*b^3*(c + d*x)^3)/d + (6*a*b^2*d*(c + d*x)*Log[1 + E^((2*I)*(e + f*x))])/f^2 - (3*a^2*b*(c + d*x)^2*Log[1 + E^((2*I)*(e + f*x))])/f + (b^3*(c + d*x)^2*Log[1 + E^((2*I)*(e + f*x))])/f - (b^3*d^2*Log[Cos[e + f*x]])/f^3 - ((3*I)*a*b^2*d^2*PolyLog[2, -E^((2*I)*(e + f*x))])/f^3 + ((3*I)*a^2*b*d*(c + d*x)*PolyLog[2, -E^((2*I)*(e + f*x))])/f^2 - (I*b^3*d*(c + d*x)*PolyLog[2, -E^((2*I)*(e + f*x))])/f^2 - (3*a^2*b*d^2*PolyLog[3, -E^((2*I)*(e + f*x))])/(2*f^3) + (b^3*d^2*PolyLog[3, -E^((2*I)*(e + f*x))])/(2*f^3) - (b^3*d*(c + d*x)*Tan[e + f*x])/f^2 + (3*a*b^2*(c + d*x)^2*Tan[e + f*x])/f + (b^3*(c + d*x)^2*Tan[e + f*x]^2)/(2*f)$

Rule 32

Int[((a_.) + (b_.)*(x_))^(m_), x_Symbol] := Simp[(a + b*x)^(m + 1)/(b*(m + 1)), x] /; FreeQ[{a, b, m}, x] && NeQ[m, -1]

Rule 2190

Int[(((F_)^(g_.)*((e_.) + (f_.)*(x_)))^(n_.)*((c_.) + (d_.)*(x_))^(m_.))/((a_.) + (b_.)*((F_)^(g_.)*((e_.) + (f_.)*(x_)))^(n_.)), x_Symbol] := Simp[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_.) + (b_.)*((F_)^(e_.)*((c_.) + (d_.)*(x_)))^(n_.)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2282

```
Int[u_, x_Symbol] :=> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x],
Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_.) + (b_.)*x))*(F_)[v_]] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 2391

```
Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] :=> -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 2531

```
Int[Log[1 + (e_)*((F_)^((c_)*((a_.) + (b_.)*(x_))))^(n_)]*((f_.) + (g_.)*(x_))^(m_), x_Symbol] :=> -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x))))^n])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m-1)*PolyLog[2, -(e*(F^(c*(a + b*x))))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]
```

Rule 3475

```
Int[tan[(c_.) + (d_.)*(x_)], x_Symbol] :=> -Simp[Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]
```

Rule 3719

```
Int[((c_.) + (d_.)*(x_))^(m_)*tan[(e_.) + (f_.)*(x_)], x_Symbol] :=> Simp[(I*(c + d*x)^(m+1))/(d*(m+1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 3720

```
Int[((c_.) + (d_.)*(x_))^(m_)*((b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] :=> Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n-1))/(f*(n-1)), x] + (-Dist[(b*d*m)/(f*(n-1)), Int[(c + d*x)^(m-1)*(b*Tan[e + f*x])^(n-1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n-2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]
```

Rule 3722

```
Int[((c_.) + (d_.)*(x_))^(m_)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] :=> Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 6589

```
Int[PolyLog[n_, (c_)*((a_.) + (b_.)*(x_))^(p_)]/((d_.) + (e_.)*(x_)), x_Symbol] :=> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned}
\int (c + dx)^2(a + b \tan(e + fx))^3 dx &= \int (a^3(c + dx)^2 + 3a^2b(c + dx)^2 \tan(e + fx) + 3ab^2(c + dx)^2 \tan^2(e + fx) + \\
&= \frac{a^3(c + dx)^3}{3d} + (3a^2b) \int (c + dx)^2 \tan(e + fx) dx + (3ab^2) \int (c + dx)^2 \tan^2(e + fx) dx \\
&= \frac{a^3(c + dx)^3}{3d} + \frac{ia^2b(c + dx)^3}{d} + \frac{3ab^2(c + dx)^2 \tan(e + fx)}{f} + \frac{b^3(c + dx)^2 \tan^2(e + fx)}{2f} \\
&= -\frac{3iab^2(c + dx)^2}{f} + \frac{a^3(c + dx)^3}{3d} + \frac{ia^2b(c + dx)^3}{d} - \frac{ab^2(c + dx)^3}{d} - \frac{ib^3(c + dx)^2}{3d} \\
&= \frac{b^3cdx}{f} + \frac{b^3d^2x^2}{2f} - \frac{3iab^2(c + dx)^2}{f} + \frac{a^3(c + dx)^3}{3d} + \frac{ia^2b(c + dx)^3}{d} - \frac{ab^2(c + dx)^3}{d} \\
&= \frac{b^3cdx}{f} + \frac{b^3d^2x^2}{2f} - \frac{3iab^2(c + dx)^2}{f} + \frac{a^3(c + dx)^3}{3d} + \frac{ia^2b(c + dx)^3}{d} - \frac{ab^2(c + dx)^3}{d} \\
&= \frac{b^3cdx}{f} + \frac{b^3d^2x^2}{2f} - \frac{3iab^2(c + dx)^2}{f} + \frac{a^3(c + dx)^3}{3d} + \frac{ia^2b(c + dx)^3}{d} - \frac{ab^2(c + dx)^3}{d} \\
&= \frac{b^3cdx}{f} + \frac{b^3d^2x^2}{2f} - \frac{3iab^2(c + dx)^2}{f} + \frac{a^3(c + dx)^3}{3d} + \frac{ia^2b(c + dx)^3}{d} - \frac{ab^2(c + dx)^3}{d}
\end{aligned}$$

Mathematica [B] time = 7.85, size = 1846, normalized size = 4.23

result too large to display

Warning: Unable to verify antiderivative.

[In] Integrate[(c + d*x)^2*(a + b*Tan[e + f*x])^3,x]

[Out] $((-1/4*I)*a^2*b*d^2*(2*f^2*x^2*(2*f*x - (3*I)*(1 + E^{((2*I)*e)}))*Log[1 + E^{((-2*I)*(e + f*x))}] + 6*(1 + E^{((2*I)*e)})*f*x*PolyLog[2, -E^{((-2*I)*(e + f*x))}] - (3*I)*(1 + E^{((2*I)*e)})*PolyLog[3, -E^{((-2*I)*(e + f*x))}])*Sec[e]/(E^{(I*e)*f^3} + ((I/12)*b^3*d^2*(2*f^2*x^2*(2*f*x - (3*I)*(1 + E^{((2*I)*e)}))*Log[1 + E^{((-2*I)*(e + f*x))}] + 6*(1 + E^{((2*I)*e)})*f*x*PolyLog[2, -E^{((-2*I)*(e + f*x))}] - (3*I)*(1 + E^{((2*I)*e)})*PolyLog[3, -E^{((-2*I)*(e + f*x))}])*Sec[e]/(E^{(I*e)*f^3} - (b^3*d^2*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f^3*(Cos[e]^2 + Sin[e]^2)) + (6*a*b^2*c*d*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f^2*(Cos[e]^2 + Sin[e]^2)) - (3*a^2*b*c^2*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f*(Cos[e]^2 + Sin[e]^2)) + (b^3*c^2*Sec[e]*(Cos[e]*Log[Cos[e]*Cos[f*x] - Sin[e]*Sin[f*x]] + f*x*Sin[e]))/(f*(Cos[e]^2 + Sin[e]^2)) + (3*a*b^2*d^2*Csc[e]*((f^2*x^2)/E^{(I*ArcTan[Cot[e]])}) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]]) - Pi*Log[1 + E^{((-2*I)*f*x}] - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^{((2*I)*(f*x - ArcTan[Cot[e]])}])) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]]) + I*PolyLog[2, E^{((2*I)*(f*x - ArcTan[Cot[e]])}))))/Sqrt[1 + Cot[e]^2])*Sec[e]/(f^3*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2)) - (3*a^2*b*c*d*Csc[e]*((f^2*x^2)/E^{(I*ArcTan[Cot[e]])}) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]]) - Pi*Log[1 + E^{((-2*I)*f*x}] - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^{((2*I)*(f*x - ArcTan[Cot[e]])}])) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]]) + I*PolyLog[2, E^{((2*I)*(f*x - ArcTan[Cot[e]])}))))/Sqrt[1 + Cot[e]^2])*Sec[e]/(f^2*Sqrt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2)) + (b^3*c*d*Csc[e]*((f^2*x^2)/E^{(I*ArcTan[Cot[e]])}) - (Cot[e]*(I*f*x*(-Pi - 2*ArcTan[Cot[e]]) - Pi*Log[1 + E^{((-2*I)*f*x}] - 2*(f*x - ArcTan[Cot[e]])*Log[1 - E^{((2*I)*(f*x - ArcTan[Cot[e]])}])) + Pi*Log[Cos[f*x]] - 2*ArcTan[Cot[e]]*Log[Sin[f*x - ArcTan[Cot[e]]]) + I*PolyLog[2, E^{((2*I)*(f*x - ArcTan[Cot[e]])}))))/Sqrt[1 + Cot[e]^2])*Sec[e]/(f^2*Sq$

```

rt[Csc[e]^2*(Cos[e]^2 + Sin[e]^2))] + (Sec[e]*Sec[e + f*x]^2*(6*b^3*c^2*f*Cos[e] + 12*b^3*c*d*f*x*Cos[e] + 6*a^3*c^2*f^2*x*Cos[e] - 18*a*b^2*c^2*f^2*x*Cos[e] + 6*b^3*d^2*f*x^2*Cos[e] + 6*a^3*c*d*f^2*x^2*Cos[e] - 18*a*b^2*c*d*f^2*x^2*Cos[e] + 2*a^3*d^2*f^2*x^3*Cos[e] - 6*a*b^2*d^2*f^2*x^3*Cos[e] + 3*a^3*c^2*f^2*x*Cos[e + 2*f*x] - 9*a*b^2*c^2*f^2*x*Cos[e + 2*f*x] + 3*a^3*c*d*f^2*x^2*Cos[e + 2*f*x] - 9*a*b^2*c*d*f^2*x^2*Cos[e + 2*f*x] + a^3*d^2*f^2*x^3*Cos[e + 2*f*x] - 3*a*b^2*d^2*f^2*x^3*Cos[e + 2*f*x] + 3*a^3*c^2*f^2*x*Cos[3*e + 2*f*x] - 9*a*b^2*c^2*f^2*x*Cos[3*e + 2*f*x] + 3*a^3*c*d*f^2*x^2*Cos[3*e + 2*f*x] - 9*a*b^2*c*d*f^2*x^2*Cos[3*e + 2*f*x] + a^3*d^2*f^2*x^3*Cos[3*e + 2*f*x] - 3*a*b^2*d^2*f^2*x^3*Cos[3*e + 2*f*x] + 6*b^3*c*d*Sin[e] - 18*a*b^2*c^2*f*Sin[e] + 6*b^3*d^2*x*Sin[e] - 36*a*b^2*c*d*f*x*Sin[e] + 18*a^2*b*c^2*f^2*x*Sin[e] - 6*b^3*c^2*f^2*x*Sin[e] - 18*a*b^2*d^2*f*x^2*Sin[e] + 18*a^2*b*c*d*f^2*x^2*Sin[e] - 6*b^3*c*d*f^2*x^2*Sin[e] + 6*a^2*b*d^2*f^2*x^3*Sin[e] - 2*b^3*d^2*f^2*x^3*Sin[e] - 6*b^3*c*d*Sin[e + 2*f*x] + 18*a*b^2*c^2*f*Sin[e + 2*f*x] - 6*b^3*d^2*x*Sin[e + 2*f*x] + 36*a*b^2*c*d*f*x*Sin[e + 2*f*x] - 9*a^2*b*c^2*f^2*x*Sin[e + 2*f*x] + 3*b^3*c^2*f^2*x*Sin[e + 2*f*x] + 18*a*b^2*d^2*f*x^2*Sin[e + 2*f*x] - 9*a^2*b*c*d*f^2*x^2*Sin[e + 2*f*x] + 3*b^3*c*d*f^2*x^2*Sin[e + 2*f*x] - 3*a^2*b*d^2*f^2*x^3*Sin[e + 2*f*x] + b^3*d^2*f^2*x^3*Sin[e + 2*f*x] + 9*a^2*b*c^2*f^2*x*Sin[3*e + 2*f*x] - 3*b^3*c^2*f^2*x*Sin[3*e + 2*f*x] + 9*a^2*b*c*d*f^2*x^2*Sin[3*e + 2*f*x] - 3*b^3*c*d*f^2*x^2*Sin[3*e + 2*f*x] + 3*a^2*b*d^2*f^2*x^3*Sin[3*e + 2*f*x] - b^3*d^2*f^2*x^3*Sin[3*e + 2*f*x]))/(12*f^2)

```

fricas [C] time = 0.54, size = 686, normalized size = 1.57

$$4(a^3 - 3ab^2)d^2f^3x^3 - 3(3a^2b - b^3)d^2\text{polylog}\left(3, \frac{\tan(fx+e)^2 + 2i \tan(fx+e) - 1}{\tan(fx+e)^2 + 1}\right) - 3(3a^2b - b^3)d^2\text{polylog}\left(3, \frac{\tan(fx+e)^2 + 2i \tan(fx+e) - 1}{\tan(fx+e)^2 + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*(a+b*tan(f*x+e))^3,x, algorithm="fricas")
```

```

[Out] 1/12*(4*(a^3 - 3*a*b^2)*d^2*f^3*x^3 - 3*(3*a^2*b - b^3)*d^2*polylog(3, (tan(f*x + e)^2 + 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 3*(3*a^2*b - b^3)*d^2*polylog(3, (tan(f*x + e)^2 - 2*I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) + 6*(b^3*d^2*f^2 + 2*(a^3 - 3*a*b^2)*c*d*f^3)*x^2 + 6*(b^3*d^2*f^2*x^2 + 2*b^3*c*d*f^2*x + b^3*c^2*f^2)*tan(f*x + e)^2 + 12*(b^3*c*d*f^2 + (a^3 - 3*a*b^2)*c^2*f^3)*x + (18*I*a*b^2*d^2 - 6*I*(3*a^2*b - b^3)*d^2*f*x - 6*I*(3*a^2*b - b^3)*c*d*f)*dilog(2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) + (-18*I*a*b^2*d^2 + 6*I*(3*a^2*b - b^3)*d^2*f*x + 6*I*(3*a^2*b - b^3)*c*d*f)*dilog(2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) - 6*((3*a^2*b - b^3)*d^2*f^2*x^2 - 6*a*b^2*c*d*f + b^3*d^2 + (3*a^2*b - b^3)*c^2*f^2 - 2*(3*a*b^2*d^2*f - (3*a^2*b - b^3)*c*d*f^2)*x)*log(-2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) - 6*((3*a^2*b - b^3)*d^2*f^2*x^2 - 6*a*b^2*c*d*f + b^3*d^2 + (3*a^2*b - b^3)*c^2*f^2 - 2*(3*a*b^2*d^2*f - (3*a^2*b - b^3)*c*d*f^2)*x)*log(-2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) + 12*(3*a*b^2*d^2*f^2*x^2 + 3*a*b^2*c^2*f^2 - b^3*c*d*f + (6*a*b^2*c*d*f^2 - b^3*d^2*f)*x)*tan(f*x + e))/f^3

```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)^2 (b \tan(fx + e) + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*(a+b*tan(f*x+e))^3,x, algorithm="giac")
```

```
[Out] integrate((d*x + c)^2*(b*tan(f*x + e) + a)^3, x)
```

maple [B] time = 0.84, size = 1090, normalized size = 2.50

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((d*x+c)^2*(a+b*\tan(f*x+e))^3,x)$

[Out]
$$\begin{aligned} & -3*a*b^2*c*d*x^2-1/3*I*b^3*d^2*x^3-12/f^2*b*a^2*c*d*e*\ln(\exp(I*(f*x+e)))-6/f \\ & *b*\ln(\exp(2*I*(f*x+e))+1)*a^2*c*d*x+3*I/f^2*b*a^2*c*d*\text{polylog}(2,-\exp(2*I*(f*x+e))) \\ & -12*I/f^2*b^2*a*d^2*e*x-4*I/f*b^3*c*d*e*x+3*I/f^2*b*\text{polylog}(2,-\exp(2*I*(f*x+e))) \\ & *a^2*d^2*x+6*I/f^2*b*a^2*c*d*e^2-6*I/f^2*b*a^2*d^2*e^2*x+a^3*c*d*x^2+12*I/f*b*a^2*c*d*e*x \\ & -2/f*b^3*c^2*\ln(\exp(I*(f*x+e)))+1/f*b^3*c^2*\ln(\exp(2*I*(f*x+e))+1)+2/f^3*b^3*d^2*\ln(\exp(I*(f*x+e))) \\ & -1/f^3*b^3*d^2*\ln(\exp(2*I*(f*x+e))+1)-I*b^3*c*d*x^2+I*b^3*c^2*x-a*b^2*d^2*x^3-3*b^2*a*c^2*x+2*b^2*(3*I*a*d^2*f*x^2*\exp(2*I*(f*x+e))+6*I*a*c*d*f*x*\exp(2*I*(f*x+e))+b*d^2*f*x^2*\exp(2*I*(f*x+e))+3*I*a*c^2*f*\exp(2*I*(f*x+e))+3*I*a*d^2*f*x^2-I*b*d^2*x*\exp(2*I*(f*x+e))+2*b*c*d*f*x*\exp(2*I*(f*x+e))+6*I*a*c*d*f*x-I*b*c*d*\exp(2*I*(f*x+e))+b*c^2*f*\exp(2*I*(f*x+e))+3*I*a*c^2*f-I*d^2*x*b-I*b*c*d)/f^2/(\exp(2*I*(f*x+e))+1)^2+I*a^2*b*d^2*x^3-3/2*a^2*b*d^2*\text{polylog}(3,-\exp(2*I*(f*x+e)))/f^3-2/f^3*b^3*d^2*e^2*\ln(\exp(I*(f*x+e)))+6/f*b*a^2*c^2*\ln(\exp(I*(f*x+e)))+1/3*a^3*d^2*x^3+a^3*c^2*x-3*I*a^2*b*c^2*x+3*I*a^2*b*c*d*x^2+4/f^2*b^3*c*d*e*\ln(\exp(I*(f*x+e)))-12/f^2*b^2*a*c*d*\ln(\exp(I*(f*x+e)))+6/f^2*b^2*a*c*d*\ln(\exp(2*I*(f*x+e))+1)+6/f^2*b^2*\ln(\exp(2*I*(f*x+e))+1)*a*d^2*x+2/f*b^3*\ln(\exp(2*I*(f*x+e))+1)*c*d*x-3/f*b*\ln(\exp(2*I*(f*x+e))+1)*a^2*d^2*x^2-6*I/f*b^2*a*d^2*x^2-2*I/f^2*b^3*c*d*e^2-3/f*b*a^2*c^2*\ln(\exp(2*I*(f*x+e))+1)+1/f*b^3*\ln(\exp(2*I*(f*x+e))+1)*d^2*x^2+4/3*I/f^3*b^3*d^2*e^3+6/f^3*b*a^2*d^2*e^2*\ln(\exp(I*(f*x+e)))-I/f^2*b^3*c*d*\text{polylog}(2,-\exp(2*I*(f*x+e)))-4*I/f^3*b*a^2*d^2*e^3-6*I/f^3*b^2*a*d^2*e^2-I/f^2*b^3*\text{polylog}(2,-\exp(2*I*(f*x+e)))*d^2*x+2*I/f^2*b^3*d^2*e^2*x+1/2*b^3*d^2*\text{polylog}(3,-\exp(2*I*(f*x+e)))/f^3+12/f^3*b^2*a*d^2*e*\ln(\exp(I*(f*x+e)))-3*I*a*b^2*d^2*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^3 \end{aligned}$$

maxima [B] time = 3.98, size = 3396, normalized size = 7.79

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x+c)^2*(a+b*\tan(f*x+e))^3,x, \text{algorithm}="maxima")$

[Out]
$$\begin{aligned} & 1/3*(3*(f*x + e)*a^3*c^2 + (f*x + e)^3*a^3*d^2/f^2 - 3*(f*x + e)^2*a^3*d^2*e/f^2 + 3*(f*x + e)*a^3*d^2*e^2/f^2 + 3*(f*x + e)^2*a^3*c*d/f - 6*(f*x + e) \\ & *a^3*c*d*e/f + 9*a^2*b*c^2*\log(\sec(f*x + e)) + 9*a^2*b*d^2*e^2*\log(\sec(f*x + e))/f^2 - 18*a^2*b*c*d*e*\log(\sec(f*x + e))/f + 3*(36*a*b^2*d^2*e^2 + 36*a \\ & *b^2*c^2*f^2 + (6*a^2*b + 6*I*a*b^2 - 2*b^3)*(f*x + e)^3*d^2 + 12*b^3*d^2*e - ((18*a^2*b + 18*I*a*b^2 - 6*b^3)*d^2*e - (18*a^2*b + 18*I*a*b^2 - 6*b^3) \\ & *c*d*f)*(f*x + e)^2 + ((18*I*a*b^2 - 6*b^3)*d^2*e^2 + (-36*I*a*b^2 + 12*b^3)*c*d*e*f + (18*I*a*b^2 - 6*b^3)*c^2*f^2)*(f*x + e) - 12*(6*a*b^2*c*d*e + b \\ & ^3*c*d)*f + (6*b^3*d^2*e^2 + 6*b^3*c^2*f^2 - 36*a*b^2*d^2*e - 6*(3*a^2*b - b^3)*(f*x + e)^2*d^2 - 6*b^3*d^2 + 12*(3*a*b^2*d^2 + (3*a^2*b - b^3)*d^2*e - (3*a^2*b - b^3)*c*d*f)*(f*x + e) - 12*(b^3*c*d*e - 3*a*b^2*c*d)*f + 6*(b^3*d^2*e^2 + b^3*c^2*f^2 - 6*a*b^2*d^2*e - (3*a^2*b - b^3)*(f*x + e)^2*d^2 - b^3*d^2 + 2*(3*a*b^2*d^2 + (3*a^2*b - b^3)*d^2*e - (3*a^2*b - b^3)*c*d*f)*(f*x + e) - 2*(b^3*c*d*e - 3*a*b^2*c*d)*f)*\cos(4*f*x + 4*e) + 12*(b^3*d^2*e^2 + b^3*c^2*f^2 - 6*a*b^2*d^2*e - (3*a^2*b - b^3)*(f*x + e)^2*d^2 - b^3*d^2 + 2*(3*a*b^2*d^2 + (3*a^2*b - b^3)*d^2*e - (3*a^2*b - b^3)*c*d*f)*(f*x + e) - 2*(b^3*c*d*e - 3*a*b^2*c*d)*f)*\cos(2*f*x + 2*e) + (6*I*b^3*d^2*e^2 + 6*I*b^3*c^2*f^2 - 36*I*a*b^2*d^2*e + (-18*I*a^2*b + 6*I*b^3)*(f*x + e)^2*d^2 - 6*I*b^3*d^2 + (36*I*a*b^2*d^2 + (36*I*a^2*b - 12*I*b^3)*d^2*e + (-36*I*a^2*b + 12*I*b^3)*c*d*f)*(f*x + e) + (-12*I*b^3*c*d*e + 36*I*a*b^2*c*d)*f)*\sin(4*f*x + 4*e) + (12*I*b^3*d^2*e^2 + 12*I*b^3*c^2*f^2 - 72*I*a*b^2*d^2*e + \end{aligned}$$

$$\begin{aligned}
& (-36Ia^2b + 12Ib^3)(fx + e)^2d^2 - 12Ib^3d^2 + (72Ia^2b^2d^2 \\
& + (72Ia^2b - 24Ib^3)d^2e + (-72Ia^2b + 24Ib^3)c^2d^2)(fx + e) \\
& + (-24Ib^3c^2d^2e + 72Ia^2b^2c^2d^2)(fx + e)\sin(2fx + 2e) \arctan2(\sin(2fx + 2e), \cos(2fx + 2e) + 1) + ((6a^2b + 6Ia^2b^2 - 2b^3)(fx + e)^3d^2 - (36a^2b^2d^2 + (18a^2b + 18Ia^2b^2 - 6b^3)d^2e - (18a^2b + 18Ia^2b^2 - 6b^3)c^2d^2)(fx + e)^2 + (72a^2b^2d^2e + 12b^3d^2 + (18Ia^2b^2 - 6b^3)d^2e^2 + (18Ia^2b^2 - 6b^3)c^2f^2 - (72a^2b^2c^2d - (-36Ia^2b^2 + 12b^3)c^2d^2e)(fx + e))\cos(4fx + 4e) + ((12a^2b + 12Ia^2b^2 - 4b^3)(fx + e)^3d^2 + 12b^3d^2e + 12(3a^2b^2 - Ib^3)d^2e^2 + 12(3a^2b^2 - Ib^3)c^2f^2 - ((36a^2b + 36Ia^2b^2 - 12b^3)d^2e - (36a^2b + 36Ia^2b^2 - 12b^3)c^2d^2f + 12(3a^2b^2 + Ib^3)d^2)(fx + e)^2 + (12b^3d^2 + (36Ia^2b^2 - 12b^3)d^2e^2 + (36Ia^2b^2 - 12b^3)c^2f^2 + 24(3a^2b^2 + Ib^3)d^2e + ((-72Ia^2b^2 + 24b^3)c^2d^2e - 24(3a^2b^2 + Ib^3)c^2d^2)(fx + e) - 12(b^3c^2d + 2(3a^2b^2 - Ib^3)c^2d^2e)(fx + e)\cos(2fx + 2e) - (18a^2b^2d^2 - 6(3a^2b - b^3)(fx + e)d^2 + 6(3a^2b - b^3)d^2e - 6(3a^2b - b^3)c^2d^2f + 6(3a^2b^2d^2 - (3a^2b - b^3)(fx + e)d^2 + (3a^2b - b^3)d^2e - (3a^2b - b^3)c^2d^2f)\cos(4fx + 4e) + 12(3a^2b^2d^2 - (3a^2b - b^3)(fx + e)d^2 + (3a^2b - b^3)d^2e - (3a^2b - b^3)c^2d^2f)\cos(2fx + 2e) - (-18Ia^2b^2d^2 + (18Ia^2b - 6Ib^3)(fx + e)d^2 + (-18Ia^2b + 6Ib^3)d^2e + (18Ia^2b - 6Ib^3)c^2d^2f)\sin(4fx + 4e) - (-36Ia^2b^2d^2 + (36Ia^2b - 12Ib^3)(fx + e)d^2 + (-36Ia^2b + 12Ib^3)d^2e + (36Ia^2b - 12Ib^3)c^2d^2f)\sin(2fx + 2e))\operatorname{dilog}(-e^{(2Ifx + 2Ie)}) + (-3Ib^3d^2e^2 - 3Ib^3c^2f^2 + 18Ia^2b^2d^2e + (9Ia^2b - 3Ib^3)(fx + e)^2d^2 + 3Ib^3d^2 + (-18Ia^2b^2d^2 + (-18Ia^2b + 6Ib^3)d^2e + (18Ia^2b - 6Ib^3)c^2d^2f)(fx + e) + (6Ib^3c^2d^2e - 18Ia^2b^2c^2d^2f + (-3Ib^3d^2e^2 - 3Ib^3c^2f^2 + 18Ia^2b^2d^2e + (9Ia^2b - 3Ib^3)(fx + e)^2d^2 + 3Ib^3d^2 + (-18Ia^2b^2d^2 + (-18Ia^2b + 6Ib^3)d^2e + (18Ia^2b - 6Ib^3)c^2d^2f)(fx + e) + (6Ib^3c^2d^2e - 18Ia^2b^2c^2d^2f)\cos(4fx + 4e) + (-6Ib^3d^2e^2 - 6Ib^3c^2f^2 + 36Ia^2b^2d^2e + (18Ia^2b - 6Ib^3)(fx + e)^2d^2 + 6Ib^3d^2 + (-36Ia^2b^2d^2 + (-36Ia^2b + 12Ib^3)d^2e + (36Ia^2b - 12Ib^3)c^2d^2f)(fx + e) + (12Ib^3c^2d^2e - 36Ia^2b^2c^2d^2f)\cos(2fx + 2e) + 3(b^3d^2e^2 + b^3c^2f^2 - 6a^2b^2d^2e - (3a^2b - b^3)(fx + e)^2d^2 - b^3d^2 + 2(3a^2b^2d^2 + (3a^2b - b^3)d^2e - (3a^2b - b^3)c^2d^2f)(fx + e) - 2(b^3c^2d^2e - 3a^2b^2c^2d^2f)\sin(4fx + 4e) + 6(b^3d^2e^2 + b^3c^2f^2 - 6a^2b^2d^2e - (3a^2b - b^3)(fx + e)^2d^2 - b^3d^2 + 2(3a^2b^2d^2 + (3a^2b - b^3)d^2e - (3a^2b - b^3)c^2d^2f)(fx + e) - 2(b^3c^2d^2e - 3a^2b^2c^2d^2f)\sin(2fx + 2e))\log(\cos(2fx + 2e)^2 + \sin(2fx + 2e)^2 + 2\cos(2fx + 2e) + 1) + ((9Ia^2b - 3Ib^3)d^2\cos(4fx + 4e) + (18Ia^2b - 6Ib^3)d^2\cos(2fx + 2e) - 3(3a^2b - b^3)d^2\sin(4fx + 4e) - 6(3a^2b - b^3)d^2\sin(2fx + 2e) + (9Ia^2b - 3Ib^3)d^2)\operatorname{polylog}(3, -e^{(2Ifx + 2Ie)}) + ((6Ia^2b - 6a^2b^2 - 2Ib^3)(fx + e)^3d^2 + (-36Ia^2b^2d^2 + (-18Ia^2b + 18a^2b^2 + 6Ib^3)d^2e + (18Ia^2b - 18a^2b^2 - 6Ib^3)c^2d^2f)(fx + e)^2 + (72Ia^2b^2d^2e + 12Ib^3d^2 - 6(3a^2b^2 + Ib^3)d^2e^2 - 6(3a^2b^2 + Ib^3)c^2f^2 + (-72Ia^2b^2c^2d + 12(3a^2b^2 + Ib^3)c^2d^2e)(fx + e))\sin(4fx + 4e) + ((12Ia^2b - 12a^2b^2 - 4Ib^3)(fx + e)^3d^2 + 12Ib^3d^2e + (36Ia^2b^2 + 12b^3)d^2e^2 + (36Ia^2b^2 + 12b^3)c^2f^2 + ((-36Ia^2b + 36a^2b^2 + 12Ib^3)d^2e + (36Ia^2b - 36a^2b^2 - 12Ib^3)c^2d^2f + (-36Ia^2b + 12b^3)d^2)(fx + e)^2 + (12Ib^3d^2 - 12(3a^2b^2 + Ib^3)d^2e^2 - 12(3a^2b^2 + Ib^3)c^2f^2 + (72Ia^2b^2 - 24b^3)d^2e + (24(3a^2b^2 + Ib^3)c^2d^2e + (-72Ia^2b^2 + 24b^3)c^2d^2)(fx + e) + (-12Ib^3c^2d + (-72Ia^2b^2 - 24b^3)c^2d^2e)(fx + e)\sin(2fx + 2e))/(-6If^2\cos(4fx + 4e) - 12If^2\cos(2fx + 2e) + 6f^2\sin(4fx + 4e) + 12f^2\sin(2fx + 2e) - 6If^2)/f
\end{aligned}$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + b \tan(e + f x))^3 (c + d x)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^3*(c + d*x)^2,x)

[Out] int((a + b*tan(e + f*x))^3*(c + d*x)^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + f x))^3 (c + d x)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2*(a+b*tan(f*x+e))**3,x)

[Out] Integral((a + b*tan(e + f*x))**3*(c + d*x)**2, x)

3.51 $\int (c + dx)(a + b \tan(e + fx))^3 dx$

Optimal. Leaf size=277

$$\frac{a^3(c + dx)^2}{2d} - \frac{3a^2b(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{3ia^2b(c + dx)^2}{2d} + \frac{3ia^2bd\text{Li}_2(-e^{2i(e+fx)})}{2f^2} + \frac{3ab^2(c + dx) \tan(e + fx)}{f}$$

[Out] $-3*a*b^2*c*x+1/2*b^3*d*x/f-3/2*a*b^2*d*x^2+1/2*a^3*(d*x+c)^2/d+3/2*I*a^2*b*(d*x+c)^2/d-1/2*I*b^3*(d*x+c)^2/d-3*a^2*b*(d*x+c)*\ln(1+\exp(2*I*(f*x+e)))/f+b^3*(d*x+c)*\ln(1+\exp(2*I*(f*x+e)))/f+3*a*b^2*d*\ln(\cos(f*x+e))/f^2+3/2*I*a^2*b*d*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^2-1/2*I*b^3*d*\text{polylog}(2,-\exp(2*I*(f*x+e)))/f^2-1/2*b^3*d*\tan(f*x+e)/f^2+3*a*b^2*(d*x+c)*\tan(f*x+e)/f+1/2*b^3*(d*x+c)*\tan(f*x+e)^2/f$

Rubi [A] time = 0.34, antiderivative size = 277, normalized size of antiderivative = 1.00, number of steps used = 16, number of rules used = 9, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3722, 3719, 2190, 2279, 2391, 3720, 3475, 3473, 8}

$$-\frac{3a^2b(c + dx) \log(1 + e^{2i(e+fx)})}{f} + \frac{3ia^2b(c + dx)^2}{2d} + \frac{3ia^2bd\text{Li}_2(-e^{2i(e+fx)})}{2f^2} + \frac{a^3(c + dx)^2}{2d} + \frac{3ab^2(c + dx) \tan(e + fx)}{f}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)*(a + b*Tan[e + f*x])^3,x]

[Out] $-3*a*b^2*c*x + (b^3*d*x)/(2*f) - (3*a*b^2*d*x^2)/2 + (a^3*(c + d*x)^2)/(2*d) + (((3*I)/2)*a^2*b*(c + d*x)^2/d - ((I/2)*b^3*(c + d*x)^2/d - (3*a^2*b*(c + d*x)*\text{Log}[1 + E^{((2*I)*(e + f*x))}])/f + (b^3*(c + d*x)*\text{Log}[1 + E^{((2*I)*(e + f*x))}])/f + (3*a*b^2*d*\text{Log}[\text{Cos}[e + f*x]])/f^2 + (((3*I)/2)*a^2*b*d*\text{PolyLog}[2, -E^{((2*I)*(e + f*x))}])/f^2 - ((I/2)*b^3*d*\text{PolyLog}[2, -E^{((2*I)*(e + f*x))}])/f^2 - (b^3*d*\text{Tan}[e + f*x])/(2*f^2) + (3*a*b^2*(c + d*x)*\text{Tan}[e + f*x])/f + (b^3*(c + d*x)*\text{Tan}[e + f*x]^2)/(2*f)$

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 2190

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^((n_)*((c_) + (d_)*(x_)))^((m_)))/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^((n_))), x_Symbol] := Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n]/a)]/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n]/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_)))^((n_))], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

Int[Log[(c_)*((d_) + (e_)*(x_)^((n_)))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 3473

Int[((b_)*tan[(c_) + (d_)*(x_)])^((n_)), x_Symbol] := Simp[(b*(b*Tan[c + d*x])^(n - 1))/(d*(n - 1)), x] - Dist[b^2, Int[(b*Tan[c + d*x])^(n - 2), x],

x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1]

Rule 3475

Int[tan[(c_.) + (d_.)*(x_.)], x_Symbol] := -Simp[Log[RemoveContent[Cos[c + d*x], x]]/d, x] /; FreeQ[{c, d}, x]

Rule 3719

Int[((c_.) + (d_.)*(x_.))^(m_.)*tan[(e_.) + (f_.)*(x_.)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m*E^(2*I*(e + f*x)))/(1 + E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 3720

Int[((c_.) + (d_.)*(x_.))^(m_.)*((b_.)*tan[(e_.) + (f_.)*(x_.)])^(n_.), x_Symbol] := Simp[(b*(c + d*x)^m*(b*Tan[e + f*x])^(n - 1))/(f*(n - 1)), x] + (-Dist[(b*d*m)/(f*(n - 1)), Int[(c + d*x)^(m - 1)*(b*Tan[e + f*x])^(n - 1), x], x] - Dist[b^2, Int[(c + d*x)^m*(b*Tan[e + f*x])^(n - 2), x], x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 0]

Rule 3722

Int[((c_.) + (d_.)*(x_.))^(m_.)*((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_.)])^(n_.), x_Symbol] := Int[ExpandIntegrand[(c + d*x)^m, (a + b*Tan[e + f*x])^n, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[m, 0] && IGtQ[n, 0]

Rubi steps

$$\begin{aligned}
 \int (c + dx)(a + b \tan(e + fx))^3 dx &= \int (a^3(c + dx) + 3a^2b(c + dx) \tan(e + fx) + 3ab^2(c + dx) \tan^2(e + fx) + b^3(c + dx) \tan^3(e + fx)) dx \\
 &= \frac{a^3(c + dx)^2}{2d} + (3a^2b) \int (c + dx) \tan(e + fx) dx + (3ab^2) \int (c + dx) \tan^2(e + fx) dx + b^3 \int (c + dx) \tan^3(e + fx) dx \\
 &= \frac{a^3(c + dx)^2}{2d} + \frac{3a^2b(c + dx)^2}{2d} + \frac{3ab^2(c + dx) \tan(e + fx)}{f} + \frac{b^3(c + dx) \tan^2(e + fx)}{2f} \\
 &= -3ab^2cx - \frac{3}{2}ab^2dx^2 + \frac{a^3(c + dx)^2}{2d} + \frac{3a^2b(c + dx)^2}{2d} - \frac{ib^3(c + dx)^2}{2d} - \frac{3a^2b(c + dx)^2}{2d} \\
 &= -3ab^2cx + \frac{b^3dx}{2f} - \frac{3}{2}ab^2dx^2 + \frac{a^3(c + dx)^2}{2d} + \frac{3a^2b(c + dx)^2}{2d} - \frac{ib^3(c + dx)^2}{2d} \\
 &= -3ab^2cx + \frac{b^3dx}{2f} - \frac{3}{2}ab^2dx^2 + \frac{a^3(c + dx)^2}{2d} + \frac{3a^2b(c + dx)^2}{2d} - \frac{ib^3(c + dx)^2}{2d} \\
 &= -3ab^2cx + \frac{b^3dx}{2f} - \frac{3}{2}ab^2dx^2 + \frac{a^3(c + dx)^2}{2d} + \frac{3a^2b(c + dx)^2}{2d} - \frac{ib^3(c + dx)^2}{2d}
 \end{aligned}$$

Mathematica [A] time = 3.69, size = 277, normalized size = 1.00

$$\cos(e + fx)(a + b \tan(e + fx))^3 \left(-ibd(b^2 - 3a^2) \operatorname{Li}_2(-e^{2i(e+fx)}) \cos^2(e + fx) + \cos^2(e + fx) (2b \log(\cos(e + fx))) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)*(a + b*Tan[e + f*x])^3,x]

[Out] (Cos[e + f*x]*(Cos[e + f*x]^2*(-((e + f*x)*((-3*I)*a^2*b*d*(e + f*x) + I*b^3*d*(e + f*x) + 3*a*b^2*(-(d*e) + 2*c*f + d*f*x) + a^3*(-2*c*f + d*(e - f*x)))) + 2*b*(-3*a^2 + b^2)*d*(e + f*x)*Log[1 + E^((2*I)*(e + f*x))] + 2*b*(3*a*b*d + 3*a^2*(d*e - c*f) + b^2*(-(d*e) + c*f))*Log[Cos[e + f*x]]) - I*b*(-3*a^2 + b^2)*d*Cos[e + f*x]^2*PolyLog[2, -E^((2*I)*(e + f*x))] + (b^2*(2*b*f*(c + d*x) + (-b*d) + 6*a*f*(c + d*x))*Sin[2*(e + f*x)])/2)*(a + b*Tan[e + f*x])^3)/(2*f^2*(a*Cos[e + f*x] + b*SIN[e + f*x])^3)

fricas [A] time = 0.63, size = 327, normalized size = 1.18

$$2(a^3 - 3ab^2)df^2x^2 - i(3a^2b - b^3)d\text{Li}_2\left(\frac{2(i \tan(fx+e)-1)}{\tan(fx+e)^2+1} + 1\right) + i(3a^2b - b^3)d\text{Li}_2\left(\frac{2(-i \tan(fx+e)-1)}{\tan(fx+e)^2+1} + 1\right) + 2(b^3$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e))^3,x, algorithm="fricas")

[Out] 1/4*(2*(a^3 - 3*a*b^2)*d*f^2*x^2 - I*(3*a^2*b - b^3)*d*dilog(2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) + I*(3*a^2*b - b^3)*d*dilog(2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1) + 1) + 2*(b^3*d*f*x + b^3*c*f)*tan(f*x + e)^2 + 2*(b^3*d*f + 2*(a^3 - 3*a*b^2)*c*f^2)*x + 2*(3*a*b^2*d - (3*a^2*b - b^3)*d*f*x - (3*a^2*b - b^3)*c*f)*log(-2*(I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) + 2*(3*a*b^2*d - (3*a^2*b - b^3)*d*f*x - (3*a^2*b - b^3)*c*f)*log(-2*(-I*tan(f*x + e) - 1)/(tan(f*x + e)^2 + 1)) + 2*(6*a*b^2*d*f*x + 6*a*b^2*c*f - b^3*d)*tan(f*x + e))/f^2

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (dx + c)(b \tan(fx + e) + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e))^3,x, algorithm="giac")

[Out] integrate((d*x + c)*(b*tan(f*x + e) + a)^3, x)

maple [A] time = 0.77, size = 493, normalized size = 1.78

$$\frac{3ia^2bd \text{polylog}\left(2, -e^{2i(fx+e)}\right)}{2f^2} + \frac{6ib a^2 d e x}{f} + \frac{b^3 \ln\left(e^{2i(fx+e)} + 1\right) dx}{f} - \frac{3b a^2 c \ln\left(e^{2i(fx+e)} + 1\right)}{f} + \frac{6b a^2 c \ln\left(e^{i(fx+e)}\right)}{f}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)*(a+b*tan(f*x+e))^3,x)

[Out] 1/f*b^3*ln(exp(2*I*(f*x+e))+1)*d*x-3/f*b*a^2*c*ln(exp(2*I*(f*x+e))+1)+6/f*b*a^2*c*ln(exp(I*(f*x+e)))+3/f^2*b^2*a*d*ln(exp(2*I*(f*x+e))+1)-6/f^2*b^2*a*d*ln(exp(I*(f*x+e)))+2/f^2*b^3*d*e*ln(exp(I*(f*x+e)))-I/f^2*b^3*d*e^2+b^2*(6*I*a*d*f*x*exp(2*I*(f*x+e))+6*I*a*c*f*exp(2*I*(f*x+e))+2*b*d*f*x*exp(2*I*(f*x+e))+6*I*a*d*f*x-I*b*d*exp(2*I*(f*x+e))+2*b*c*f*exp(2*I*(f*x+e))+6*I*a*c*f-I*d*b)/f^2/(exp(2*I*(f*x+e))+1)^2+I*b^3*c*x+3/2*I*a^2*b*d*polylog(2,-exp(2*I*(f*x+e)))/f^2+6*I/f*b*a^2*d*e*x+3/2*I*a^2*b*d*x^2-1/2*I*b^3*d*x^2+1/f*b^3*c*ln(exp(2*I*(f*x+e))+1)-2/f*b^3*c*ln(exp(I*(f*x+e)))-1/2*I*b^3*d*polylog(2,-exp(2*I*(f*x+e)))/f^2-6/f^2*b*a^2*d*e*ln(exp(I*(f*x+e)))-3/f*b*ln(exp(2*I*(f*x+e))+1)*a^2*d*x-2*I/f*b^3*d*e*x+3*I/f^2*b*a^2*d*e^2-3*I*a^2*b*c*x+1/2*a^3*d*x^2+a^3*c*x-3*a*b^2*c*x-3/2*a*b^2*d*x^2

maxima [B] time = 1.68, size = 1327, normalized size = 4.79

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e))^3,x, algorithm="maxima")

[Out] $\frac{1}{2} * (2 * (f * x + e) * a^3 * c + (f * x + e)^2 * a^3 * d / f - 2 * (f * x + e) * a^3 * d * e / f + 6 * a^2 * b * c * \log(\sec(f * x + e)) - 6 * a^2 * b * d * e * \log(\sec(f * x + e)) / f - 2 * (12 * a * b^2 * d * e - 12 * a * b^2 * c * f - (3 * a^2 * b + 3 * I * a * b^2 - b^3) * (f * x + e)^2 * d + 2 * b^3 * d - ((-6 * I * a * b^2 + 2 * b^3) * d * e + (6 * I * a * b^2 - 2 * b^3) * c * f) * (f * x + e) + (2 * b^3 * d * e - 2 * b^3 * c * f - 6 * a * b^2 * d + 2 * (3 * a^2 * b - b^3) * (f * x + e) * d + 2 * (b^3 * d * e - b^3 * c * f - 3 * a * b^2 * d + (3 * a^2 * b - b^3) * (f * x + e) * d) * \cos(4 * f * x + 4 * e) + 4 * (b^3 * d * e - b^3 * c * f - 3 * a * b^2 * d + (3 * a^2 * b - b^3) * (f * x + e) * d) * \cos(2 * f * x + 2 * e) - (-2 * I * b^3 * d * e + 2 * I * b^3 * c * f + 6 * I * a * b^2 * d + (-6 * I * a^2 * b + 2 * I * b^3) * (f * x + e) * d) * \sin(4 * f * x + 4 * e) - (-4 * I * b^3 * d * e + 4 * I * b^3 * c * f + 12 * I * a * b^2 * d + (-12 * I * a^2 * b + 4 * I * b^3) * (f * x + e) * d) * \sin(2 * f * x + 2 * e)) * \arctan2(\sin(2 * f * x + 2 * e), \cos(2 * f * x + 2 * e) + 1) - ((3 * a^2 * b + 3 * I * a * b^2 - b^3) * (f * x + e)^2 * d - (12 * a * b^2 * d - (-6 * I * a * b^2 + 2 * b^3) * d * e - (6 * I * a * b^2 - 2 * b^3) * c * f) * (f * x + e)) * \cos(4 * f * x + 4 * e) - ((6 * a^2 * b + 6 * I * a * b^2 - 2 * b^3) * (f * x + e)^2 * d - 2 * b^3 * d - 4 * (3 * a * b^2 - I * b^3) * d * e + 4 * (3 * a * b^2 - I * b^3) * c * f + ((-12 * I * a * b^2 + 4 * b^3) * d * e + (12 * I * a * b^2 - 4 * b^3) * c * f - 4 * (3 * a * b^2 + I * b^3) * d) * (f * x + e)) * \cos(2 * f * x + 2 * e) - ((3 * a^2 * b - b^3) * d * \cos(4 * f * x + 4 * e) + 2 * (3 * a^2 * b - b^3) * d * \cos(2 * f * x + 2 * e) + (3 * I * a^2 * b - I * b^3) * d * \sin(4 * f * x + 4 * e) + (6 * I * a^2 * b - 2 * I * b^3) * d * \sin(2 * f * x + 2 * e) + (3 * a^2 * b - b^3) * d) * \operatorname{dilog}(-e^{(2 * I * f * x + 2 * I * e)}) - (I * b^3 * d * e - I * b^3 * c * f - 3 * I * a * b^2 * d + (3 * I * a^2 * b - I * b^3) * (f * x + e) * d + (I * b^3 * d * e - I * b^3 * c * f - 3 * I * a * b^2 * d + (3 * I * a^2 * b - I * b^3) * (f * x + e) * d) * \cos(4 * f * x + 4 * e) + (2 * I * b^3 * d * e - 2 * I * b^3 * c * f - 6 * I * a * b^2 * d + (6 * I * a^2 * b - 2 * I * b^3) * (f * x + e) * d) * \cos(2 * f * x + 2 * e) - (b^3 * d * e - b^3 * c * f - 3 * a * b^2 * d + (3 * a^2 * b - b^3) * (f * x + e) * d) * \sin(4 * f * x + 4 * e) - 2 * (b^3 * d * e - b^3 * c * f - 3 * a * b^2 * d + (3 * a^2 * b - b^3) * (f * x + e) * d) * \sin(2 * f * x + 2 * e)) * \log(\cos(2 * f * x + 2 * e)^2 + \sin(2 * f * x + 2 * e)^2 + 2 * \cos(2 * f * x + 2 * e) + 1) - ((3 * I * a^2 * b - 3 * a * b^2 - I * b^3) * (f * x + e)^2 * d + (-12 * I * a * b^2 * d + 2 * (3 * a * b^2 + I * b^3) * d * e - 2 * (3 * a * b^2 + I * b^3) * c * f) * (f * x + e)) * \sin(4 * f * x + 4 * e) - ((6 * I * a^2 * b - 6 * a * b^2 - 2 * I * b^3) * (f * x + e)^2 * d - 2 * I * b^3 * d + (-12 * I * a * b^2 - 4 * b^3) * d * e + (12 * I * a * b^2 + 4 * b^3) * c * f + (4 * (3 * a * b^2 + I * b^3) * d * e - 4 * (3 * a * b^2 + I * b^3) * c * f + (-12 * I * a * b^2 + 4 * b^3) * d) * (f * x + e)) * \sin(2 * f * x + 2 * e) / (-2 * I * f * \cos(4 * f * x + 4 * e) - 4 * I * f * \cos(2 * f * x + 2 * e) + 2 * f * \sin(4 * f * x + 4 * e) + 4 * f * \sin(2 * f * x + 2 * e) - 2 * I * f) / f$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int (a + b \tan(e + f x))^3 (c + d x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^3*(c + d*x),x)

[Out] int((a + b*tan(e + f*x))^3*(c + d*x), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int (a + b \tan(e + f x))^3 (c + d x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)*(a+b*tan(f*x+e))**3,x)

[Out] Integral((a + b*tan(e + f*x))**3*(c + d*x), x)

$$3.52 \quad \int \frac{(a+b \tan(e+fx))^3}{c+dx} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{(a+b \tan(e+fx))^3}{c+dx}, x\right)$$

[Out] Unintegrable((a+b*tan(f*x+e))^3/(d*x+c), x)

Rubi [A] time = 0.05, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a+b \tan(e+fx))^3}{c+dx} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*Tan[e + f*x])^3/(c + d*x), x]

[Out] Defer[Int][(a + b*Tan[e + f*x])^3/(c + d*x), x]

Rubi steps

$$\int \frac{(a+b \tan(e+fx))^3}{c+dx} dx = \int \frac{(a+b \tan(e+fx))^3}{c+dx} dx$$

Mathematica [A] time = 14.57, size = 0, normalized size = 0.00

$$\int \frac{(a+b \tan(e+fx))^3}{c+dx} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*Tan[e + f*x])^3/(c + d*x), x]

[Out] Integrate[(a + b*Tan[e + f*x])^3/(c + d*x), x]

fricas [A] time = 0.95, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{b^3 \tan^3(fx + e) + 3ab^2 \tan^2(fx + e) + 3a^2b \tan(fx + e) + a^3}{dx + c}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^3/(d*x+c), x, algorithm="fricas")

[Out] integral((b^3*tan(f*x + e)^3 + 3*a*b^2*tan(f*x + e)^2 + 3*a^2*b*tan(f*x + e) + a^3)/(d*x + c), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(b \tan(fx + e) + a)^3}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^3/(d*x+c), x, algorithm="giac")

[Out] integrate((b*tan(f*x + e) + a)^3/(d*x + c), x)

maple [A] time = 4.50, size = 0, normalized size = 0.00

$$\int \frac{(a + b \tan(fx + e))^3}{dx + c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*tan(f*x+e))^3/(d*x+c),x)

[Out] int((a+b*tan(f*x+e))^3/(d*x+c),x)

maxima [A] time = 0.00, size = 0, normalized size = 0.00

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^3/(d*x+c),x, algorithm="maxima")

[Out] (((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*cos(4*f*x + 4*e)^2*log(d*x + c) + ((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c)*sin(4*f*x + 4*e)^2 + 4*(b^3*d^2*f*x + b^3*c*d*f + ((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c)*cos(2*f*x + 2*e)^2 + 4*(b^3*d^2*f*x + b^3*c*d*f + ((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c)*sin(2*f*x + 2*e)^2 + (2*(b^3*d^2*f*x + b^3*c*d*f + 2*((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c))*cos(2*f*x + 2*e) + 2*((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c) - (6*a*b^2*d^2*f*x + 6*a*b^2*c*d*f + b^3*d^2)*sin(2*f*x + 2*e))*cos(4*f*x + 4*e) + 2*(b^3*d^2*f*x + b^3*c*d*f + 2*((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c))*cos(2*f*x + 2*e) - (d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(4*f*x + 4*e)^2 + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(2*f*x + 2*e)^2 + (d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*sin(4*f*x + 4*e)^2 + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*sin(4*f*x + 4*e)*sin(2*f*x + 2*e) + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*sin(2*f*x + 2*e)^2 + 2*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2) + 2*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(2*f*x + 2*e))*cos(4*f*x + 4*e) + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(2*f*x + 2*e))*integrate(-2*((3*a^2*b - b^3)*d^2*f^2*x^2 + 3*a*b^2*c*d*f + b^3*d^2 + (3*a^2*b - b^3)*c^2*f^2 + (3*a*b^2*d^2*f + 2*(3*a^2*b - b^3)*c*d*f^2)*x)*sin(2*f*x + 2*e)/(d^3*f^2*x^3 + 3*c*d^2*f^2*x^2 + 3*c^2*d*f^2*x + c^3*f^2 + (d^3*f^2*x^3 + 3*c*d^2*f^2*x^2 + 3*c^2*d*f^2*x + c^3*f^2)*cos(2*f*x + 2*e)^2 + (d^3*f^2*x^3 + 3*c*d^2*f^2*x^2 + 3*c^2*d*f^2*x + c^3*f^2)*sin(2*f*x + 2*e)^2 + 2*(d^3*f^2*x^3 + 3*c*d^2*f^2*x^2 + 3*c^2*d*f^2*x + c^3*f^2)*cos(2*f*x + 2*e)), x) + ((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c) + (6*a*b^2*d^2*f*x + 6*a*b^2*c*d*f + b^3*d^2 + (6*a*b^2*d^2*f*x + 6*a*b^2*c*d*f + b^3*d^2)*cos(2*f*x + 2*e) + 2*(b^3*d^2*f*x + b^3*c*d*f + 2*((a^3 - 3*a*b^2)*d^2*f^2*x^2 + 2*(a^3 - 3*a*b^2)*c*d*f^2*x + (a^3 - 3*a*b^2)*c^2*f^2)*log(d*x + c))*sin(2*f*x + 2*e))*sin(4*f*x + 4*e) + (6*a*b^2*d^2*f*x + 6*a*b^2*c*d*f + b^3*d^2)*sin(2*f*x + 2*e))/(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2 + (d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(4*f*x + 4*e)^2 + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(2*f*x + 2*e)^2 + (d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*sin(4*f*x + 4*e)^2 + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*sin(4*f*x + 4*e)*sin(2*f*x + 2*e) + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*sin(2*f*x + 2*e)^2 + 2*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2 + 2*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(2*f*x + 2*e))*cos(4*f*x + 4*e) + 4*(d^3*f^2*x^2 + 2*c*d^2*f^2*x + c^2*d*f^2)*cos(2*f*x + 2*e))

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{(a + b \tan(e + fx))^3}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a + b*tan(e + f*x))^3/(c + d*x), x)

[Out] int((a + b*tan(e + f*x))^3/(c + d*x), x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + b \tan(e + fx))^3}{c + dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))**3/(d*x+c), x)

[Out] Integral((a + b*tan(e + f*x))**3/(c + d*x), x)

$$3.53 \quad \int \frac{(a+b \tan(e+fx))^3}{(c+dx)^2} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{(a+b \tan(e+fx))^3}{(c+dx)^2}, x\right)$$

[Out] Unintegrable((a+b*tan(f*x+e))^3/(d*x+c)^2,x)

Rubi [A] time = 0.05, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{(a+b \tan(e+fx))^3}{(c+dx)^2} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*Tan[e + f*x])^3/(c + d*x)^2,x]

[Out] Defer[Int][(a + b*Tan[e + f*x])^3/(c + d*x)^2, x]

Rubi steps

$$\int \frac{(a+b \tan(e+fx))^3}{(c+dx)^2} dx = \int \frac{(a+b \tan(e+fx))^3}{(c+dx)^2} dx$$

Mathematica [A] time = 20.11, size = 0, normalized size = 0.00

$$\int \frac{(a+b \tan(e+fx))^3}{(c+dx)^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*Tan[e + f*x])^3/(c + d*x)^2,x]

[Out] Integrate[(a + b*Tan[e + f*x])^3/(c + d*x)^2, x]

fricas [A] time = 0.52, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{b^3 \tan(fx+e)^3 + 3ab^2 \tan(fx+e)^2 + 3a^2b \tan(fx+e) + a^3}{d^2x^2 + 2cdx + c^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^3/(d*x+c)^2,x, algorithm="fricas")

[Out] integral((b^3*tan(f*x + e)^3 + 3*a*b^2*tan(f*x + e)^2 + 3*a^2*b*tan(f*x + e) + a^3)/(d^2*x^2 + 2*c*d*x + c^2), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(b \tan(fx+e) + a)^3}{(dx+c)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*tan(f*x+e))^3/(d*x+c)^2,x, algorithm="giac")


```

3*d*f^2)*sin(4*f*x + 4*e)*sin(2*f*x + 2*e) + 4*(d^4*f^2*x^3 + 3*c*d^3*f^2*x
^2 + 3*c^2*d^2*f^2*x + c^3*d*f^2)*sin(2*f*x + 2*e)^2 + 2*(d^4*f^2*x^3 + 3*c
*d^3*f^2*x^2 + 3*c^2*d^2*f^2*x + c^3*d*f^2 + 2*(d^4*f^2*x^3 + 3*c*d^3*f^2*x
^2 + 3*c^2*d^2*f^2*x + c^3*d*f^2))*cos(2*f*x + 2*e))*cos(4*f*x + 4*e) + 4*(d
^4*f^2*x^3 + 3*c*d^3*f^2*x^2 + 3*c^2*d^2*f^2*x + c^3*d*f^2)*cos(2*f*x + 2*e
))

```

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{(a + b \tan(e + f x))^3}{(c + d x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a + b*tan(e + f*x))^3/(c + d*x)^2,x)
```

```
[Out] int((a + b*tan(e + f*x))^3/(c + d*x)^2, x)
```

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(a + b \tan(e + f x))^3}{(c + d x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*tan(f*x+e))**3/(d*x+c)**2,x)
```

```
[Out] Integral((a + b*tan(e + f*x))**3/(c + d*x)**2, x)
```


$$3.54 \quad \int \frac{(c+dx)^3}{a+b \tan(e+fx)} dx$$

Optimal. Leaf size=243

$$\frac{3bd^2(c+dx)\operatorname{Li}_3\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^3(a^2+b^2)} - \frac{3ibd(c+dx)^2\operatorname{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^2(a^2+b^2)} + \frac{b(c+dx)^3 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f(a^2+b^2)} + \dots$$

[Out] $1/4*(d*x+c)^4/(a+I*b)/d+b*(d*x+c)^3*\ln(1+(a^2+b^2)*\exp(2*I*(f*x+e)))/(a+I*b)^2/(a^2+b^2)/f-3/2*I*b*d*(d*x+c)^2*\operatorname{polylog}(2,-(a^2+b^2)*\exp(2*I*(f*x+e)))/(a+I*b)^2/(a^2+b^2)/f^2+3/2*b*d^2*(d*x+c)*\operatorname{polylog}(3,-(a^2+b^2)*\exp(2*I*(f*x+e)))/(a+I*b)^2/(a^2+b^2)/f^3+3/4*I*b*d^3*\operatorname{polylog}(4,-(a^2+b^2)*\exp(2*I*(f*x+e)))/(a+I*b)^2/(a^2+b^2)/f^4$

Rubi [A] time = 0.33, antiderivative size = 243, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.300$, Rules used = {3732, 2190, 2531, 6609, 2282, 6589}

$$\frac{3bd^2(c+dx)\operatorname{Li}_3\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^3(a^2+b^2)} - \frac{3ibd(c+dx)^2\operatorname{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^2(a^2+b^2)} + \frac{b(c+dx)^3 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f(a^2+b^2)} + \dots$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(c + d*x)^3/(a + b*\operatorname{Tan}[e + f*x]), x]$

[Out] $(c + d*x)^4/(4*(a + I*b)*d) + (b*(c + d*x)^3*\operatorname{Log}[1 + ((a^2 + b^2)*E^{((2*I)*(e + f*x))})/(a + I*b)^2])/(a + I*b)^2)/((a^2 + b^2)*f) - (((3*I)/2)*b*d*(c + d*x)^2*\operatorname{PolyLog}[2, -(((a^2 + b^2)*E^{((2*I)*(e + f*x))})/(a + I*b)^2)])/(a^2 + b^2)*f^2 + (3*b*d^2*(c + d*x)*\operatorname{PolyLog}[3, -(((a^2 + b^2)*E^{((2*I)*(e + f*x))})/(a + I*b)^2)])/(2*(a^2 + b^2)*f^3) + (((3*I)/4)*b*d^3*\operatorname{PolyLog}[4, -(((a^2 + b^2)*E^{((2*I)*(e + f*x))})/(a + I*b)^2)])/(a^2 + b^2)*f^4$

Rule 2190

$\operatorname{Int}[(F_)^{((g_.)*((e_.) + (f_.)*(x_)))}^{(n_.)}*((c_.) + (d_.)*(x_))^{(m_.)}]/((a_.) + (b_.)*(F_)^{((g_.)*((e_.) + (f_.)*(x_)))}^{(n_.)}), x_Symbol] \rightarrow \operatorname{Simp}[(c + d*x)^m*\operatorname{Log}[1 + (b*(F^{(g*(e + f*x)))})^n/a]/(b*f*g*n*\operatorname{Log}[F]), x] - \operatorname{Dist}[(d*m)/(b*f*g*n*\operatorname{Log}[F]), \operatorname{Int}[(c + d*x)^{(m-1)}*\operatorname{Log}[1 + (b*(F^{(g*(e + f*x)))})^n/a], x], x] /; \operatorname{FreeQ}\{F, a, b, c, d, e, f, g, n\}, x] \&\& \operatorname{IGtQ}[m, 0]$

Rule 2282

$\operatorname{Int}[u, x_Symbol] \rightarrow \operatorname{With}\{v = \operatorname{FunctionOfExponential}[u, x]\}, \operatorname{Dist}[v/D[v, x], \operatorname{Subst}[\operatorname{Int}[\operatorname{FunctionOfExponentialFunction}[u, x]/x, x], x, v], x] /; \operatorname{FunctionOfExponentialQ}[u, x] \&\& !\operatorname{MatchQ}[u, (w_)*((a_.)*(v_))^{(n_)}]^{(m_)} /; \operatorname{FreeQ}\{a, m, n\}, x] \&\& \operatorname{IntegerQ}[m*n] \&\& !\operatorname{MatchQ}[u, E^{((c_.)*((a_.) + (b_.)*x))}*(F_)[v_]] /; \operatorname{FreeQ}\{a, b, c\}, x] \&\& \operatorname{InverseFunctionQ}[F[x]]$

Rule 2531

$\operatorname{Int}[\operatorname{Log}[1 + (e_.)*(F_)^{((c_.)*((a_.) + (b_.)*(x_)))}^{(n_.)}]]*((f_.) + (g_.)*(x_))^{(m_.)}, x_Symbol] \rightarrow -\operatorname{Simp}[(f + g*x)^m*\operatorname{PolyLog}[2, -(e*(F^{(c*(a + b*x)))})^n]/(b*c*n*\operatorname{Log}[F]), x] + \operatorname{Dist}[(g*m)/(b*c*n*\operatorname{Log}[F]), \operatorname{Int}[(f + g*x)^{(m-1)}*\operatorname{PolyLog}[2, -(e*(F^{(c*(a + b*x)))})^n], x], x] /; \operatorname{FreeQ}\{F, a, b, c, e, f, g, n\}, x] \&\& \operatorname{GtQ}[m, 0]$

Rule 3732

```
Int[((c_.) + (d_.)*(x_))^(m_.)/((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[((c + d*x)^m*E^Simp[2*I*(e + f*x), x]]/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2
*I*(e + f*x), x]), x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 6609

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_))))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p]/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{(c + dx)^3}{a + b \tan(e + fx)} dx &= \frac{(c + dx)^4}{4(a + ib)d} + (2ib) \int \frac{e^{2i(e+fx)}(c + dx)^3}{(a + ib)^2 + (a^2 + b^2)e^{2i(e+fx)}} dx \\ &= \frac{(c + dx)^4}{4(a + ib)d} + \frac{b(c + dx)^3 \log\left(1 + \frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{(a^2 + b^2)f} - \frac{(3bd) \int (c + dx)^2 \log\left(1 + \frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{(a^2 + b^2)f} \\ &= \frac{(c + dx)^4}{4(a + ib)d} + \frac{b(c + dx)^3 \log\left(1 + \frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{(a^2 + b^2)f} - \frac{3ibd(c + dx)^2 \text{Li}_2\left(-\frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{2(a^2 + b^2)f^2} + \\ &= \frac{(c + dx)^4}{4(a + ib)d} + \frac{b(c + dx)^3 \log\left(1 + \frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{(a^2 + b^2)f} - \frac{3ibd(c + dx)^2 \text{Li}_2\left(-\frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{2(a^2 + b^2)f^2} + \\ &= \frac{(c + dx)^4}{4(a + ib)d} + \frac{b(c + dx)^3 \log\left(1 + \frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{(a^2 + b^2)f} - \frac{3ibd(c + dx)^2 \text{Li}_2\left(-\frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{2(a^2 + b^2)f^2} + \\ &= \frac{(c + dx)^4}{4(a + ib)d} + \frac{b(c + dx)^3 \log\left(1 + \frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{(a^2 + b^2)f} - \frac{3ibd(c + dx)^2 \text{Li}_2\left(-\frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{2(a^2 + b^2)f^2} + \\ &= \frac{(c + dx)^4}{4(a + ib)d} + \frac{b(c + dx)^3 \log\left(1 + \frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{(a^2 + b^2)f} - \frac{3ibd(c + dx)^2 \text{Li}_2\left(-\frac{(a^2 + b^2)e^{2i(e+fx)}}{(a + ib)^2}\right)}{2(a^2 + b^2)f^2} + \end{aligned}$$

Mathematica [A] time = 2.31, size = 297, normalized size = 1.22

$$\frac{x \cos(e) (4c^3 + 6c^2 dx + 4cd^2 x^2 + d^3 x^3)}{4(a \cos(e) + b \sin(e))} + \frac{1}{4} b \left(\frac{3d \left(2if^2(c + dx)^2 \text{Li}_2\left(\frac{(-a-ib)e^{-2i(e+fx)}}{a-ib}\right) + d \left(2f(c + dx) \text{Li}_3\left(\frac{(-a-ib)e^{-2i(e+fx)}}{a-ib}\right) \right)}{f^4 (a^2 + b^2)} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^3/(a + b*Tan[e + f*x]),x]
```

```
[Out] (b*((-2*(c + d*x)^4)/((I*a + b)*d*((-I)*b*(-1 + E^((2*I)*e)) + a*(1 + E^((2*I)*e)))) + (4*(c + d*x)^3*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(e + f*x))])]/((a^2 + b^2)*f) + (3*d*((2*I)*f^2*(c + d*x)^2*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x))]) + d*(2*f*(c + d*x)*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x))]) - I*d*PolyLog[4, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x))])])]/((a^2 + b^2)*f^4))/4 + (x*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d^3*x^3)*Cos[e])/(4*(a*Cos[e] + b*Sin[e]))
```

fricas [C] time = 0.54, size = 1183, normalized size = 4.87

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3/(a+b*tan(f*x+e)),x, algorithm="fricas")
```

```
[Out] 1/8*(2*a*d^3*f^4*x^4 + 8*a*c*d^2*f^4*x^3 + 12*a*c^2*d*f^4*x^2 + 8*a*c^3*f^4*x - 3*I*b*d^3*polylog(4, ((a^2 + 2*I*a*b - b^2)*tan(f*x + e)^2 - a^2 - 2*I*a*b + b^2 + (2*I*a^2 - 4*a*b - 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + 3*I*b*d^3*polylog(4, ((a^2 - 2*I*a*b - b^2)*tan(f*x + e)^2 - a^2 + 2*I*a*b + b^2 + (-2*I*a^2 - 4*a*b + 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + (6*I*b*d^3*f^2*x^2 + 12*I*b*c*d^2*f^2*x + 6*I*b*c^2*d*f^2)*dilog((2*(I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2) + 1) + (-6*I*b*d^3*f^2*x^2 - 12*I*b*c*d^2*f^2*x - 6*I*b*c^2*d*f^2)*dilog((2*(-I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2) + 1) + 4*(b*d^3*f^3*x^3 + 3*b*c*d^2*f^3*x^2 + 3*b*c^2*d*f^3*x + b*d^3*e^3 - 3*b*c*d^2*e^2*f + 3*b*c^2*d*e*f^2)*log(-(2*(I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + 4*(b*d^3*f^3*x^3 + 3*b*c*d^2*f^3*x^2 + 3*b*c^2*d*f^3*x + b*d^3*e^3 - 3*b*c*d^2*e^2*f + 3*b*c^2*d*e*f^2)*log(-(2*(-I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) - 4*(b*d^3*e^3 - 3*b*c*d^2*e^2*f + 3*b*c^2*d*e*f^2 - b*c^3*f^3)*log(((I*a*b + b^2)*tan(f*x + e)^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*tan(f*x + e))/(tan(f*x + e)^2 + 1)) - 4*(b*d^3*e^3 - 3*b*c*d^2*e^2*f + 3*b*c^2*d*e*f^2 - b*c^3*f^3)*log(((I*a*b - b^2)*tan(f*x + e)^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*tan(f*x + e))/(tan(f*x + e)^2 + 1)) + 6*(b*d^3*f*x + b*c*d^2*f)*polylog(3, ((a^2 + 2*I*a*b - b^2)*tan(f*x + e)^2 - a^2 - 2*I*a*b + b^2 + (2*I*a^2 - 4*a*b - 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + 6*(b*d^3*f*x + b*c*d^2*f)*polylog(3, ((a^2 - 2*I*a*b - b^2)*tan(f*x + e)^2 - a^2 + 2*I*a*b + b^2 + (-2*I*a^2 - 4*a*b + 2*I*b^2)*tan(f*x + e)))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)))/((a^2 + b^2)*f^4)
```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^3}{b \tan(fx + e) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3/(a+b*tan(f*x+e)),x, algorithm="giac")
```

```
[Out] integrate((d*x + c)^3/(b*tan(f*x + e) + a), x)
```

maple [B] time = 1.18, size = 1450, normalized size = 5.97

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(a+b*tan(f*x+e)),x)

[Out]
$$-1/4/(I*b-a)*d^3*x^4-1/(I*b-a)*c^3*x-1/2/(I*a+b)*b*d^3/(-I*b-a)*x^4+4/f^3/(I*a+b)*b*c*d^2*e^3/(-I*b-a)-3/f^2/(I*a+b)*b*c^2*d/(-I*b-a)*e^2-2/f^3/(I*a+b)*b*d^3/(-I*b-a)*e^3*x-2*I/f/(I*a+b)*b*c^3/(a+I*b)*\ln(\exp(I*(f*x+e)))-I/f^4/(I*a+b)*b*d^3*e^3/(a+I*b)*\ln(I*\exp(2*I*(f*x+e)))*b-a*\exp(2*I*(f*x+e))-I*b-a)+6/f^2/(I*a+b)*b*c*d^2*e^2/(-I*b-a)*x-3/f^2/(I*a+b)*b*c*d^2/(-I*b-a)*\text{polylog}(2,(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*x-3/2*I/f^3/(I*a+b)*b*d^3/(-I*b-a)*\text{polylog}(3,(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*x+2*I/f^4/(I*a+b)*b*d^3*e^3/(a+I*b)*\ln(\exp(I*(f*x+e)))-3/2*I/f^3/(I*a+b)*b*c*d^2/(-I*b-a)*\text{polylog}(3,(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))-I/f/(I*a+b)*b*d^3/(-I*b-a)*\ln(1-(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*x^3-I/f^4/(I*a+b)*b*d^3/(-I*b-a)*\ln(1-(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*e^3-6/f/(I*a+b)*b*c^2*d/(-I*b-a)*e*x-1/(I*b-a)*c*d^2*x^3-3/2/(I*b-a)*c^2*d*x^2-3*I/f/(I*a+b)*b*c^2*d/(-I*b-a)*\ln(1-(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*x-3*I/f^2/(I*a+b)*b*c^2*d/(-I*b-a)*\ln(1-(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*e+6*I/f^2/(I*a+b)*b*c^2*d*e/(a+I*b)*\ln(\exp(I*(f*x+e)))+3*I/f^3/(I*a+b)*b*c*d^2/(-I*b-a)*\ln(1-(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*e^2-3*I/f^2/(I*a+b)*b*c^2*d*e/(a+I*b)*\ln(I*\exp(2*I*(f*x+e)))*b-a*\exp(2*I*(f*x+e))-I*b-a)-3*I/f/(I*a+b)*b*c*d^2/(-I*b-a)*\ln(1-(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*x^2-6*I/f^3/(I*a+b)*b*c*d^2*e^2/(a+I*b)*\ln(\exp(I*(f*x+e)))+3*I/f^3/(I*a+b)*b*c*d^2*e^2/(a+I*b)*\ln(I*\exp(2*I*(f*x+e)))*b-a*\exp(2*I*(f*x+e))-I*b-a)-3/2/f^2/(I*a+b)*b*d^3/(-I*b-a)*\text{polylog}(2,(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))*x^2-3/2/f^2/(I*a+b)*b*c^2*d/(-I*b-a)*\text{polylog}(2,(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))+I/f/(I*a+b)*b*c^3/(a+I*b)*\ln(I*\exp(2*I*(f*x+e)))*b-a*\exp(2*I*(f*x+e))-I*b-a)-2/(I*a+b)*b*c*d^2/(-I*b-a))*x^3-3/(I*a+b)*b*c^2*d/(-I*b-a))*x^2-3/2/f^4/(I*a+b)*b*d^3/(-I*b-a)*e^4+3/4/f^4/(I*a+b)*b*d^3/(-I*b-a)*\text{polylog}(4,(a-I*b)*\exp(2*I*(f*x+e)))/(-I*b-a))$$

maxima [B] time = 1.61, size = 977, normalized size = 4.02

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+b*tan(f*x+e)),x, algorithm="maxima")

[Out]
$$-1/12*(18*c^2*d*e*(2*(f*x + e)*a/((a^2 + b^2)*f) + 2*b*\log(b*\tan(f*x + e) + a)/((a^2 + b^2)*f) - b*\log(\tan(f*x + e)^2 + 1)/((a^2 + b^2)*f)) - 6*(2*(f*x + e)*a/(a^2 + b^2) + 2*b*\log(b*\tan(f*x + e) + a)/(a^2 + b^2) - b*\log(\tan(f*x + e)^2 + 1)/(a^2 + b^2))*c^3 - (3*(f*x + e)^4*(a - I*b)*d^3 + 12*I*b*d^3*\text{polylog}(4, (I*a + b)*e^{(2*I*f*x + 2*I*e)}/(-I*a + b)) - 12*((a - I*b)*d^3*e - (a - I*b)*c*d^2*f)*(f*x + e)^3 + 18*((a - I*b)*d^3*e^2 - 2*(a - I*b)*c*d^2*e*f + (a - I*b)*c^2*d*f^2)*(f*x + e)^2 - 12*((a - I*b)*d^3*e^3 - 3*(a - I*b)*c*d^2*e^2*f)*(f*x + e) + (-12*I*b*d^3*e^3 + 36*I*b*c*d^2*e^2*f)*\arctan2(-b*\cos(2*f*x + 2*e) + a*\sin(2*f*x + 2*e) + b, a*\cos(2*f*x + 2*e) + b*\sin(2*f*x + 2*e) + a) + (-16*I*(f*x + e)^3*b*d^3 + (36*I*b*d^3*e - 36*I*b*c*d^2*f)*(f*x + e)^2 + (-36*I*b*d^3*e^2 + 72*I*b*c*d^2*e*f - 36*I*b*c^2*d*f^2)*(f*x + e))*\arctan2((2*a*b*\cos(2*f*x + 2*e) - (a^2 - b^2)*\sin(2*f*x + 2*e))/(a^2 + b^2), (2*a*b*\sin(2*f*x + 2*e) + a^2 + b^2 + (a^2 - b^2)*\cos(2*f*x + 2*e))/(a^2 + b^2)) + (-24*I*(f*x + e)^2*b*d^3 - 18*I*b*d^3*e^2 + 36*I*b*c*d^2*e*f - 18*I*b*c^2*d*f^2 + (36*I*b*d^3*e - 36*I*b*c*d^2*f)*(f*x + e))*\text{dilog}((I*a + b)*e^{(2*I*f*x + 2*I*e)}/(-I*a + b)) - 6*(b*d^3*e^3 - 3*b*c*d^2*e^2*f)*\log((a^2 + b^2)*\cos(2*f*x + 2*e)^2 + 4*a*b*\sin(2*f*x + 2*e) + (a^2 + b^2)*\sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*f*x + 2*e)) + 2*(4*(f*x + e)^3*b*d^3 - 9*(b*d^3*e - b*c*d^2*f)*(f*x + e)^2 + 9*(b*d^3*e^2 - 2*b*c*d^2*e*f + b*c^2*d*f^2)*(f*x + e))*\log(((a^2 + b^2)*\cos(2*f*x + 2*e)^2 + 4*a*b*\sin(2*f*x + 2*e) + (a^2 + b^2)*\sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*f*x + 2*e))/(a^2 + b^2)) + 6*(4*(f*x + e)*b*d^3 - 3*b*d^3*e + 3*b*c*d^2*f)*\text{polylog}(3, (I*a + b)*e^{(2*I*f*x + 2*I*e)}/(-I*a + b)))/((a^2 + b^2)*f^3))/f$$

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^3}{a + b \tan(e + fx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*tan(e + f*x)), x)

[Out] int((c + d*x)^3/(a + b*tan(e + f*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^3}{a + b \tan(e + fx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**3/(a+b*tan(f*x+e)), x)

[Out] Integral((c + d*x)**3/(a + b*tan(e + f*x)), x)

$$3.55 \quad \int \frac{(c+dx)^2}{a+b \tan(e+fx)} dx$$

Optimal. Leaf size=181

$$-\frac{ibd(c+dx)\text{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f^2(a^2+b^2)} + \frac{b(c+dx)^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f(a^2+b^2)} + \frac{bd^2\text{Li}_3\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^3(a^2+b^2)} + \frac{(c+dx)^3}{3d(a+ib)}$$

[Out] 1/3*(d*x+c)^3/(a+I*b)/d+b*(d*x+c)^2*ln(1+(a^2+b^2)*exp(2*I*(f*x+e))/(a+I*b)^2)/(a^2+b^2)/f-I*b*d*(d*x+c)*polylog(2,-(a^2+b^2)*exp(2*I*(f*x+e))/(a+I*b)^2)/(a^2+b^2)/f^2+1/2*b*d^2*polylog(3,-(a^2+b^2)*exp(2*I*(f*x+e))/(a+I*b)^2)/(a^2+b^2)/f^3

Rubi [A] time = 0.27, antiderivative size = 181, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {3732, 2190, 2531, 2282, 6589}

$$-\frac{ibd(c+dx)\text{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f^2(a^2+b^2)} + \frac{b(c+dx)^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f(a^2+b^2)} + \frac{bd^2\text{Li}_3\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^3(a^2+b^2)} + \frac{(c+dx)^3}{3d(a+ib)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^2/(a + b*Tan[e + f*x]),x]

[Out] (c + d*x)^3/(3*(a + I*b)*d) + (b*(c + d*x)^2*Log[1 + ((a^2 + b^2)*E^((2*I)*(e + f*x)))/(a + I*b)^2])/((a^2 + b^2)*f) - (I*b*d*(c + d*x)*PolyLog[2, -((a^2 + b^2)*E^((2*I)*(e + f*x)))/(a + I*b)^2])/((a^2 + b^2)*f^2) + (b*d^2*PolyLog[3, -(((a^2 + b^2)*E^((2*I)*(e + f*x)))/(a + I*b)^2)]/(2*(a^2 + b^2)*f^3)

Rule 2190

Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a]]/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m-1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 2531

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_)))^(n_))]*((f_) + (g_)*(x_))^(m_), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x))))^n]]/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m-1)*PolyLog[2, -(e*(F^(c*(a + b*x))))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3732

Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c + d*x)^(m+1)/(d*(m+1)*(a + I*b)), x] + Dist[2*I*b, Int

```
[((c + d*x)^m*E^Simp[2*I*(e + f*x), x]]/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*I*(e + f*x), x]), x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0] && IGtQ[m, 0]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_.))^(p_.)]/((d_.) + (e_.)*(x_.)), x_Symbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int \frac{(c + dx)^2}{a + b \tan(e + fx)} dx &= \frac{(c + dx)^3}{3(a + ib)d} + (2ib) \int \frac{e^{2i(e+fx)}(c + dx)^2}{(a + ib)^2 + (a^2 + b^2)e^{2i(e+fx)}} dx \\ &= \frac{(c + dx)^3}{3(a + ib)d} + \frac{b(c + dx)^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f} - \frac{(2bd) \int (c + dx) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f} \\ &= \frac{(c + dx)^3}{3(a + ib)d} + \frac{b(c + dx)^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f} - \frac{ibd(c + dx)\text{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f^2} + \\ &= \frac{(c + dx)^3}{3(a + ib)d} + \frac{b(c + dx)^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f} - \frac{ibd(c + dx)\text{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f^2} + \\ &= \frac{(c + dx)^3}{3(a + ib)d} + \frac{b(c + dx)^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f} - \frac{ibd(c + dx)\text{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2)f^2} + \end{aligned}$$

Mathematica [A] time = 1.86, size = 236, normalized size = 1.30

$$\frac{x \cos(e) (3c^2 + 3cdx + d^2x^2)}{3(a \cos(e) + b \sin(e))} + \frac{1}{6}b \left(\frac{3d \left(2if(c + dx)\text{Li}_2\left(\frac{(-a-ib)e^{-2i(e+fx)}}{a-ib}\right) + d\text{Li}_3\left(\frac{(-a-ib)e^{-2i(e+fx)}}{a-ib}\right) \right)}{f^3(a^2 + b^2)} + \frac{6(c + dx)^2 \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^2/(a + b*Tan[e + f*x]), x]
```

```
[Out] (b*((-4*(c + d*x)^3)/((I*a + b)*d*((-I)*b*(-1 + E^((2*I)*e)) + a*(1 + E^((2*I)*e)))) + (6*(c + d*x)^2*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(e + f*x))])]/((a^2 + b^2)*f) + (3*d*((2*I)*f*(c + d*x)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x))]) + d*PolyLog[3, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x)))]))/((a^2 + b^2)*f^3))/6 + (x*(3*c^2 + 3*c*d*x + d^2*x^2)*Cos[e])/ (3*(a*Cos[e] + b*Sin[e]))
```

fricas [C] time = 1.22, size = 836, normalized size = 4.62

$$4ad^2f^3x^3 + 12acd f^3x^2 + 12ac^2f^3x + 3bd^2 \text{polylog}\left(3, \frac{(a^2+2iab-b^2)\tan(fx+e)^2 - a^2 - 2iab + b^2 + (2ia^2 - 4ab - 2ib^2)\tan(fx+e)}{(a^2+b^2)\tan(fx+e)^2 + a^2 + b^2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+b*tan(f*x+e)),x, algorithm="fricas")

[Out] $\frac{1}{12} \cdot (4 \cdot a \cdot d^2 \cdot f^3 \cdot x^3 + 12 \cdot a \cdot c \cdot d \cdot f^3 \cdot x^2 + 12 \cdot a \cdot c^2 \cdot f^3 \cdot x + 3 \cdot b \cdot d^2 \cdot \text{polylog}(3, ((a^2 + 2 \cdot I \cdot a \cdot b - b^2) \cdot \tan(f \cdot x + e))^2 - a^2 - 2 \cdot I \cdot a \cdot b + b^2 + (2 \cdot I \cdot a^2 - 4 \cdot a \cdot b - 2 \cdot I \cdot b^2) \cdot \tan(f \cdot x + e)) / ((a^2 + b^2) \cdot \tan(f \cdot x + e))^2 + a^2 + b^2)) + 3 \cdot b \cdot d^2 \cdot \text{polylog}(3, ((a^2 - 2 \cdot I \cdot a \cdot b - b^2) \cdot \tan(f \cdot x + e))^2 - a^2 + 2 \cdot I \cdot a \cdot b + b^2 + (-2 \cdot I \cdot a^2 - 4 \cdot a \cdot b + 2 \cdot I \cdot b^2) \cdot \tan(f \cdot x + e)) / ((a^2 + b^2) \cdot \tan(f \cdot x + e))^2 + a^2 + b^2)) + (6 \cdot I \cdot b \cdot d^2 \cdot f \cdot x + 6 \cdot I \cdot b \cdot c \cdot d \cdot f) \cdot \text{dilog}((2 \cdot (I \cdot a \cdot b - b^2) \cdot \tan(f \cdot x + e))^2 - 2 \cdot a^2 - 2 \cdot I \cdot a \cdot b - (-2 \cdot I \cdot a^2 + 4 \cdot a \cdot b + 2 \cdot I \cdot b^2) \cdot \tan(f \cdot x + e)) / ((a^2 + b^2) \cdot \tan(f \cdot x + e))^2 + a^2 + b^2) + 1) + (-6 \cdot I \cdot b \cdot d^2 \cdot f \cdot x - 6 \cdot I \cdot b \cdot c \cdot d \cdot f) \cdot \text{dilog}((2 \cdot (-I \cdot a \cdot b - b^2) \cdot \tan(f \cdot x + e))^2 - 2 \cdot a^2 + 2 \cdot I \cdot a \cdot b - (2 \cdot I \cdot a^2 + 4 \cdot a \cdot b - 2 \cdot I \cdot b^2) \cdot \tan(f \cdot x + e)) / ((a^2 + b^2) \cdot \tan(f \cdot x + e))^2 + a^2 + b^2) + 1) + 6 \cdot (b \cdot d^2 \cdot f^2 \cdot x^2 + 2 \cdot b \cdot c \cdot d \cdot f^2 \cdot x - b \cdot d^2 \cdot e^2 + 2 \cdot b \cdot c \cdot d \cdot e \cdot f) \cdot \log(-2 \cdot (I \cdot a \cdot b - b^2) \cdot \tan(f \cdot x + e))^2 - 2 \cdot a^2 - 2 \cdot I \cdot a \cdot b - (-2 \cdot I \cdot a^2 + 4 \cdot a \cdot b + 2 \cdot I \cdot b^2) \cdot \tan(f \cdot x + e)) / ((a^2 + b^2) \cdot \tan(f \cdot x + e))^2 + a^2 + b^2) + 6 \cdot (b \cdot d^2 \cdot f^2 \cdot x^2 + 2 \cdot b \cdot c \cdot d \cdot f^2 \cdot x - b \cdot d^2 \cdot e^2 + 2 \cdot b \cdot c \cdot d \cdot e \cdot f) \cdot \log(-2 \cdot (-I \cdot a \cdot b - b^2) \cdot \tan(f \cdot x + e))^2 - 2 \cdot a^2 + 2 \cdot I \cdot a \cdot b - (2 \cdot I \cdot a^2 + 4 \cdot a \cdot b - 2 \cdot I \cdot b^2) \cdot \tan(f \cdot x + e)) / ((a^2 + b^2) \cdot \tan(f \cdot x + e))^2 + a^2 + b^2) + 6 \cdot (b \cdot d^2 \cdot e^2 - 2 \cdot b \cdot c \cdot d \cdot e \cdot f + b \cdot c^2 \cdot f^2) \cdot \log(((I \cdot a \cdot b + b^2) \cdot \tan(f \cdot x + e))^2 - a^2 + I \cdot a \cdot b + (I \cdot a^2 + I \cdot b^2) \cdot \tan(f \cdot x + e)) / (\tan(f \cdot x + e)^2 + 1)) + 6 \cdot (b \cdot d^2 \cdot e^2 - 2 \cdot b \cdot c \cdot d \cdot e \cdot f + b \cdot c^2 \cdot f^2) \cdot \log(((I \cdot a \cdot b - b^2) \cdot \tan(f \cdot x + e))^2 + a^2 + I \cdot a \cdot b + (I \cdot a^2 + I \cdot b^2) \cdot \tan(f \cdot x + e)) / (\tan(f \cdot x + e)^2 + 1))) / ((a^2 + b^2) \cdot f^3)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^2}{b \tan(fx+e) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+b*tan(f*x+e)),x, algorithm="giac")

[Out] integrate((d*x + c)^2/(b*tan(f*x + e) + a), x)

maple [B] time = 1.10, size = 922, normalized size = 5.09

$$\frac{\frac{d^2 x^3}{3(ib-a)} - \frac{cdx^2}{ib-a} - \frac{c^2 x}{ib-a} - \frac{ib d^2 \ln\left(1 - \frac{(-ib+a)e^{2i(fx+e)}}{-ib-a}\right) x^2}{f(ia+b)(-ib-a)} + \frac{ib c^2 \ln\left(ie^{2i(fx+e)}b - a e^{2i(fx+e)} - ib - a\right)}{f(ia+b)(ib+a)} - \frac{2b d^2 x}{3(ia+b)(-ib-a)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(a+b*tan(f*x+e)),x)

[Out] $-1/3 / (I \cdot b - a) \cdot d^2 \cdot x^3 - 1 / (I \cdot b - a) \cdot c \cdot d \cdot x^2 - 1 / (I \cdot b - a) \cdot c^2 \cdot x - I / f / (I \cdot a + b) \cdot b \cdot d^2 / (-I \cdot b - a) \cdot \ln(1 - (a - I \cdot b) \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) / (-I \cdot b - a)) \cdot x^2 + I / f / (I \cdot a + b) \cdot b \cdot c^2 / (a + I \cdot b) \cdot \ln(I \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) \cdot b - a \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) - I \cdot b - a) - 2/3 / (I \cdot a + b) \cdot b \cdot d^2 / (-I \cdot b - a) \cdot x^3 + 2/f^2 / (I \cdot a + b) \cdot b \cdot d^2 / (-I \cdot b - a) \cdot e^{2 \cdot x} + 4/3 / f^3 / (I \cdot a + b) \cdot b \cdot d^2 / (-I \cdot b - a) \cdot e^3 - 1/f^2 / (I \cdot a + b) \cdot b \cdot d^2 / (-I \cdot b - a) \cdot \text{polylog}(2, (a - I \cdot b) \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) / (-I \cdot b - a)) \cdot x + 4 \cdot I / f^2 / (I \cdot a + b) \cdot b \cdot c \cdot d \cdot e / (a + I \cdot b) \cdot \ln(\exp(I \cdot (f \cdot x + e))) - 2 \cdot I / f^3 / (I \cdot a + b) \cdot b \cdot d^2 \cdot e^2 / (a + I \cdot b) \cdot \ln(\exp(I \cdot (f \cdot x + e))) - 1/2 \cdot I / f^3 / (I \cdot a + b) \cdot b \cdot d^2 / (-I \cdot b - a) \cdot \text{polylog}(3, (a - I \cdot b) \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) / (-I \cdot b - a)) + I / f^3 / (I \cdot a + b) \cdot b \cdot d^2 \cdot e^2 / (a + I \cdot b) \cdot \ln(I \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) \cdot b - a \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) - I \cdot b - a) + I / f^3 / (I \cdot a + b) \cdot b \cdot d^2 \cdot e^2 / (-I \cdot b - a) \cdot \ln(1 - (a - I \cdot b) \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) / (-I \cdot b - a)) - 2 \cdot I / f / (I \cdot a + b) \cdot b \cdot c \cdot d / (-I \cdot b - a) \cdot \ln(1 - (a - I \cdot b) \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) / (-I \cdot b - a)) \cdot x - 2 \cdot I / f^2 / (I \cdot a + b) \cdot b \cdot c \cdot d / (-I \cdot b - a) \cdot \ln(1 - (a - I \cdot b) \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) / (-I \cdot b - a)) \cdot e - 2 \cdot I / f^2 / (I \cdot a + b) \cdot b \cdot c \cdot d \cdot e / (a + I \cdot b) \cdot \ln(I \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) \cdot b - a \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) - I \cdot b - a) - 2 \cdot I / f / (I \cdot a + b) \cdot b \cdot c^2 / (a + I \cdot b) \cdot \ln(\exp(I \cdot (f \cdot x + e))) - 2 / (I \cdot a + b) \cdot b \cdot c \cdot d / (-I \cdot b - a) \cdot x^2 - 4 / f / (I \cdot a + b) \cdot b \cdot c \cdot d / (-I \cdot b - a) \cdot e \cdot x - 2 / f^2 / (I \cdot a + b) \cdot b \cdot c \cdot d / (-I \cdot b - a) \cdot e^2 - 1 / f^2 / (I \cdot a + b) \cdot b \cdot c \cdot d / (-I \cdot b - a) \cdot \text{polylog}(2, (a - I \cdot b) \cdot \exp(2 \cdot I \cdot (f \cdot x + e)) / (-I \cdot b - a))$

maxima [B] time = 1.22, size = 712, normalized size = 3.93

$$6cde \left(\frac{2(fx+e)a}{(a^2+b^2)f} + \frac{2b \log(b \tan(fx+e)+a)}{(a^2+b^2)f} - \frac{b \log(\tan(fx+e)^2+1)}{(a^2+b^2)f} \right) - 3 \left(\frac{2(fx+e)a}{a^2+b^2} + \frac{2b \log(b \tan(fx+e)+a)}{a^2+b^2} - \frac{b \log(\tan(fx+e)^2+1)}{a^2+b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+b*tan(f*x+e)),x, algorithm="maxima")

[Out]
$$-1/6*(6*c*d*e*(2*(f*x + e)*a/((a^2 + b^2)*f) + 2*b*\log(b*\tan(f*x + e) + a)/((a^2 + b^2)*f) - b*\log(\tan(f*x + e)^2 + 1)/((a^2 + b^2)*f)) - 3*(2*(f*x + e)*a/(a^2 + b^2) + 2*b*\log(b*\tan(f*x + e) + a)/(a^2 + b^2) - b*\log(\tan(f*x + e)^2 + 1)/(a^2 + b^2))*c^2 - (2*(f*x + e)^3*(a - I*b)*d^2 + 6*(f*x + e)*(a - I*b)*d^2*e^2 + 6*I*b*d^2*e^2*\arctan2(-b*\cos(2*f*x + 2*e) + a*\sin(2*f*x + 2*e) + b, a*\cos(2*f*x + 2*e) + b*\sin(2*f*x + 2*e) + a) + 3*b*d^2*e^2*\log((a^2 + b^2)*\cos(2*f*x + 2*e)^2 + 4*a*b*\sin(2*f*x + 2*e) + (a^2 + b^2)*\sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*f*x + 2*e)) + 3*b*d^2*\text{polylog}(3, (I*a + b)*e^(2*I*f*x + 2*I*e)/(-I*a + b)) - 6*((a - I*b)*d^2*e - (a - I*b)*c*d*f)*(f*x + e)^2 + (-6*I*(f*x + e)^2*b*d^2 + (12*I*b*d^2*e - 12*I*b*c*d*f)*(f*x + e)*\arctan2((2*a*b*\cos(2*f*x + 2*e) - (a^2 - b^2)*\sin(2*f*x + 2*e))/(a^2 + b^2), (2*a*b*\sin(2*f*x + 2*e) + a^2 + b^2 + (a^2 - b^2)*\cos(2*f*x + 2*e))/(a^2 + b^2)) + (-6*I*(f*x + e)*b*d^2 + 6*I*b*d^2*e - 6*I*b*c*d*f)*\text{dilog}((I*a + b)*e^(2*I*f*x + 2*I*e)/(-I*a + b)) + 3*((f*x + e)^2*b*d^2 - 2*(b*d^2*e - b*c*d*f)*(f*x + e))*\log(((a^2 + b^2)*\cos(2*f*x + 2*e)^2 + 4*a*b*\sin(2*f*x + 2*e) + (a^2 + b^2)*\sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*\cos(2*f*x + 2*e))/(a^2 + b^2)))/((a^2 + b^2)*f^2))/f$$

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(c + dx)^2}{a + b \tan(e + fx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^2/(a + b*tan(e + f*x)),x)

[Out] int((c + d*x)^2/(a + b*tan(e + f*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^2}{a + b \tan(e + fx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2/(a+b*tan(f*x+e)),x)

[Out] Integral((c + d*x)**2/(a + b*tan(e + f*x)), x)

3.56 $\int \frac{c+dx}{a+b \tan(e+fx)} dx$

Optimal. Leaf size=125

$$\frac{b(c+dx) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f(a^2+b^2)} - \frac{ibd\text{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^2(a^2+b^2)} + \frac{(c+dx)^2}{2d(a+ib)}$$

[Out] $1/2*(d*x+c)^2/(a+I*b)/d+b*(d*x+c)*\ln(1+(a^2+b^2)*\exp(2*I*(f*x+e))/(a+I*b)^2)/(a^2+b^2)/f-1/2*I*b*d*\text{polylog}(2,-(a^2+b^2)*\exp(2*I*(f*x+e))/(a+I*b)^2)/(a^2+b^2)/f^2$

Rubi [A] time = 0.16, antiderivative size = 125, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {3732, 2190, 2279, 2391}

$$\frac{b(c+dx) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f(a^2+b^2)} - \frac{ibd\text{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2f^2(a^2+b^2)} + \frac{(c+dx)^2}{2d(a+ib)}$$

Antiderivative was successfully verified.

[In] `Int[(c + d*x)/(a + b*Tan[e + f*x]),x]`

[Out] $(c + d*x)^2/(2*(a + I*b)*d) + (b*(c + d*x)*\text{Log}[1 + ((a^2 + b^2)*E^{((2*I)*(e + f*x))})/(a + I*b)^2])/((a^2 + b^2)*f) - ((I/2)*b*d*\text{PolyLog}[2, -((a^2 + b^2)*E^{((2*I)*(e + f*x))})/(a + I*b)^2])/((a^2 + b^2)*f^2)$

Rule 2190

```
Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/
((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp
[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a]]/(b*f*g*n*Log[F]), x] - Di
st[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)
))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2279

```
Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_))))^(n_)], x_Symbol]
:= Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)
))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2391

```
Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := -Simp[PolyLog[2
, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rule 3732

```
Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Sy
mbol] := Simp[(c + d*x)^(m + 1)/(d*(m + 1)*(a + I*b)), x] + Dist[2*I*b, Int
[((c + d*x)^m*E^Simp[2*I*(e + f*x), x]]/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2
*I*(e + f*x), x]), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2,
0] && IGtQ[m, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{c + dx}{a + b \tan(e + fx)} dx &= \frac{(c + dx)^2}{2(a + ib)d} + (2ib) \int \frac{e^{2i(e+fx)}(c + dx)}{(a + ib)^2 + (a^2 + b^2)e^{2i(e+fx)}} dx \\
&= \frac{(c + dx)^2}{2(a + ib)d} + \frac{b(c + dx) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2) f} - \frac{(bd) \int \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right) dx}{(a^2 + b^2) f} \\
&= \frac{(c + dx)^2}{2(a + ib)d} + \frac{b(c + dx) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2) f} + \frac{(ibd) \operatorname{Subst}\left(\int \frac{\log\left(1 + \frac{(a^2+b^2)x}{(a+ib)^2}\right)}{x} dx, x, \right)}{2(a^2 + b^2) f^2} \\
&= \frac{(c + dx)^2}{2(a + ib)d} + \frac{b(c + dx) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{(a^2 + b^2) f} - \frac{ibd \operatorname{Li}_2\left(-\frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{2(a^2 + b^2) f^2}
\end{aligned}$$

Mathematica [A] time = 1.92, size = 177, normalized size = 1.42

$$\frac{b(c + dx) \log\left(1 + \frac{(a+ib)e^{-2i(e+fx)}}{a-ib}\right)}{f(a^2 + b^2)} + \frac{ibd \operatorname{Li}_2\left(\frac{(-a-ib)e^{-2i(e+fx)}}{a-ib}\right)}{2f^2(a^2 + b^2)} + \frac{b(c + dx)^2}{d(a - ib)(-ia(1 + e^{2ie}) + b(-e^{2ie}) + b)} + \frac{x \cos(e)}{2(a \cos(e))}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)/(a + b*Tan[e + f*x]), x]

[Out] (b*(c + d*x)^2)/((a - I*b)*d*(b - b*E^((2*I)*e) - I*a*(1 + E^((2*I)*e)))) + (b*(c + d*x)*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(e + f*x)))]/((a^2 + b^2)*f) + ((I/2)*b*d*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x)))]/((a^2 + b^2)*f^2) + (x*(2*c + d*x)*Cos[e])/(2*(a*Cos[e] + b*Sin[e]))

fricas [B] time = 0.46, size = 533, normalized size = 4.26

$$\frac{2ad^2f^2x^2 + 4acf^2x + ibd \operatorname{Li}_2\left(\frac{2(iab-b^2)\tan(fx+e)^2 - 2a^2 - 2iab - (-2ia^2 + 4ab + 2ib^2)\tan(fx+e)}{(a^2+b^2)\tan(fx+e)^2 + a^2 + b^2} + 1\right) - ibd \operatorname{Li}_2\left(\frac{2(-iab-b^2)\tan(fx+e)}{(a^2+b^2)\tan(fx+e)^2 + a^2 + b^2}\right)}{f(a^2 + b^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+b*tan(f*x+e)), x, algorithm="fricas")

[Out] 1/4*(2*a*d*f^2*x^2 + 4*a*c*f^2*x + I*b*d*dilog((2*(I*a*b - b^2)*tan(f*x + e))^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2) + 1) - I*b*d*dilog((2*(-I*a*b - b^2)*tan(f*x + e))^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2) + 1) + 2*(b*d*f*x + b*d*e)*log(-(2*(I*a*b - b^2)*tan(f*x + e))^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2) + 2*(b*d*f*x + b*d*e)*log(-(2*(-I*a*b - b^2)*tan(f*x + e))^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2) - 2*(b*d*e - b*c*f)*log(((I*a*b + b^2)*tan(f*x + e))^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*tan(f*x + e))/(tan(f*x + e)^2 + 1) - 2*(b*d*e - b*c*f)*log(((I*a*b - b^2)*tan(f*x + e))^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*tan(f*x + e))/(tan(f*x + e)^2 + 1))/((a^2 + b^2)*f^2)

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{dx + c}{b \tan(fx + e) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+b*tan(f*x+e)),x, algorithm="giac")

[Out] integrate((d*x + c)/(b*tan(f*x + e) + a), x)

maple [B] time = 0.96, size = 462, normalized size = 3.70

$$\frac{dx^2}{2(ib-a)} - \frac{cx}{ib-a} - \frac{2bc \ln\left(e^{i(fx+e)}\right)}{f(-ib+a)(ib+a)} + \frac{bc \ln\left(i e^{2i(fx+e)} b - a e^{2i(fx+e)} - ib - a\right)}{f(-ib+a)(ib+a)} - \frac{bd \ln\left(1 - \frac{(-ib+a)e^{2i(fx+e)}}{-ib-a}\right)}{f(-ib+a)(-ib-a)} - \frac{bd \ln\left(1 - \frac{(-ib+a)e^{2i(fx+e)}}{-ib-a}\right)}{f(-ib+a)(-ib-a)} - \frac{bd \ln\left(1 - \frac{(-ib+a)e^{2i(fx+e)}}{-ib-a}\right)}{f(-ib+a)(-ib-a)} - \frac{bd \ln\left(1 - \frac{(-ib+a)e^{2i(fx+e)}}{-ib-a}\right)}{f(-ib+a)(-ib-a)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)/(a+b*tan(f*x+e)),x)

[Out] -1/2/(I*b-a)*d*x^2-1/(I*b-a)*c*x-2/f*b/(a-I*b)*c/(a+I*b)*ln(exp(I*(f*x+e)))
+1/f*b/(a-I*b)*c/(a+I*b)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e))-I*b-a)-
1/f*b/(a-I*b)*d/(-I*b-a)*ln(1-(a-I*b)*exp(2*I*(f*x+e)))/(-I*b-a)*x-1/f^2*b/
(a-I*b)*d/(-I*b-a)*ln(1-(a-I*b)*exp(2*I*(f*x+e)))/(-I*b-a)*e+I*b/(a-I*b)*d/
(-I*b-a)*x^2+2*I/f*b/(a-I*b)*d/(-I*b-a)*e*x+I/f^2*b/(a-I*b)*d/(-I*b-a)*e^2+
1/2*I/f^2*b/(a-I*b)*d/(-I*b-a)*polylog(2,(a-I*b)*exp(2*I*(f*x+e)))/(-I*b-a))
+2/f^2*b/(a-I*b)*d*e/(a+I*b)*ln(exp(I*(f*x+e)))-1/f^2*b/(a-I*b)*d*e/(a+I*b)
*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e))-I*b-a)

maxima [B] time = 1.76, size = 399, normalized size = 3.19

$$(a - ib)d f^2 x^2 + 2(a - ib)c f^2 x - 2i b d f x \arctan\left(\frac{2ab \cos(2fx+2e) - (a^2 - b^2) \sin(2fx+2e)}{a^2 + b^2}, \frac{2ab \sin(2fx+2e) + a^2 + b^2 + (a^2 - b^2) \cos(2fx+2e)}{a^2 + b^2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+b*tan(f*x+e)),x, algorithm="maxima")

[Out] 1/2*((a - I*b)*d*f^2*x^2 + 2*(a - I*b)*c*f^2*x - 2*I*b*d*f*x*arctan2((2*a*b*cos(2*f*x + 2*e) - (a^2 - b^2)*sin(2*f*x + 2*e))/(a^2 + b^2), (2*a*b*sin(2*f*x + 2*e) + a^2 + b^2 + (a^2 - b^2)*cos(2*f*x + 2*e))/(a^2 + b^2)) + b*d*f*x*log(((a^2 + b^2)*cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) + (a^2 + b^2)*sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e))/(a^2 + b^2)) + 2*I*b*c*f*arctan2(-b*cos(2*f*x + 2*e) + a*sin(2*f*x + 2*e) + b, a*cos(2*f*x + 2*e) + b*sin(2*f*x + 2*e) + a) + b*c*f*log((a^2 + b^2)*cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) + (a^2 + b^2)*sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e)) - I*b*d*dilog((I*a + b)*e^(2*I*f*x + 2*I*e)/(-I*a + b)))/((a^2 + b^2)*f^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{c + dx}{a + b \tan(e + fx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)/(a + b*tan(e + f*x)),x)

[Out] int((c + d*x)/(a + b*tan(e + f*x)), x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{c + dx}{a + b \tan(e + fx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)/(a+b*tan(f*x+e)),x)
```

```
[Out] Integral((c + d*x)/(a + b*tan(e + f*x)), x)
```

$$3.57 \quad \int \frac{1}{(c+dx)(a+b \tan(e+fx))} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{1}{(c+dx)(a+b \tan(e+fx))}, x\right)$$

[Out] Unintegrable(1/(d*x+c)/(a+b*tan(f*x+e)), x)

Rubi [A] time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{(c+dx)(a+b \tan(e+fx))} dx$$

Verification is Not applicable to the result.

[In] Int[1/((c + d*x)*(a + b*Tan[e + f*x])), x]

[Out] Defer[Int][1/((c + d*x)*(a + b*Tan[e + f*x])), x]

Rubi steps

$$\int \frac{1}{(c+dx)(a+b \tan(e+fx))} dx = \int \frac{1}{(c+dx)(a+b \tan(e+fx))} dx$$

Mathematica [A] time = 1.97, size = 0, normalized size = 0.00

$$\int \frac{1}{(c+dx)(a+b \tan(e+fx))} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/((c + d*x)*(a + b*Tan[e + f*x])), x]

[Out] Integrate[1/((c + d*x)*(a + b*Tan[e + f*x])), x]

fricas [A] time = 0.64, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{1}{adx + ac + (bdx + bc) \tan(fx + e)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e)), x, algorithm="fricas")

[Out] integral(1/(a*d*x + a*c + (b*d*x + b*c)*tan(f*x + e)), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(dx+c)(b \tan(fx+e)+a)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e)), x, algorithm="giac")

[Out] integrate(1/((d*x + c)*(b*tan(f*x + e) + a)), x)

maple [A] time = 1.72, size = 0, normalized size = 0.00

$$\int \frac{1}{(dx+c)(a+b \tan (fx+e))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)/(a+b*tan(f*x+e)),x)

[Out] int(1/(d*x+c)/(a+b*tan(f*x+e)),x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e)),x, algorithm="maxima")

[Out] Timed out

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{1}{(a+b \tan (e+f x))(c+d x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*tan(e + f*x))*(c + d*x)),x)

[Out] int(1/((a + b*tan(e + f*x))*(c + d*x)), x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+b \tan (e+f x))(c+d x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e)),x)

[Out] Integral(1/((a + b*tan(e + f*x))*(c + d*x)), x)

$$3.58 \quad \int \frac{1}{(c+dx)^2(a+b \tan(e+fx))} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{1}{(c+dx)^2(a+b \tan(e+fx))}, x\right)$$

[Out] Unintegrable(1/(d*x+c)^2/(a+b*tan(f*x+e)), x)

Rubi [A] time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))} dx$$

Verification is Not applicable to the result.

[In] Int[1/((c + d*x)^2*(a + b*Tan[e + f*x])), x]

[Out] Defer[Int][1/((c + d*x)^2*(a + b*Tan[e + f*x])), x]

Rubi steps

$$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))} dx = \int \frac{1}{(c+dx)^2(a+b \tan(e+fx))} dx$$

Mathematica [A] time = 4.98, size = 0, normalized size = 0.00

$$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/((c + d*x)^2*(a + b*Tan[e + f*x])), x]

[Out] Integrate[1/((c + d*x)^2*(a + b*Tan[e + f*x])), x]

fricas [A] time = 0.49, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{1}{ad^2x^2 + 2acdx + ac^2 + (bd^2x^2 + 2bcdx + bc^2) \tan(fx + e)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+b*tan(f*x+e)), x, algorithm="fricas")

[Out] integral(1/(a*d^2*x^2 + 2*a*c*d*x + a*c^2 + (b*d^2*x^2 + 2*b*c*d*x + b*c^2)*tan(f*x + e)), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+b*tan(f*x+e)), x, algorithm="giac")

[Out] Timed out

maple [A] time = 3.20, size = 0, normalized size = 0.00

$$\int \frac{1}{(dx+c)^2 (a+b \tan (fx+e))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^2/(a+b*tan(f*x+e)),x)

[Out] int(1/(d*x+c)^2/(a+b*tan(f*x+e)),x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+b*tan(f*x+e)),x, algorithm="maxima")

[Out] Timed out

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{1}{(a+b \tan (e+f x))(c+d x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*tan(e + f*x))*(c + d*x)^2),x)

[Out] int(1/((a + b*tan(e + f*x))*(c + d*x)^2), x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+b \tan (e+f x))(c+d x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**2/(a+b*tan(f*x+e)),x)

[Out] Integral(1/((a + b*tan(e + f*x))*(c + d*x)**2), x)

$$3.59 \quad \int \frac{(c+dx)^3}{(a+b \tan(e+fx))^2} dx$$

Optimal. Leaf size=848

$$\frac{b(c+dx)^4}{(ia-b)(a-ib)^2d} + \frac{(c+dx)^4}{4(a-ib)^2d} - \frac{b^2(c+dx)^4}{(a^2+b^2)^2d} + \frac{2b \log\left(\frac{e^{2ie+2ifx(a-ib)}}{a+ib} + 1\right)(c+dx)^3}{(a-ib)^2(a+ib)f} - \frac{2ib^2 \log\left(\frac{e^{2ie+2ifx(a-ib)}}{a+ib} + 1\right)(c+dx)^2}{(a^2+b^2)^2f}$$

[Out] $-3I*b^2*d^2*(d*x+c)*\text{polylog}(3, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^3+2*b^2*(d*x+c)^3/(a+I*b)/(I*a+b)^2/(I*a-b+(I*a+b)*\exp(2*I*e+2*I*f*x))/f+1/4*(d*x+c)^4/(a-I*b)^2/d+b*(d*x+c)^4/(I*a-b)/(a-I*b)^2/d-b^2*(d*x+c)^4/(a^2+b^2)^2/d+3*b^2*d*(d*x+c)^2*\ln(1+(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^2+2*b*(d*x+c)^3*\ln(1+(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a-I*b)^2/(a+I*b)/f-2*I*b^2*(d*x+c)^3*\ln(1+(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f-3*I*b^2*d^2*(d*x+c)*\text{polylog}(2, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^3+3*b*d*(d*x+c)^2*\text{polylog}(2, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(I*a-b)/(a-I*b)^2/f^2-3*b^2*d*(d*x+c)^2*\text{polylog}(2, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^2+3/2*b^2*d^3*\text{polylog}(3, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^4+3*b*d^2*(d*x+c)*\text{polylog}(3, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a-I*b)^2/(a+I*b)/f^3-2*I*b^2*(d*x+c)^3/(a^2+b^2)^2/f-3/2*b*d^3*\text{polylog}(4, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(I*a-b)/(a-I*b)^2/f^4+3/2*b^2*d^3*\text{polylog}(4, -(a-I*b)*\exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^4$

Rubi [A] time = 2.00, antiderivative size = 848, normalized size of antiderivative = 1.00, number of steps used = 21, number of rules used = 9, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.450$, Rules used = {3734, 2185, 2184, 2190, 2531, 6609, 2282, 6589, 2191}

$$\frac{b(c+dx)^4}{(ia-b)(a-ib)^2d} + \frac{(c+dx)^4}{4(a-ib)^2d} - \frac{b^2(c+dx)^4}{(a^2+b^2)^2d} + \frac{2b \log\left(\frac{e^{2ie+2ifx(a-ib)}}{a+ib} + 1\right)(c+dx)^3}{(a-ib)^2(a+ib)f} - \frac{2ib^2 \log\left(\frac{e^{2ie+2ifx(a-ib)}}{a+ib} + 1\right)(c+dx)^2}{(a^2+b^2)^2f}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)^3/(a + b*Tan[e + f*x])^2, x]

[Out] $((-2*I)*b^2*(c+d*x)^3)/((a^2+b^2)^2*f) + (2*b^2*(c+d*x)^3)/((a+I*b)*(I*a+b)^2*(I*a-b+(I*a+b)*E^((2*I)*e+(2*I)*f*x))*f) + (c+d*x)^4/(4*(a-I*b)^2*d) + (b*(c+d*x)^4)/((I*a-b)*(a-I*b)^2*d) - (b^2*(c+d*x)^4)/((a^2+b^2)^2*d) + (3*b^2*d*(c+d*x)^2*\text{Log}[1+((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((a^2+b^2)^2*f^2) + (2*b*(c+d*x)^3*\text{Log}[1+((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((a-I*b)^2*(a+I*b)*f) - ((2*I)*b^2*(c+d*x)^3*\text{Log}[1+((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((a^2+b^2)^2*f) - ((3*I)*b^2*d^2*(c+d*x)*\text{PolyLog}[2, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((a^2+b^2)^2*f^3) + (3*b*d*(c+d*x)^2*\text{PolyLog}[2, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((I*a-b)*(a-I*b)^2*f^2) - (3*b^2*d*(c+d*x)^2*\text{PolyLog}[2, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((a^2+b^2)^2*f^2) + (3*b^2*d^3*\text{PolyLog}[3, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((2*(a^2+b^2)^2*f^4) + (3*b*d^2*(c+d*x)*\text{PolyLog}[3, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((a-I*b)^2*(a+I*b)*f^3) - ((3*I)*b^2*d^2*(c+d*x)*\text{PolyLog}[3, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((a^2+b^2)^2*f^3) - (3*b*d^3*\text{PolyLog}[4, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((2*(I*a-b)*(a-I*b)^2*f^4) + (3*b^2*d^3*\text{PolyLog}[4, -(((a-I*b)*E^((2*I)*e+(2*I)*f*x))/(a+I*b)])/((2*(a^2+b^2)^2*f^4)$

Rule 2184

Int[((c_.) + (d_.)*(x_))^(m_.)/((a_.) + (b_.)*((F_)^(g_.)*((e_.) + (f_.)*(x_))))^(n_.), x_Symbol] :> Simp[(c + d*x)^(m + 1)/(a*d*(m + 1)), x] - Dist[

$b/a, \text{Int}[(c + dx)^m (F^{(g(e + fx)))^n}) / (a + b(F^{(g(e + fx)))^n}), x], x] /;$ FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2185

$\text{Int}[(a + b(F^{(g(e + fx)))^n})^{(p)} * ((c + d(x))^m), x_Symbol] := \text{Dist}[1/a, \text{Int}[(c + dx)^m (a + b(F^{(g(e + fx)))^n})^{(p + 1)}, x], x] - \text{Dist}[b/a, \text{Int}[(c + dx)^m (F^{(g(e + fx)))^n})^{(p)}, x], x] /;$ FreeQ[{F, a, b, c, d, e, f, g, n}, x] && ILtQ[p, 0] && IGtQ[m, 0]

Rule 2190

$\text{Int}[(F^{(g(e + fx)))^n} * ((c + d(x))^m) / ((a + b(F^{(g(e + fx)))^n})), x_Symbol] := \text{Simp}[(c + dx)^m \text{Log}[1 + (b(F^{(g(e + fx)))^n})/a] / (b*f*g*n*\text{Log}[F]), x] - \text{Dist}[(d*m) / (b*f*g*n*\text{Log}[F]), \text{Int}[(c + dx)^{(m - 1)} \text{Log}[1 + (b(F^{(g(e + fx)))^n})/a], x], x] /;$ FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2191

$\text{Int}[(F^{(g(e + fx)))^n} * ((a + b(F^{(g(e + fx)))^n})^{(p)} * ((c + d(x))^m), x_Symbol] := \text{Simp}[(c + dx)^m (a + b(F^{(g(e + fx)))^n})^{(p + 1)} / (b*f*g*n*(p + 1)*\text{Log}[F]), x] - \text{Dist}[(d*m) / (b*f*g*n*(p + 1)*\text{Log}[F]), \text{Int}[(c + dx)^{(m - 1)} (a + b(F^{(g(e + fx)))^n})^{(p + 1)}, x], x] /;$ FreeQ[{F, a, b, c, d, e, f, g, m, n, p}, x] && NeQ[p, -1]

Rule 2282

$\text{Int}[u, x_Symbol] := \text{With}[\{v = \text{FunctionOfExponential}[u, x]\}, \text{Dist}[v/D[v, x], \text{Subst}[\text{Int}[\text{FunctionOfExponentialFunction}[u, x]/x, x], x, v], x] /;$ FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^n)^m] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))* (F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]

Rule 2531

$\text{Int}[\text{Log}[1 + (e_)*(F^{(c_)*((a_) + (b_)*x)})^n] * ((f_ + g_)*(x))^m, x_Symbol] := -\text{Simp}[(f + gx)^m \text{PolyLog}[2, -(e(F^{(c(a + bx)))^n})] / (b*c*n*\text{Log}[F]), x] + \text{Dist}[(g*m) / (b*c*n*\text{Log}[F]), \text{Int}[(f + gx)^{(m - 1)} \text{PolyLog}[2, -(e(F^{(c(a + bx)))^n})], x], x] /;$ FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 3734

$\text{Int}[(c + d(x))^m * ((a + b*\tan[(e + f(x))])^n), x_Symbol] := \text{Int}[\text{ExpandIntegrand}[(c + dx)^m, (1/(a - I*b) - (2*I*b)/(a^2 + b^2 + (a - I*b)^2 * E^{(2*I*(e + fx))})^{-n}), x], x] /;$ FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0] && ILtQ[n, 0] && IGtQ[m, 0]

Rule 6589

$\text{Int}[\text{PolyLog}[n, (c_)*((a_) + (b_)*x)] / ((d_) + (e_)*(x)), x_Symbol] := \text{Simp}[\text{PolyLog}[n + 1, c*(a + bx)^p] / (e*p), x] /;$ FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rule 6609

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*(a_.) + (b_.
)*(x_)))^(p_.)], x_Symbol] :> Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p])/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{(c + dx)^3}{(a + b \tan(e + fx))^2} dx &= \int \left(\frac{(c + dx)^3}{(a - ib)^2} - \frac{4b^2(c + dx)^3}{(ia + b)^2 \left(ia \left(1 + \frac{ib}{a} \right) + ia \left(1 - \frac{ib}{a} \right) e^{2ie+2ifx} \right)^2} + \frac{4b(c + dx)^3}{(a - ib)^2 \left(ia \left(1 + \frac{ib}{a} \right) \right)} \right) dx \\ &= \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{(4b) \int \frac{(c+dx)^3}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ie+2ifx}} dx}{(a - ib)^2} - \frac{(4b^2) \int \frac{(c+dx)^3}{(ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ie+2ifx})^2} dx}{(ia + b)^2} \\ &= \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{b(c + dx)^4}{(ia - b)(a - ib)^2 d} + \frac{(4b^2) \int \frac{(c+dx)^3}{ia(1+\frac{ib}{a})+ia(1-\frac{ib}{a})e^{2ie+2ifx}} dx}{(ia - b)(a - ib)^2} - \frac{(4b) \int \frac{e^{2ie}}{ia(1+\frac{ib}{a})} dx}{a^2} \\ &= -\frac{2b^2(c + dx)^3}{(a - ib)^2(a + ib) \left(ia - b + (ia + b)e^{2ie+2ifx} \right) f} + \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{b(c + dx)^4}{(ia - b)(a - ib)^2 d} - \frac{b}{(a - ib)^2} \\ &= -\frac{2ib^2(c + dx)^3}{(a^2 + b^2)^2 f} - \frac{2b^2(c + dx)^3}{(a - ib)^2(a + ib) \left(ia - b + (ia + b)e^{2ie+2ifx} \right) f} + \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{b}{(ia - b)(a - ib)^2} \\ &= -\frac{2ib^2(c + dx)^3}{(a^2 + b^2)^2 f} - \frac{2b^2(c + dx)^3}{(a - ib)^2(a + ib) \left(ia - b + (ia + b)e^{2ie+2ifx} \right) f} + \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{b}{(ia - b)(a - ib)^2} \\ &= -\frac{2ib^2(c + dx)^3}{(a^2 + b^2)^2 f} - \frac{2b^2(c + dx)^3}{(a - ib)^2(a + ib) \left(ia - b + (ia + b)e^{2ie+2ifx} \right) f} + \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{b}{(ia - b)(a - ib)^2} \\ &= -\frac{2ib^2(c + dx)^3}{(a^2 + b^2)^2 f} - \frac{2b^2(c + dx)^3}{(a - ib)^2(a + ib) \left(ia - b + (ia + b)e^{2ie+2ifx} \right) f} + \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{b}{(ia - b)(a - ib)^2} \\ &= -\frac{2ib^2(c + dx)^3}{(a^2 + b^2)^2 f} - \frac{2b^2(c + dx)^3}{(a - ib)^2(a + ib) \left(ia - b + (ia + b)e^{2ie+2ifx} \right) f} + \frac{(c + dx)^4}{4(a - ib)^2 d} + \frac{b}{(ia - b)(a - ib)^2} \end{aligned}$$

Mathematica [A] time = 10.85, size = 1673, normalized size = 1.97

result too large to display

Warning: Unable to verify antiderivative.

```
[In] Integrate[(c + d*x)^3/(a + b*Tan[e + f*x])^2,x]
```

```
[Out] (b*((4*b*(c + d*x)^3)/(a - I*b) + (2*a*f*(c + d*x)^4)/((a - I*b)*d) + (12*c
*d*((-I)*b*(-1 + E^((2*I)*e)) + a*(1 + E^((2*I)*e))))*(b*d + a*c*f)*x*Log[1
```

$$\begin{aligned}
& + (a + I*b)/((a - I*b)*E^{((2*I)*(e + f*x))})/((a + I*b)*(I*a + b)*f) + (6*d^2*((-I)*b*(-1 + E^{((2*I)*e)}) + a*(1 + E^{((2*I)*e)}))*(b*d + 2*a*c*f)*x^2* \\
& \text{og}[1 + (a + I*b)/((a - I*b)*E^{((2*I)*(e + f*x))})]/((a + I*b)*(I*a + b)*f) \\
& + (4*a*d^3*((-I)*b*(-1 + E^{((2*I)*e)}) + a*(1 + E^{((2*I)*e)}))*x^3*\text{Log}[1 + (a \\
& + I*b)/((a - I*b)*E^{((2*I)*(e + f*x))})]/((a + I*b)*(I*a + b)) - (2*c^2*((-I)*b*(-1 + E^{((2*I)*e)}) + a*(1 + E^{((2*I)*e)}))* \\
& (3*b*d + 2*a*c*f)*(2*f*x + I*\text{Log}[a + I*b + (a - I*b)*E^{((2*I)*(e + f*x))})]/((a^2 + b^2)*f) + (6*c*d*((-I)*b*(-1 + E^{((2*I)*e)}) + a*(1 + E^{((2*I)*e)}))* \\
& (b*d + a*c*f)*\text{PolyLog}[2, (-a - I*b)/((a - I*b)*E^{((2*I)*(e + f*x))})]/((a^2 + b^2)*f^2) + (3*d^2*((-I)*b*(-1 + E^{((2*I)*e)}) + a*(1 + E^{((2*I)*e)}))* \\
& (b*d + 2*a*c*f)*(2*f*x*\text{PolyLog}[2, (-a - I*b)/((a - I*b)*E^{((2*I)*(e + f*x))})] - I*\text{PolyLog}[3, (-a - I*b)/ \\
& ((a - I*b)*E^{((2*I)*(e + f*x))})]/((a^2 + b^2)*f^3) + (3*a*d^3*((-I)*b*(-1 + E^{((2*I)*e)}) + a*(1 + E^{((2*I)*e)}))* \\
& (2*f^2*x^2*\text{PolyLog}[2, (-a - I*b)/((a - I*b)*E^{((2*I)*(e + f*x))})] - (2*I)*f*x*\text{PolyLog}[3, (-a - I*b)/((a - I*b)* \\
& E^{((2*I)*(e + f*x))})] - \text{PolyLog}[4, (-a - I*b)/((a - I*b)*E^{((2*I)*(e + f*x))})])]/((a^2 + b^2)*f^3))/((2*(a - I*b)*(a + I*b)*(b - b*E^{((2*I)*e)} - I*a*(\\
& 1 + E^{((2*I)*e)})*f) + (3*x^2*(a*c^2*d - I*b*c^2*d + a*c^2*d*\text{Cos}[2*e] + I*b*c^2*d*\text{Cos}[2*e] + I*a*c^2*d*\text{Sin}[2*e] - b*c^2*d*\text{Sin}[2*e]))/(2*(a - I*b)*(a + \\
& I*b)*(a + I*b + a*\text{Cos}[2*e] - I*b*\text{Cos}[2*e] + I*a*\text{Sin}[2*e] + b*\text{Sin}[2*e])) + \\
& (x^3*(a*c*d^2 - I*b*c*d^2 + a*c*d^2*\text{Cos}[2*e] + I*b*c*d^2*\text{Cos}[2*e] + I*a*c*d^2*\text{Sin}[2*e] - b*c*d^2*\text{Sin}[2*e]))/(a - I*b)*(a + I*b)*(a + I*b + a*\text{Cos}[2*e] \\
& - I*b*\text{Cos}[2*e] + I*a*\text{Sin}[2*e] + b*\text{Sin}[2*e])) + (x^4*(a*d^3 - I*b*d^3 + a*d^3*\text{Cos}[2*e] + I*b*d^3*\text{Cos}[2*e] + I*a*d^3*\text{Sin}[2*e] - b*d^3*\text{Sin}[2*e]))/(4*(a \\
& - I*b)*(a + I*b)*(a + I*b + a*\text{Cos}[2*e] - I*b*\text{Cos}[2*e] + I*a*\text{Sin}[2*e] + b*\text{Sin}[2*e])) + x*(c^3/(a^2 + (2*I)*a*b - b^2 + a^2*\text{Cos}[4*e] - (2*I)*a*b*\text{Cos}[4*e] \\
& - b^2*\text{Cos}[4*e] + I*a^2*\text{Sin}[4*e] + 2*a*b*\text{Sin}[4*e] - I*b^2*\text{Sin}[4*e])) + ((-a - I*b + a*\text{Cos}[2*e] - I*b*\text{Cos}[2*e] + I*a*\text{Sin}[2*e] + b*\text{Sin}[2*e))*((-4*I)*a*b \\
& *c^3*\text{Cos}[2*e] + 4*a*b*c^3*\text{Sin}[2*e]))/(a - I*b)*(a + I*b)*(a + I*b + a*\text{Cos}[2*e] - I*b*\text{Cos}[2*e] + I*a*\text{Sin}[2*e] + b*\text{Sin}[2*e))*(a^2 + (2*I)*a*b - b^2 + a^2*\text{Cos}[4*e] \\
& - (2*I)*a*b*\text{Cos}[4*e] - b^2*\text{Cos}[4*e] + I*a^2*\text{Sin}[4*e] + 2*a*b*\text{Sin}[4*e] - I*b^2*\text{Sin}[4*e])) + (c^3*\text{Cos}[4*e] + I*c^3*\text{Sin}[4*e])/(a^2 + (2*I)*a*b - b^2 + a^2*\text{Cos}[4*e] \\
& - (2*I)*a*b*\text{Cos}[4*e] - b^2*\text{Cos}[4*e] + I*a^2*\text{Sin}[4*e] + 2*a*b*\text{Sin}[4*e] - I*b^2*\text{Sin}[4*e])) + (b^2*c^3*\text{Sin}[f*x] + 3*b^2*c^2*d*x*\text{Sin}[f*x] + 3*b^2*c*d^2*x^2*\text{Sin}[f*x] + b^2*d^3*x^3*\text{Sin}[f*x])/((a - I*b)*(a + I*b)*f*(a*\text{Cos}[e] + b*\text{Sin}[e]))*(a*\text{Cos}[e + f*x] + b*\text{Sin}[e + f*x]))
\end{aligned}$$

fricas [C] time = 0.69, size = 2535, normalized size = 2.99

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+b*tan(f*x+e))^2,x, algorithm="fricas")

[Out] $1/4*((a^3 - a*b^2)*d^3*f^4*x^4 - 4*b^3*c^3*f^3 - 4*(b^3*d^3*f^3 - (a^3 - a*b^2)*c*d^2*f^4)*x^3 - 6*(2*b^3*c*d^2*f^3 - (a^3 - a*b^2)*c^2*d*f^4)*x^2 - 4*(3*b^3*c^2*d*f^3 - (a^3 - a*b^2)*c^3*f^4)*x + (6*I*a^2*b*d^3*f^2*x^2 + 6*I*a^2*b*c^2*d*f^2 + 6*I*a*b^2*c*d^2*f + 6*I*(2*a^2*b*c*d^2*f^2 + a*b^2*d^3*f)*x + (6*I*a*b^2*d^3*f^2*x^2 + 6*I*a*b^2*c^2*d*f^2 + 6*I*b^3*c*d^2*f + 6*I*(2*a*b^2*c*d^2*f^2 + b^3*d^3*f)*x)*\tan(f*x + e))*\text{dilog}((2*(I*a*b - b^2)*\tan(f*x + e))^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*\tan(f*x + e))/((a^2 + b^2)*\tan(f*x + e)^2 + a^2 + b^2) + 1) + (-6*I*a^2*b*d^3*f^2*x^2 - 6*I*a^2*b*c^2*d*f^2 - 6*I*a*b^2*c*d^2*f - 6*I*(2*a^2*b*c*d^2*f^2 + a*b^2*d^3*f)*x + (-6*I*a*b^2*d^3*f^2*x^2 - 6*I*a*b^2*c^2*d*f^2 - 6*I*b^3*c*d^2*f - 6*I*(2*a*b^2*c*d^2*f^2 + b^3*d^3*f)*x)*\tan(f*x + e))*\text{dilog}((2*(-I*a*b - b^2)*\tan(f*x + e))^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*\tan(f*x + e))/((a^2 + b^2)*\tan(f*x + e)^2 + a^2 + b^2) + 1) + 2*(2*a^2*b*d^3*f^3*x^3 + 2*a^2*b*d^3*e^3 + 6*a^2*b*c^2*d*e*f^2 - 3*a*b^2*d^3*e^2 + 3*(2*a^2*b*c*d^2*f^3 + a*b^2*d^3*f^2)*x^2 - 6*(a^2*b*c*d^2*e^2 - a*b^2*c*d^2*e)*f + 6*(a^2*b*c^2*d*f^3 + a*b^2*c*d^2*f^2)*x + (2*a*b^2*d^3*f^3*x^3 + 2*a*b^2*d^3*e^3 + 6*a*b^2*c^2*d*e*f^2 - 3*b^3*d^3*e^2 + 3*(2*a*b^2*c*d^2*f^3 + b^3*d^3*f^2))*$

```

x^2 - 6*(a*b^2*c*d^2*e^2 - b^3*c*d^2*e)*f + 6*(a*b^2*c^2*d*f^3 + b^3*c*d^2*
f^2)*x)*tan(f*x + e))*log(-(2*(I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 - 2*I*a*
b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2
+ a^2 + b^2)) + 2*(2*a^2*b*d^3*f^3*x^3 + 2*a^2*b*d^3*e^3 + 6*a^2*b*c^2*d*e*
f^2 - 3*a*b^2*d^3*e^2 + 3*(2*a^2*b*c*d^2*f^3 + a*b^2*d^3*f^2)*x^2 - 6*(a^2*
b*c*d^2*e^2 - a*b^2*c*d^2*e)*f + 6*(a^2*b*c^2*d*f^3 + a*b^2*c*d^2*f^2)*x +
(2*a*b^2*d^3*f^3*x^3 + 2*a*b^2*d^3*e^3 + 6*a*b^2*c^2*d*e*f^2 - 3*b^3*d^3*e^
2 + 3*(2*a*b^2*c*d^2*f^3 + b^3*d^3*f^2)*x^2 - 6*(a*b^2*c*d^2*e^2 - b^3*c*d^
2*e)*f + 6*(a*b^2*c^2*d*f^3 + b^3*c*d^2*f^2)*x)*tan(f*x + e))*log(-(2*(-I*a
*b - b^2)*tan(f*x + e)^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*ta
n(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) - 2*(2*a^2*b*d^3*e^3
- 2*a^2*b*c^3*f^3 - 3*a*b^2*d^3*e^2 + 3*(2*a^2*b*c^2*d*e - a*b^2*c^2*d)*f^2
- 6*(a^2*b*c*d^2*e^2 - a*b^2*c*d^2*e)*f + (2*a*b^2*d^3*e^3 - 2*a*b^2*c^3*f
^3 - 3*b^3*d^3*e^2 + 3*(2*a*b^2*c^2*d*e - b^3*c^2*d)*f^2 - 6*(a*b^2*c*d^2*e
^2 - b^3*c*d^2*e)*f)*tan(f*x + e))*log(((I*a*b + b^2)*tan(f*x + e)^2 - a^2
+ I*a*b + (I*a^2 + I*b^2)*tan(f*x + e))/(tan(f*x + e)^2 + 1)) - 2*(2*a^2*b*
d^3*e^3 - 2*a^2*b*c^3*f^3 - 3*a*b^2*d^3*e^2 + 3*(2*a^2*b*c^2*d*e - a*b^2*c^
2*d)*f^2 - 6*(a^2*b*c*d^2*e^2 - a*b^2*c*d^2*e)*f + (2*a*b^2*d^3*e^3 - 2*a*b
^2*c^3*f^3 - 3*b^3*d^3*e^2 + 3*(2*a*b^2*c^2*d*e - b^3*c^2*d)*f^2 - 6*(a*b^2
*c*d^2*e^2 - b^3*c*d^2*e)*f)*tan(f*x + e))*log(((I*a*b - b^2)*tan(f*x + e)^
2 + a^2 + I*a*b + (I*a^2 + I*b^2)*tan(f*x + e))/(tan(f*x + e)^2 + 1)) + (-3
*I*a*b^2*d^3*tan(f*x + e) - 3*I*a^2*b*d^3)*polylog(4, ((a^2 + 2*I*a*b - b^2
)*tan(f*x + e)^2 - a^2 - 2*I*a*b + b^2 + (2*I*a^2 - 4*a*b - 2*I*b^2)*tan(f*
x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + (3*I*a*b^2*d^3*tan(f*x
+ e) + 3*I*a^2*b*d^3)*polylog(4, ((a^2 - 2*I*a*b - b^2)*tan(f*x + e)^2 - a^
2 + 2*I*a*b + b^2 + (-2*I*a^2 - 4*a*b + 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)
*tan(f*x + e)^2 + a^2 + b^2)) + 3*(2*a^2*b*d^3*f*x + 2*a^2*b*c*d^2*f + a*b^
2*d^3 + (2*a*b^2*d^3*f*x + 2*a*b^2*c*d^2*f + b^3*d^3)*tan(f*x + e))*polylog
(3, ((a^2 + 2*I*a*b - b^2)*tan(f*x + e)^2 - a^2 - 2*I*a*b + b^2 + (2*I*a^2
- 4*a*b - 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2))
+ 3*(2*a^2*b*d^3*f*x + 2*a^2*b*c*d^2*f + a*b^2*d^3 + (2*a*b^2*d^3*f*x + 2*a
*b^2*c*d^2*f + b^3*d^3)*tan(f*x + e))*polylog(3, ((a^2 - 2*I*a*b - b^2)*tan
(f*x + e)^2 - a^2 + 2*I*a*b + b^2 + (-2*I*a^2 - 4*a*b + 2*I*b^2)*tan(f*x +
e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + ((a^2*b - b^3)*d^3*f^4*x^4
+ 4*a*b^2*c^3*f^3 + 4*(a*b^2*d^3*f^3 + (a^2*b - b^3)*c*d^2*f^4)*x^3 + 6*(2*
a*b^2*c*d^2*f^3 + (a^2*b - b^3)*c^2*d*f^4)*x^2 + 4*(3*a*b^2*c^2*d*f^3 + (a^
2*b - b^3)*c^3*f^4)*x)*tan(f*x + e))/((a^4*b + 2*a^2*b^3 + b^5)*f^4*tan(f*x
+ e) + (a^5 + 2*a^3*b^2 + a*b^4)*f^4)

```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx + c)^3}{(b \tan(fx + e) + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+b*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate((d*x + c)^3/(b*tan(f*x + e) + a)^2, x)

maple [B] time = 1.35, size = 3488, normalized size = 4.11

output too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^3/(a+b*tan(f*x+e))^2,x)

[Out] -1/4/(2*I*a*b-a^2+b^2)*d^3*x^4-1/(2*I*a*b-a^2+b^2)*c^3*x-12/(I*a+b)^2/f^2/(b-I*a)*b*a*c*d^2/(a+I*b)*e^2*x+6*I/(I*a+b)^2/f^2/(b-I*a)*b^2*c*d^2/(a+I*b)*ln(1-(I*b-a)*exp(2*I*(f*x+e)))/(a+I*b)*x+6*I/(I*a+b)^2/f^3/(b-I*a)*b^2*c*d^

$$\begin{aligned}
& 2/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*e+12*I/(I*a+b)^2/f^3/(b-I*a) \\
& *b^2*c*d^2*e/(a+I*b)*\ln(\exp(I*(f*x+e)))+3*I/(I*a+b)^2/f^3/(b-I*a)*b*a*c*d \\
& ^2/(a+I*b)*\text{polylog}(3,(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))+4*I/(I*a+b)^2/f^4/(b \\
& -I*a)*b*a*d^3*e^3/(a+I*b)*\ln(\exp(I*(f*x+e)))-2*I/(I*a+b)^2/f/(b-I*a)*b*a^2* \\
& c^3/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+2*I/(\\
& I*a+b)^2/f/(b-I*a)*b*a*d^3/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*x \\
& ^3+3*I/(I*a+b)^2/f^3/(b-I*a)*b*a*d^3/(a+I*b)*\text{polylog}(3,(I*b-a)*\exp(2*I*(f*x \\
& +e))/(a+I*b))*x+6/(I*a+b)^2/f/(b-I*a)*b^2*c*d^2/(a+I*b)*x^2+3/(I*a+b)^2/f^4 \\
& /(b-I*a)*b*a*d^3/(a+I*b)*e^4-3/2/(I*a+b)^2/f^4/(b-I*a)*b*a*d^3/(a+I*b)*\text{poly} \\
& \text{log}(4,(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))+6/(I*a+b)^2/f^3/(b-I*a)*b^2*c*d^2/(\\
& a+I*b)*e^2-6/(I*a+b)^2/f^3/(b-I*a)*b^2*d^3/(a+I*b)*e^2*x+3/(I*a+b)^2/f^3/(b \\
& -I*a)*b^2*d^3/(a+I*b)*\text{polylog}(2,(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*x+4/(I*a+ \\
& b)^2/(b-I*a)*b*a*c*d^2/(a+I*b)*x^3+6/(I*a+b)^2/(b-I*a)*b*a*c^2*d/(a+I*b)*x^ \\
& 2+3/2*I/(I*a+b)^2/f^4/(b-I*a)*b^2*d^3/(a+I*b)*\text{polylog}(3,(I*b-a)*\exp(2*I*(f* \\
& x+e))/(a+I*b))+3/(I*a+b)^2/f^3/(b-I*a)*b^2*c*d^2/(a+I*b)*\text{polylog}(2,(I*b-a)* \\
& \exp(2*I*(f*x+e))/(a+I*b))+2*I/(I*a+b)^2/f^4/(b-I*a)*b*a*d^3*e^3/(a+I*b)*\ln(\\
& 1-(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))+2/(I*a+b)^2/f^4/(b-I*a)*b^2*a*d^3*e^3/(\\
& a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+6/(I*a+b)^ \\
& 2/f^3/(b-I*a)*b^3*c*d^2*e/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I \\
& *(f*x+e))-I*b-a)+12/(I*a+b)^2/f/(b-I*a)*b*a*c^2*d/(a+I*b)*e*x+6/(I*a+b)^2/f \\
& ^2/(b-I*a)*b*a*c*d^2/(a+I*b)*\text{polylog}(2,(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*x+ \\
& 6*I/(I*a+b)^2/f^3/(b-I*a)*b^2*c*d^2*e/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e)) \\
& *b-a*\exp(2*I*(f*x+e))-I*b-a)+6*I/(I*a+b)^2/f^2/(b-I*a)*b*a^2*c^2*d*e/(a+I \\
& *b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)-6*I/(I*a+b)^2 \\
& /f^3/(b-I*a)*b*a^2*c*d^2*e^2/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(\\
& 2*I*(f*x+e))-I*b-a)+2*I/(I*a+b)^2/f^4/(b-I*a)*b*a^2*d^3*e^3/(a+I*b)/(I*b-a) \\
& *\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)-3*I/(I*a+b)^2/f^4/(b-I*a) \\
&)*b^2*d^3*e^2/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I* \\
& b-a)+12*I/(I*a+b)^2/f^2/(b-I*a)*b*a*c^2*d*e/(a+I*b)*\ln(\exp(I*(f*x+e)))+6*I \\
& /I*(I*a+b)^2/f^2/(b-I*a)*b*a*c^2*d/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f*x+e))/(a+ \\
& I*b))*e-6*I/(I*a+b)^2/f^3/(b-I*a)*b*a*c*d^2/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f \\
& *x+e))/(a+I*b))*e^2-6/(I*a+b)^2/f^3/(b-I*a)*b^2*a*c*d^2*e^2/(a+I*b)/(I*b-a) \\
& *\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+6*I/(I*a+b)^2/f/(b-I*a)* \\
& b*a*c^2*d/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*x+6*I/(I*a+b)^2/f/ \\
& (b-I*a)*b*a*c*d^2/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*x^2-12*I/(\\
& I*a+b)^2/f^3/(b-I*a)*b*a*c*d^2*e^2/(a+I*b)*\ln(\exp(I*(f*x+e)))-3*I/(I*a+b)^2 \\
& /f^2/(b-I*a)*b^2*c^2*d/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f \\
& *x+e))-I*b-a)+6/(I*a+b)^2/f^2/(b-I*a)*b^2*a*c^2*d*e/(a+I*b)/(I*b-a)*\ln(I* \\
& \exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+3/(I*a+b)^2/f^2/(b-I*a)*b*a*d^ \\
& 3/(a+I*b)*\text{polylog}(2,(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*x^2+3/(I*a+b)^2/f^2/(\\
& b-I*a)*b*a*c^2*d/(a+I*b)*\text{polylog}(2,(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))-2/(I*a \\
& +b)^2/f/(b-I*a)*b^2*a*c^3/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I \\
& *(f*x+e))-I*b-a)-3/(I*a+b)^2/f^4/(b-I*a)*b^3*d^3*e^2/(a+I*b)/(I*b-a)*\ln(I* \\
& \exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+6/(I*a+b)^2/f^2/(b-I*a)*b*a*c^2 \\
& *d/(a+I*b)*e^2-1/(2*I*a*b-a^2+b^2)*c*d^2*x^3-3/2/(2*I*a*b-a^2+b^2)*c^2*d*x^ \\
& 2-3*I/(I*a+b)^2/f^4/(b-I*a)*b^2*d^3/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f*x+e)))/(\\
& a+I*b))*e^2-3/(I*a+b)^2/f^2/(b-I*a)*b^3*c^2*d/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I* \\
& (f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+4/(I*a+b)^2/f^3/(b-I*a)*b*a*d^3/(a+I*b \\
&)*e^3*x-8/(I*a+b)^2/f^3/(b-I*a)*b*a*c*d^2/(a+I*b)*e^3+12/(I*a+b)^2/f^2/(b-I \\
& *a)*b^2*c*d^2/(a+I*b)*e*x-6*I/(I*a+b)^2/f^4/(b-I*a)*b^2*d^3*e^2/(a+I*b)*\ln(\\
& \exp(I*(f*x+e)))+3*I/(I*a+b)^2/f^2/(b-I*a)*b^2*d^3/(a+I*b)*\ln(1-(I*b-a)*\exp(\\
& 2*I*(f*x+e))/(a+I*b))*x^2-6*I/(I*a+b)^2/f^2/(b-I*a)*b^2*c^2*d/(a+I*b)*\ln(\exp \\
& (I*(f*x+e)))-4*I/(I*a+b)^2/f/(b-I*a)*b*a*c^3/(a+I*b)*\ln(\exp(I*(f*x+e)))+1/ \\
& (I*a+b)^2/(b-I*a)*b*a*d^3/(a+I*b)*x^4-4/(I*a+b)^2/f^4/(b-I*a)*b^2*d^3/(a+I* \\
& b)*e^3+2/(I*a+b)^2/f/(b-I*a)*b^2*d^3/(a+I*b)*x^3-2*I*b^2*(d^3*x^3+3*c*d^2*x \\
& ^2+3*c^2*d*x+c^3)/(b-I*a)/f/(I*a+b)^2/(\exp(2*I*(f*x+e))*b+I*a*\exp(2*I*(f*x+ \\
& e))-b+I*a)
\end{aligned}$$

maxima [B] time = 8.20, size = 4668, normalized size = 5.50

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^3/(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out]
$$-(3c^2d^2e^2(2ab \log(b \tan(fx + e)) + a) / ((a^4 + 2a^2b^2 + b^4) * f) - ab \log(\tan(fx + e)^2 + 1) / ((a^4 + 2a^2b^2 + b^4) * f) - b / ((a^2b + b^3) * f * \tan(fx + e) + (a^3 + ab^2) * f) + (a^2 - b^2) * (fx + e) / ((a^4 + 2a^2b^2 + b^4) * f)) - (2ab \log(b \tan(fx + e)) + a) / (a^4 + 2a^2b^2 + b^4) - ab \log(\tan(fx + e)^2 + 1) / (a^4 + 2a^2b^2 + b^4) + (a^2 - b^2) * (fx + e) / (a^4 + 2a^2b^2 + b^4) - b / (a^3 + ab^2 + (a^2b + b^3) * \tan(fx + e))) * c^3 - ((3a^3 - 3Ia^2b + 3ab^2 - 3Ib^3) * (fx + e)^4 * d^3 + (-24Ia^2b^2 + 24b^3) * d^3 * e^3 + (72Ia^2b^2 - 72b^3) * c * d^2 * e^2 * f - ((12a^3 - 12Ia^2b + 12ab^2 - 12Ib^3) * d^3 * e - (12a^3 - 12Ia^2b + 12ab^2 - 12Ib^3) * c * d^2 * f) * (fx + e)^3 + ((18a^3 - 18Ia^2b + 18ab^2 - 18Ib^3) * d^3 * e^2 - (36a^3 - 36Ia^2b + 36ab^2 - 36Ib^3) * c * d^2 * e * f + (18a^3 - 18Ia^2b * b + 18ab^2 - 18Ib^3) * c^2 * d * f^2) * (fx + e)^2 - ((12a^3 - 12Ia^2b + 12ab^2 - 12Ib^3) * d^3 * e^3 - (36a^3 - 36Ia^2b + 36ab^2 - 36Ib^3) * c * d^2 * e^2 * f) * (fx + e) + ((-24Ia^2b^2 + 24ab^2) * d^3 * e^3 + (36Ia^2b^2 - 36b^3) * d^3 * e^2 + (36Ia^2b^2 - 36b^3) * c^2 * d * f^2 + ((72Ia^2b^2 - 72ab^2) * c * d^2 * e^2 + (-72Ia^2b^2 + 72b^3) * c * d^2 * e) * f + ((-24Ia^2b^2 - 24ab^2) * d^3 * e^3 + (36Ia^2b^2 + 36b^3) * d^3 * e^2 + (36Ia^2b^2 + 36b^3) * c^2 * d * f^2 + ((72Ia^2b^2 + 72ab^2) * c * d^2 * e^2 + (-72Ia^2b^2 - 72b^3) * c * d^2 * e) * f) * \cos(2fx + 2e) + 12 * (2 * (a^2b - Iab^2) * d^3 * e^3 - 3 * (ab^2 - Ib^3) * d^3 * e^2 - 3 * (ab^2 - Ib^3) * c^2 * d * f^2 - 6 * ((a^2b - Iab^2) * c * d^2 * e^2 - (ab^2 - Ib^3) * c * d^2 * e) * f) * \sin(2fx + 2e)) * \arctan2(-b * \cos(2fx + 2e) + a * \sin(2fx + 2e) + b, a * \cos(2fx + 2e) + b * \sin(2fx + 2e) + a) + ((-32Ia^2b + 32ab^2) * (fx + e)^3 * d^3 + ((72Ia^2b^2 - 72ab^2) * d^3 * e + (-72Ia^2b^2 + 72ab^2) * c * d^2 * f + (-36Ia^2b^2 + 36b^3) * d^3) * (fx + e)^2 + ((-72Ia^2b^2 + 72ab^2) * d^3 * e^2 + (-72Ia^2b^2 + 72ab^2) * c^2 * d * f^2 + (72Ia^2b^2 - 72b^3) * d^3 * e + ((144Ia^2b^2 - 144ab^2) * c * d^2 * e + (-72Ia^2b^2 + 72b^3) * c * d^2) * f) * (fx + e) + ((-32Ia^2b^2 - 32ab^2) * (fx + e)^3 * d^3 + ((72Ia^2b^2 + 72ab^2) * d^3 * e + (-72Ia^2b^2 - 72ab^2) * c * d^2 * f + (-36Ia^2b^2 - 36b^3) * d^3) * (fx + e)^2 + ((-72Ia^2b^2 - 72ab^2) * c^2 * d * f^2 + (72Ia^2b^2 + 72b^3) * d^3 * e + ((144Ia^2b^2 + 144ab^2) * c * d^2 * e + (-72Ia^2b^2 - 72b^3) * c * d^2) * f) * (fx + e)) * \cos(2fx + 2e) + 4 * (8 * (a^2b - Iab^2) * (fx + e)^3 * d^3 - 9 * (2 * (a^2b - Iab^2) * d^3 * e - 2 * (a^2b - Iab^2) * c * d^2 * f - (ab^2 - Ib^3) * d^3) * (fx + e)^2 + 18 * ((a^2b - Iab^2) * d^3 * e^2 + (a^2b - Iab^2) * c^2 * d * f^2 - (ab^2 - Ib^3) * d^3 * e - (2 * (a^2b - Iab^2) * c * d^2 * e - (ab^2 - Ib^3) * c * d^2) * f) * (fx + e)) * \sin(2fx + 2e)) * \arctan2((2ab * \cos(2fx + 2e) - (a^2 - b^2) * \sin(2fx + 2e)) / (a^2 + b^2), (2ab * \sin(2fx + 2e) + a^2 + b^2 + (a^2 - b^2) * \cos(2fx + 2e)) / (a^2 + b^2)) + ((3a^3 - 9Ia^2b - 9ab^2 + 3Ib^3) * (fx + e)^4 * d^3 - ((12a^3 - 36Ia^2b - 36ab^2 + 12Ib^3) * d^3 * e - (12a^3 - 36Ia^2b - 36ab^2 + 12Ib^3) * c * d^2 * f - (-24Ia^2b^2 - 24b^3) * d^3) * (fx + e)^3 + ((18a^3 - 54Ia^2b - 54ab^2 + 18Ib^3) * d^3 * e^2 + (18a^3 - 54Ia^2b - 54ab^2 + 18Ib^3) * c^2 * d * f^2 + (72Ia^2b^2 + 72b^3) * d^3 * e - ((36a^3 - 108Ia^2b - 108ab^2 + 36Ib^3) * c * d^2 * e - (-72Ia^2b^2 - 72b^3) * c * d^2) * f) * (fx + e)^2 - ((12a^3 - 36Ia^2b - 36ab^2 + 12Ib^3) * d^3 * e^3 - (-72Ia^2b^2 - 72b^3) * d^3 * e^2 - (-72Ia^2b^2 - 72b^3) * c^2 * d * f^2 - ((36a^3 - 108Ia^2b - 108ab^2 + 36Ib^3) * c * d^2 * e^2 + (144Ia^2b^2 + 144b^3) * c * d^2 * e) * f) * (fx + e)) * \cos(2fx + 2e) + ((-48Ia^2b^2 + 48ab^2) * (fx + e)^2 * d^3 + (-36Ia^2b^2 + 36ab^2) * d^3 * e^2 + (-36Ia^2b^2 + 36ab^2) * c^2 * d * f^2 + (36Ia^2b^2 - 36b^3) * d^3 * e + ((72Ia^2b^2 - 72ab^2) * d^3 * e + (-72Ia^2b^2 + 72ab^2) * c * d^2 * f + (-36Ia^2b^2 + 36b^3) * d^3) * (fx + e) + ((72Ia^2b^2 - 72ab^2) * c * d^2 * e + (-36Ia^2b^2 + 36b^3) * c * d^2) * f + ((-48Ia^2b^2 - 48ab^2) * (fx + e)^2 * d^3 + (-36Ia^2b^2 - 36ab^2) * d^3 * e^2 + (-36Ia^2b^2 - 36ab^2) * c^2 * d * f^2 + (36Ia^2b^2 + 36b^3) * d^3 * e + ((72Ia^2b^2 + 72ab^2) * d^3 * e + (-72Ia^2b^2 - 72ab^2) * c * d^2 * f + (-36Ia^2b^2 - 36b^3) * d^3) * (fx + e) + ((72Ia^2b^2 + 72ab^2) * c * d^2 * e + (-36Ia^2b^2 - 36b^3) * c * d^2) * f) * \cos(2fx + 2e) + 12 * (4 * (a^2b - Iab^2) * (fx +$$


```

e)^2*d^3 + 3*(a^2*b - I*a*b^2)*d^3*e^2 + 3*(a^2*b - I*a*b^2)*c^2*d*f^2 - 3
*(a*b^2 - I*b^3)*d^3*e - 3*(2*(a^2*b - I*a*b^2)*d^3*e - 2*(a^2*b - I*a*b^2)
*c*d^2*f - (a*b^2 - I*b^3)*d^3)*(f*x + e) - 3*(2*(a^2*b - I*a*b^2)*c*d^2*e
- (a*b^2 - I*b^3)*c*d^2)*f)*sin(2*f*x + 2*e))*dilog((I*a + b)*e^(2*I*f*x +
2*I*e)/(-I*a + b)) - (12*(a^2*b + I*a*b^2)*d^3*e^3 - 18*(a*b^2 + I*b^3)*d^3
*e^2 - 18*(a*b^2 + I*b^3)*c^2*d*f^2 - 36*((a^2*b + I*a*b^2)*c*d^2*e^2 - (a*
b^2 + I*b^3)*c*d^2*e)*f + 6*(2*(a^2*b - I*a*b^2)*d^3*e^3 - 3*(a*b^2 - I*b^3
)*d^3*e^2 - 3*(a*b^2 - I*b^3)*c^2*d*f^2 - 6*((a^2*b - I*a*b^2)*c*d^2*e^2 -
(a*b^2 - I*b^3)*c*d^2*e)*f)*cos(2*f*x + 2*e) - ((-12*I*a^2*b - 12*a*b^2)*d^
3*e^3 + (18*I*a*b^2 + 18*b^3)*d^3*e^2 + (18*I*a*b^2 + 18*b^3)*c^2*d*f^2 + (
36*I*a^2*b + 36*a*b^2)*c*d^2*e^2 + (-36*I*a*b^2 - 36*b^3)*c*d^2*e)*f)*sin(
2*f*x + 2*e))*log((a^2 + b^2)*cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) +
(a^2 + b^2)*sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e)
)) + (16*(a^2*b + I*a*b^2)*(f*x + e)^3*d^3 - 18*(2*(a^2*b + I*a*b^2)*d^3*e
- 2*(a^2*b + I*a*b^2)*c*d^2*f - (a*b^2 + I*b^3)*d^3)*(f*x + e)^2 + 36*((a^2
*b + I*a*b^2)*d^3*e^2 + (a^2*b + I*a*b^2)*c^2*d*f^2 - (a*b^2 + I*b^3)*d^3*e
- (2*(a^2*b + I*a*b^2)*c*d^2*e - (a*b^2 + I*b^3)*c*d^2)*f)*(f*x + e) + 2*(
8*(a^2*b - I*a*b^2)*(f*x + e)^3*d^3 - 9*(2*(a^2*b - I*a*b^2)*d^3*e - 2*(a^2
*b - I*a*b^2)*c*d^2*f - (a*b^2 - I*b^3)*d^3)*(f*x + e)^2 + 18*((a^2*b - I*a
*b^2)*d^3*e^2 + (a^2*b - I*a*b^2)*c^2*d*f^2 - (a*b^2 - I*b^3)*d^3*e - (2*(a
^2*b - I*a*b^2)*c*d^2*e - (a*b^2 - I*b^3)*c*d^2)*f)*(f*x + e))*cos(2*f*x +
2*e) + ((16*I*a^2*b + 16*a*b^2)*(f*x + e)^3*d^3 + ((-36*I*a^2*b - 36*a*b^2)
*d^3*e + (36*I*a^2*b + 36*a*b^2)*c*d^2*f + (18*I*a*b^2 + 18*b^3)*d^3)*(f*x
+ e)^2 + ((36*I*a^2*b + 36*a*b^2)*d^3*e^2 + (36*I*a^2*b + 36*a*b^2)*c^2*d*f
^2 + (-36*I*a*b^2 - 36*b^3)*d^3*e + ((-72*I*a^2*b - 72*a*b^2)*c*d^2*e + (36
*I*a*b^2 + 36*b^3)*c*d^2)*f)*(f*x + e))*sin(2*f*x + 2*e))*log(((a^2 + b^2)*
cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) + (a^2 + b^2)*sin(2*f*x + 2*e)^
2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e))/(a^2 + b^2)) + ((24*I*a^2*b
+ 24*a*b^2)*d^3*cos(2*f*x + 2*e) - 24*(a^2*b - I*a*b^2)*d^3*sin(2*f*x + 2*
e) + (24*I*a^2*b - 24*a*b^2)*d^3)*polylog(4, (I*a + b)*e^(2*I*f*x + 2*I*e)/
(-I*a + b)) + (48*(a^2*b + I*a*b^2)*(f*x + e)*d^3 - 36*(a^2*b + I*a*b^2)*d^
3*e + 36*(a^2*b + I*a*b^2)*c*d^2*f + 18*(a*b^2 + I*b^3)*d^3 + 6*(8*(a^2*b -
I*a*b^2)*(f*x + e)*d^3 - 6*(a^2*b - I*a*b^2)*d^3*e + 6*(a^2*b - I*a*b^2)*c
*d^2*f + 3*(a*b^2 - I*b^3)*d^3)*cos(2*f*x + 2*e) + ((48*I*a^2*b + 48*a*b^2)
*(f*x + e)*d^3 + (-36*I*a^2*b - 36*a*b^2)*d^3*e + (36*I*a^2*b + 36*a*b^2)*c
*d^2*f + (18*I*a*b^2 + 18*b^3)*d^3)*sin(2*f*x + 2*e))*polylog(3, (I*a + b)*
e^(2*I*f*x + 2*I*e)/(-I*a + b)) + ((3*I*a^3 + 9*a^2*b - 9*I*a*b^2 - 3*b^3)*
(f*x + e)^4*d^3 + ((-12*I*a^3 - 36*a^2*b + 36*I*a*b^2 + 12*b^3)*d^3*e + (12
*I*a^3 + 36*a^2*b - 36*I*a*b^2 - 12*b^3)*c*d^2*f + 24*(a*b^2 - I*b^3)*d^3)*
(f*x + e)^3 + ((18*I*a^3 + 54*a^2*b - 54*I*a*b^2 - 18*b^3)*d^3*e^2 + (18*I*
a^3 + 54*a^2*b - 54*I*a*b^2 - 18*b^3)*c^2*d*f^2 - 72*(a*b^2 - I*b^3)*d^3*e
+ ((-36*I*a^3 - 108*a^2*b + 108*I*a*b^2 + 36*b^3)*c*d^2*e + 72*(a*b^2 - I*b
^3)*c*d^2)*f)*(f*x + e)^2 + ((-12*I*a^3 - 36*a^2*b + 36*I*a*b^2 + 12*b^3)*d
^3*e^3 + 72*(a*b^2 - I*b^3)*d^3*e^2 + 72*(a*b^2 - I*b^3)*c^2*d*f^2 + ((36*I
*a^3 + 108*a^2*b - 108*I*a*b^2 - 36*b^3)*c*d^2*e^2 - 144*(a*b^2 - I*b^3)*c*
d^2*e)*f)*(f*x + e))*sin(2*f*x + 2*e))/((12*a^5 - 12*I*a^4*b + 24*a^3*b^2 -
24*I*a^2*b^3 + 12*a*b^4 - 12*I*b^5)*f^3*cos(2*f*x + 2*e) + (12*I*a^5 + 12*
a^4*b + 24*I*a^3*b^2 + 24*a^2*b^3 + 12*I*a*b^4 + 12*b^5)*f^3*sin(2*f*x + 2*
e) + (12*a^5 + 12*I*a^4*b + 24*a^3*b^2 + 24*I*a^2*b^3 + 12*a*b^4 + 12*I*b^5
)*f^3))/f

```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^3}{(a + b \tan(e + fx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)^3/(a + b*tan(e + f*x))^2,x)

```
[Out] int((c + d*x)^3/(a + b*tan(e + f*x))^2, x)
```

```
sympy [F] time = 0.00, size = 0, normalized size = 0.00
```

$$\int \frac{(c + dx)^3}{(a + b \tan(e + fx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**3/(a+b*tan(f*x+e))**2,x)
```

```
[Out] Integral((c + d*x)**3/(a + b*tan(e + f*x))**2, x)
```

$$3.60 \quad \int \frac{(c+dx)^2}{(a+b \tan(e+fx))^2} dx$$

Optimal. Leaf size=654

$$\frac{2b^2d(c+dx)\operatorname{Li}_2\left(-\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f^2(a^2+b^2)^2} + \frac{2b^2d(c+dx)\log\left(1+\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f^2(a^2+b^2)^2} - \frac{2ib^2(c+dx)^2\log\left(1+\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f(a^2+b^2)^2} - \frac{2ib^2(c+dx)^2\log\left(1+\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f(a^2+b^2)^2}$$

```
[Out] -2*I*b^2*(d*x+c)^2/(a^2+b^2)^2/f+2*b^2*(d*x+c)^2/(a+I*b)/(I*a+b)^2/(I*a-b+(I*a+b)*exp(2*I*e+2*I*f*x))/f+1/3*(d*x+c)^3/(a-I*b)^2/d+4/3*b*(d*x+c)^3/(I*a-b)/(a-I*b)^2/d-4/3*b^2*(d*x+c)^3/(a^2+b^2)^2/d+2*b^2*d*(d*x+c)*ln(1+(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^2+2*b*(d*x+c)^2*ln(1+(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(a-I*b)^2/(a+I*b)/f-2*I*b^2*(d*x+c)^2*ln(1+(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f-2*b^2*d^2*polylog(2,-(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^2+2*b*d*(d*x+c)*polylog(2,-(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(I*a-b)/(a-I*b)^2/f^2-2*b^2*d*(d*x+c)*polylog(2,-(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^2+b*d^2*polylog(3,-(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(a-I*b)^2/(a+I*b)/f^3-2*b^2*d^2*polylog(3,-(a-I*b)*exp(2*I*e+2*I*f*x)/(a+I*b))/(a^2+b^2)^2/f^3
```

Rubi [A] time = 1.54, antiderivative size = 654, normalized size of antiderivative = 1.00, number of steps used = 18, number of rules used = 10, integrand size = 20, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {3734, 2185, 2184, 2190, 2531, 2282, 6589, 2191, 2279, 2391}

$$\frac{2b^2d(c+dx)\operatorname{Li}_2\left(-\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f^2(a^2+b^2)^2} + \frac{2b^2d(c+dx)\log\left(1+\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f^2(a^2+b^2)^2} - \frac{2ib^2(c+dx)^2\log\left(1+\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f(a^2+b^2)^2} - \frac{2ib^2(c+dx)^2\log\left(1+\frac{(a-ib)e^{2ie+2ifx}}{a+ib}\right)}{f(a^2+b^2)^2}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^2/(a + b*Tan[e + f*x])^2,x]
```

```
[Out] ((-2*I)*b^2*(c + d*x)^2)/((a^2 + b^2)^2*f) + (2*b^2*(c + d*x)^2)/((a + I*b)*(I*a + b)^2*(I*a - b + (I*a + b)*E^((2*I)*e + (2*I)*f*x))*f) + (c + d*x)^3/(3*(a - I*b)^2*d) + (4*b*(c + d*x)^3)/(3*(I*a - b)*(a - I*b)^2*d) - (4*b^2*(c + d*x)^3)/(3*(a^2 + b^2)^2*d) + (2*b^2*d*(c + d*x)*Log[1 + ((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b)])/(a^2 + b^2)^2*f^2) + (2*b*(c + d*x)^2*Log[1 + ((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b)])/(a - I*b)^2*(a + I*b)*f) - ((2*I)*b^2*(c + d*x)^2*Log[1 + ((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b)])/(a^2 + b^2)^2*f) - (I*b^2*d^2*PolyLog[2, -(((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b))])/(a^2 + b^2)^2*f^3) + (2*b*d*(c + d*x)*PolyLog[2, -(((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b))])/(I*a - b)*(a - I*b)^2*f^2) - (2*b^2*d*(c + d*x)*PolyLog[2, -(((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b))])/(a^2 + b^2)^2*f^2) + (b*d^2*PolyLog[3, -(((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b))])/(a - I*b)^2*(a + I*b)*f^3) - (I*b^2*d^2*PolyLog[3, -(((a - I*b)*E^((2*I)*e + (2*I)*f*x))/(a + I*b))])/(a^2 + b^2)^2*f^3)
```

Rule 2184

```
Int[((c_.) + (d_.)*(x_))^(m_.)/((a_.) + (b_.)*((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)), x_Symbol] := Simp[(c + d*x)^(m + 1)/(a*d*(m + 1)), x] - Dist[b/a, Int[(c + d*x)^m*(F^(g*(e + f*x)))^n/(a + b*(F^(g*(e + f*x)))^n), x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2185

```
Int[((a_.) + (b_.)*((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.))^p)*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] := Dist[1/a, Int[(c + d*x)^m*(a + b*(F^(g*(e + f*x))))^n, x], x]
```

$(f*x)))^n)^{p+1}, x], x] - \text{Dist}[b/a, \text{Int}[(c + d*x)^m*(F^{(g*(e + f*x)))^n*(a + b*(F^{(g*(e + f*x)))^n})^p, x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, n\}, x] \&\& \text{ILtQ}[p, 0] \&\& \text{IGtQ}[m, 0]$

Rule 2190

$\text{Int}[(((F_)^{(g_)*((e_)+(f_)*(x_)))^{(n_)*((c_)+(d_)*(x_))^{(m_)}})/((a_)+(b_)*((F_)^{(g_)*((e_)+(f_)*(x_)))^{(n_)}), x_Symbol] \rightarrow \text{Simp}[(c + d*x)^m*\text{Log}[1 + (b*(F^{(g*(e + f*x)))^n})/a]]/(b*f*g*n*\text{Log}[F]), x] - \text{Dist}[(d*m)/(b*f*g*n*\text{Log}[F]), \text{Int}[(c + d*x)^{(m-1)}*\text{Log}[1 + (b*(F^{(g*(e + f*x)))^n})/a], x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, n\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 2191

$\text{Int}[((F_)^{(g_)*((e_)+(f_)*(x_)))^{(n_)*((a_)+(b_)*((F_)^{(g_)*((e_)+(f_)*(x_)))^{(n_)}))^{(p_)*((c_)+(d_)*(x_))^{(m_)}), x_Symbol] \rightarrow \text{Simp}[(c + d*x)^m*(a + b*(F^{(g*(e + f*x)))^n})^{(p+1)}]/(b*f*g*n*(p+1)*\text{Log}[F]), x] - \text{Dist}[(d*m)/(b*f*g*n*(p+1)*\text{Log}[F]), \text{Int}[(c + d*x)^{(m-1)}*(a + b*(F^{(g*(e + f*x)))^n})^{(p+1)}, x], x] /; \text{FreeQ}\{F, a, b, c, d, e, f, g, m, n, p\}, x] \&\& \text{NeQ}[p, -1]$

Rule 2279

$\text{Int}[\text{Log}[(a_)+(b_)*((F_)^{(e_)*((c_)+(d_)*(x_)))^{(n_)}], x_Symbol] \rightarrow \text{Dist}[1/(d*e*n*\text{Log}[F]), \text{Subst}[\text{Int}[\text{Log}[a + b*x]/x, x], x, (F^{(e*(c + d*x))})^n], x] /; \text{FreeQ}\{F, a, b, c, d, e, n\}, x] \&\& \text{GtQ}[a, 0]$

Rule 2282

$\text{Int}[u, x_Symbol] \rightarrow \text{With}\{v = \text{FunctionOfExponential}[u, x]\}, \text{Dist}[v/D[v, x], \text{Subst}[\text{Int}[\text{FunctionOfExponentialFunction}[u, x]/x, x], x, v], x] /; \text{FunctionOfExponentialQ}[u, x] \&\& !\text{MatchQ}[u, (w_)*((a_)*(v_)^{(n_))^{(m_)} /; \text{FreeQ}\{a, m, n\}, x] \&\& \text{IntegerQ}[m*n] \&\& !\text{MatchQ}[u, E^{((c_)*((a_)+(b_)*x))* (F_)[v_]} /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{InverseFunctionQ}[F[x]]$

Rule 2391

$\text{Int}[\text{Log}[(c_)*((d_)+(e_)*(x_)^{(n_)})]/(x_), x_Symbol] \rightarrow -\text{Simp}[\text{PolyLog}[2, -(c*e*x^n)]/n, x] /; \text{FreeQ}\{c, d, e, n\}, x] \&\& \text{EqQ}[c*d, 1]$

Rule 2531

$\text{Int}[\text{Log}[1 + (e_)*((F_)^{(c_)*((a_)+(b_)*(x_)))^{(n_)}]*(f_)+(g_)*(x_))^{(m_)}, x_Symbol] \rightarrow -\text{Simp}[(f + g*x)^m*\text{PolyLog}[2, -(e*(F^{(c*(a + b*x)))^n})]]/(b*c*n*\text{Log}[F]), x] + \text{Dist}[(g*m)/(b*c*n*\text{Log}[F]), \text{Int}[(f + g*x)^{(m-1)}*\text{PolyLog}[2, -(e*(F^{(c*(a + b*x)))^n})], x], x] /; \text{FreeQ}\{F, a, b, c, e, f, g, n\}, x] \&\& \text{GtQ}[m, 0]$

Rule 3734

$\text{Int}[((c_)+(d_)*(x_))^{(m_)*((a_)+(b_)*\tan[(e_)+(f_)*(x_)])^{(n_)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(c + d*x)^m, (1/(a - I*b) - (2*I*b)/(a^2 + b^2 + (a - I*b)^2*E^{(2*I*(e + f*x))})^{-n}), x], x] /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{NeQ}[a^2 + b^2, 0] \&\& \text{ILtQ}[n, 0] \&\& \text{IGtQ}[m, 0]$

Rule 6589

$\text{Int}[\text{PolyLog}[n, (c_)*((a_)+(b_)*(x_))^{(p_)}]/((d_)+(e_)*(x_)), x_Symbol] \rightarrow \text{Simp}[\text{PolyLog}[n + 1, c*(a + b*x)^p]/(e*p), x] /; \text{FreeQ}\{a, b, c, d$

, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned}
 \int \frac{(c+dx)^2}{(a+b \tan(e+fx))^2} dx &= \int \left(\frac{(c+dx)^2}{(a-ib)^2} - \frac{4b^2(c+dx)^2}{(ia+b)^2 \left(ia \left(1 + \frac{ib}{a} \right) + ia \left(1 - \frac{ib}{a} \right) e^{2ie+2ifx} \right)^2} + \frac{4b}{(a-ib)^2 \left(ia \left(1 + \frac{ib}{a} \right) + ia \left(1 - \frac{ib}{a} \right) e^{2ie+2ifx} \right)} \right) dx \\
 &= \frac{(c+dx)^3}{3(a-ib)^2 d} + \frac{(4b) \int \frac{(c+dx)^2}{ia \left(1 + \frac{ib}{a} \right) + ia \left(1 - \frac{ib}{a} \right) e^{2ie+2ifx}} dx}{(a-ib)^2} - \frac{(4b^2) \int \frac{(c+dx)^2}{\left(ia \left(1 + \frac{ib}{a} \right) + ia \left(1 - \frac{ib}{a} \right) e^{2ie+2ifx} \right)^2} dx}{(ia+b)^2} \\
 &= \frac{(c+dx)^3}{3(a-ib)^2 d} + \frac{4b(c+dx)^3}{3(ia-b)(a-ib)^2 d} + \frac{(4b^2) \int \frac{(c+dx)^2}{ia \left(1 + \frac{ib}{a} \right) + ia \left(1 - \frac{ib}{a} \right) e^{2ie+2ifx}} dx}{(ia-b)(a-ib)^2} - \frac{(4b) \int \frac{(c+dx)^2}{ia \left(1 + \frac{ib}{a} \right) + ia \left(1 - \frac{ib}{a} \right) e^{2ie+2ifx}} dx}{(ia-b)(a-ib)^2} \\
 &= -\frac{2b^2(c+dx)^2}{(a-ib)^2(a+ib) \left(ia-b + (ia+b)e^{2ie+2ifx} \right) f} + \frac{(c+dx)^3}{3(a-ib)^2 d} + \frac{4b(c+dx)^3}{3(ia-b)(a-ib)^2 d} \\
 &= -\frac{2ib^2(c+dx)^2}{(a^2+b^2)^2 f} - \frac{2b^2(c+dx)^2}{(a-ib)^2(a+ib) \left(ia-b + (ia+b)e^{2ie+2ifx} \right) f} + \frac{(c+dx)^3}{3(a-ib)^2 d} + \frac{4b(c+dx)^3}{3(ia-b)(a-ib)^2 d} \\
 &= -\frac{2ib^2(c+dx)^2}{(a^2+b^2)^2 f} - \frac{2b^2(c+dx)^2}{(a-ib)^2(a+ib) \left(ia-b + (ia+b)e^{2ie+2ifx} \right) f} + \frac{(c+dx)^3}{3(a-ib)^2 d} + \frac{4b(c+dx)^3}{3(ia-b)(a-ib)^2 d} \\
 &= -\frac{2ib^2(c+dx)^2}{(a^2+b^2)^2 f} - \frac{2b^2(c+dx)^2}{(a-ib)^2(a+ib) \left(ia-b + (ia+b)e^{2ie+2ifx} \right) f} + \frac{(c+dx)^3}{3(a-ib)^2 d} + \frac{4b(c+dx)^3}{3(ia-b)(a-ib)^2 d} \\
 &= -\frac{2ib^2(c+dx)^2}{(a^2+b^2)^2 f} - \frac{2b^2(c+dx)^2}{(a-ib)^2(a+ib) \left(ia-b + (ia+b)e^{2ie+2ifx} \right) f} + \frac{(c+dx)^3}{3(a-ib)^2 d} + \frac{4b(c+dx)^3}{3(ia-b)(a-ib)^2 d}
 \end{aligned}$$

Mathematica [A] time = 9.60, size = 714, normalized size = 1.09

$$\frac{fx(a^2+b^2)(3c^2+3cdx+d^2x^2) \cos(2e+fx) + fx(a^2-b^2)(3c^2+3cdx+d^2x^2) \cos(fx) + 2b \sin(fx) (afx(3c^2+3cdx+d^2x^2) + 3b(c+dx)^2)}{(a \cos(e) + b \sin(e))(a \cos(e+fx) + b \sin(e+fx))} + \frac{2b \left(\frac{3d(a(1+e^{2ie}) - i)}{\dots} \right)}{\dots}$$

Antiderivative was successfully verified.

[In] Integrate[(c + d*x)^2/(a + b*Tan[e + f*x])^2,x]

[Out] ((2*b*((12*c*(b*d + a*c*f)*x)/(a - I*b) + (6*d*(b*d + 2*a*c*f)*x^2)/(a - I*b) + (4*a*d^2*f*x^3)/(a - I*b) + (6*d*((-I)*b*(-1 + E^((2*I)*e)) + a*(1 + E^((2*I)*e))))*(b*d + 2*a*c*f)*x*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(e + f*x)))])/(a + I*b)*(I*a + b)*f) + (6*a*d^2*((-I)*b*(-1 + E^((2*I)*e)) + a*(

```

1 + E^((2*I)*e)))*x^2*Log[1 + (a + I*b)/((a - I*b)*E^((2*I)*(e + f*x)))]/((
(a + I*b)*(I*a + b) - (6*c*((-I)*b*(-1 + E^((2*I)*e)) + a*(1 + E^((2*I)*e)
))*(b*d + a*c*f)*(2*f*x + I*Log[a + I*b + (a - I*b)*E^((2*I)*(e + f*x))]))/
((a^2 + b^2)*f) + (3*d*((-I)*b*(-1 + E^((2*I)*e)) + a*(1 + E^((2*I)*e)))*(b
*d + 2*a*c*f)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x)))]/((a^2
+ b^2)*f^2) + (3*a*d^2*((-I)*b*(-1 + E^((2*I)*e)) + a*(1 + E^((2*I)*e)))*
(2*f*x)*PolyLog[2, (-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x)))] - I*PolyLog[3,
(-a - I*b)/((a - I*b)*E^((2*I)*(e + f*x)))]/((a^2 + b^2)*f^2)))/(b - b*E
^((2*I)*e) - I*a*(1 + E^((2*I)*e)) + ((a^2 - b^2)*f*x*(3*c^2 + 3*c*d*x + d
^2*x^2)*Cos[f*x] + (a^2 + b^2)*f*x*(3*c^2 + 3*c*d*x + d^2*x^2)*Cos[2*e + f*
x] + 2*b*(3*b*(c + d*x)^2 + a*f*x*(3*c^2 + 3*c*d*x + d^2*x^2))*Sin[f*x])/((
a*Cos[e] + b*SIN[e])*(a*Cos[e + f*x] + b*SIN[e + f*x]))/(6*(a^2 + b^2)*f)

```

fricas [C] time = 0.60, size = 1578, normalized size = 2.41

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+b*tan(f*x+e))^2,x, algorithm="fricas")

```

[Out] 1/6*(2*(a^3 - a*b^2)*d^2*f^3*x^3 - 6*b^3*c^2*f^2 - 6*(b^3*d^2*f^2 - (a^3 -
a*b^2)*c*d*f^3)*x^2 - 6*(2*b^3*c*d*f^2 - (a^3 - a*b^2)*c^2*f^3)*x + (6*I*a^
2*b*d^2*f*x + 6*I*a^2*b*c*d*f + 3*I*a*b^2*d^2 + (6*I*a*b^2*d^2*f*x + 6*I*a*
b^2*c*d*f + 3*I*b^3*d^2)*tan(f*x + e))*dilog((2*(I*a*b - b^2)*tan(f*x + e)^
2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*tan(f*x + e))/((a^2 + b^
2)*tan(f*x + e)^2 + a^2 + b^2) + 1) + (-6*I*a^2*b*d^2*f*x - 6*I*a^2*b*c*d*f
- 3*I*a*b^2*d^2 + (-6*I*a*b^2*d^2*f*x - 6*I*a*b^2*c*d*f - 3*I*b^3*d^2)*tan
(f*x + e))*dilog((2*(-I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 + 2*I*a*b - (2*I*
a^2 + 4*a*b - 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^
2) + 1) + 6*(a^2*b*d^2*f^2*x^2 - a^2*b*d^2*e^2 + 2*a^2*b*c*d*e*f + a*b^2*d^
2*e + (2*a^2*b*c*d*f^2 + a*b^2*d^2*f)*x + (a*b^2*d^2*f^2*x^2 - a*b^2*d^2*e^
2 + 2*a*b^2*c*d*e*f + b^3*d^2*e + (2*a*b^2*c*d*f^2 + b^3*d^2*f)*x)*tan(f*x
+ e))*log(-(2*(I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 +
4*a*b + 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) +
6*(a^2*b*d^2*f^2*x^2 - a^2*b*d^2*e^2 + 2*a^2*b*c*d*e*f + a*b^2*d^2*e + (2*a
^2*b*c*d*f^2 + a*b^2*d^2*f)*x + (a*b^2*d^2*f^2*x^2 - a*b^2*d^2*e^2 + 2*a*b^
2*c*d*e*f + b^3*d^2*e + (2*a*b^2*c*d*f^2 + b^3*d^2*f)*x)*tan(f*x + e))*log(
-(2*(-I*a*b - b^2)*tan(f*x + e)^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*
I*b^2)*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + 6*(a^2*b*d
^2*e^2 + a^2*b*c^2*f^2 - a*b^2*d^2*e - (2*a^2*b*c*d*e - a*b^2*c*d)*f + (a*b
^2*d^2*e^2 + a*b^2*c^2*f^2 - b^3*d^2*e - (2*a*b^2*c*d*e - b^3*c*d)*f)*tan(f
*x + e))*log(((I*a*b + b^2)*tan(f*x + e)^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*
tan(f*x + e))/(tan(f*x + e)^2 + 1)) + 6*(a^2*b*d^2*e^2 + a^2*b*c^2*f^2 - a*
b^2*d^2*e - (2*a^2*b*c*d*e - a*b^2*c*d)*f + (a*b^2*d^2*e^2 + a*b^2*c^2*f^2
- b^3*d^2*e - (2*a*b^2*c*d*e - b^3*c*d)*f)*tan(f*x + e))*log(((I*a*b - b^2)
*tan(f*x + e)^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*tan(f*x + e))/(tan(f*x + e)
^2 + 1)) + 3*(a*b^2*d^2*tan(f*x + e) + a^2*b*d^2)*polylog(3, ((a^2 + 2*I*a*
b - b^2)*tan(f*x + e)^2 - a^2 - 2*I*a*b + b^2 + (2*I*a^2 - 4*a*b - 2*I*b^2)
*tan(f*x + e))/((a^2 + b^2)*tan(f*x + e)^2 + a^2 + b^2)) + 3*(a*b^2*d^2*tan
(f*x + e) + a^2*b*d^2)*polylog(3, ((a^2 - 2*I*a*b - b^2)*tan(f*x + e)^2 - a
^2 + 2*I*a*b + b^2 + (-2*I*a^2 - 4*a*b + 2*I*b^2)*tan(f*x + e))/((a^2 + b^2)
*tan(f*x + e)^2 + a^2 + b^2)) + 2*((a^2*b - b^3)*d^2*f^3*x^3 + 3*a*b^2*c^2
*f^2 + 3*(a*b^2*d^2*f^2 + (a^2*b - b^3)*c*d*f^3)*x^2 + 3*(2*a*b^2*c*d*f^2 +
(a^2*b - b^3)*c^2*f^3)*x)*tan(f*x + e))/((a^4*b + 2*a^2*b^3 + b^5)*f^3*tan
(f*x + e) + (a^5 + 2*a^3*b^2 + a*b^4)*f^3)

```

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(dx+c)^2}{(b \tan(fx+e)+a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+b*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate((d*x + c)^2/(b*tan(f*x + e) + a)^2, x)

maple [B] time = 1.23, size = 2160, normalized size = 3.30

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)^2/(a+b*tan(f*x+e))^2,x)

[Out]
$$\begin{aligned} & -1/3/(2*I*a*b-a^2+b^2)*d^2*x^3-1/(2*I*a*b-a^2+b^2)*c^2*x+1/(I*a+b)^2/f^3/(b \\ & -I*a)*b^2*d^2/(a+I*b)*polylog(2,(I*b-a)*exp(2*I*(f*x+e))/(a+I*b))+2/(I*a+b) \\ & ^2/f/(b-I*a)*b^2*d^2/(a+I*b)*x^2+2/(I*a+b)^2/f^3/(b-I*a)*b^2*d^2/(a+I*b)*e^ \\ & 2+4/3/(I*a+b)^2/(b-I*a)*b*a*d^2/(a+I*b)*x^3+I/(I*a+b)^2/f^3/(b-I*a)*b*a*d^2 \\ & / (a+I*b)*polylog(3,(I*b-a)*exp(2*I*(f*x+e))/(a+I*b))+2*I/(I*a+b)^2/f^3/(b-I \\ & *a)*b^2*d^2*e/(a+I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e))-I* \\ & b-a)*a+8*I/(I*a+b)^2/f^2/(b-I*a)*b*a*c*d*e/(a+I*b)*ln(exp(I*(f*x+e)))-2/(I* \\ & a+b)^2/f^2/(b-I*a)*b^3*c*d/(a+I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2* \\ & I*(f*x+e))-I*b-a)+4/(I*a+b)^2/(b-I*a)*b*a*c*d/(a+I*b)*x^2-8/3/(I*a+b)^2/f^3 \\ & / (b-I*a)*b*a*d^2*e^3/(a+I*b)+4/(I*a+b)^2/f^2/(b-I*a)*b^2*d^2/(a+I*b)*e*x+8/ \\ & (I*a+b)^2/f/(b-I*a)*b*a*c*d/(a+I*b)*e*x+4/(I*a+b)^2/f^2/(b-I*a)*b^2*a*c*d*e \\ & / (a+I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e))-I*b-a)-2*I/(I*a \\ & +b)^2/f^2/(b-I*a)*b^2*c*d/(a+I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I \\ & *(f*x+e))-I*b-a)*a+4*I/(I*a+b)^2/f^2/(b-I*a)*b*a*c*d/(a+I*b)*ln(1-(I*b-a)*e \\ & xp(2*I*(f*x+e))/(a+I*b))*e+4*I/(I*a+b)^2/f/(b-I*a)*b*a*c*d/(a+I*b)*ln(1-(I* \\ & b-a)*exp(2*I*(f*x+e))/(a+I*b))*x-2*I/(I*a+b)^2/f^3/(b-I*a)*b*a^2*d^2*e^2/(a \\ & +I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e))-I*b-a)+4*I/(I*a+b) \\ & ^2/f^2/(b-I*a)*b*a^2*c*d*e/(a+I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2* \\ & I*(f*x+e))-I*b-a)-1/(2*I*a*b-a^2+b^2)*c*d*x^2+2/(I*a+b)^2/f^2/(b-I*a)*b*a*c \\ & *d/(a+I*b)*polylog(2,(I*b-a)*exp(2*I*(f*x+e))/(a+I*b))+2/(I*a+b)^2/f^2/(b-I \\ & *a)*b*a*d^2/(a+I*b)*polylog(2,(I*b-a)*exp(2*I*(f*x+e))/(a+I*b))*x+4/(I*a+b) \\ & ^2/f^2/(b-I*a)*b*a*c*d/(a+I*b)*e^2+2/(I*a+b)^2/f^3/(b-I*a)*b^3*d^2*e/(a+I*b) \\ &)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e))-I*b-a)-2/(I*a+b)^2/f/(\\ & b-I*a)*b^2*a*c^2/(a+I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e)) \\ & -I*b-a)+4*I/(I*a+b)^2/f^3/(b-I*a)*b^2*d^2*e/(a+I*b)*ln(exp(I*(f*x+e)))-4*I/ \\ & (I*a+b)^2/f/(b-I*a)*b*a*c^2/(a+I*b)*ln(exp(I*(f*x+e)))-4/(I*a+b)^2/f^2/(b-I \\ & *a)*b*a*d^2*e^2/(a+I*b)*x-2*I*b^2*(d^2*x^2+2*c*d*x+c^2)/(b-I*a)/f/(I*a+b)^2 \\ & / (exp(2*I*(f*x+e))*b+I*a*exp(2*I*(f*x+e))-b+I*a)-2/(I*a+b)^2/f^3/(b-I*a)*b^ \\ & 2*a*d^2*e^2/(a+I*b)/(I*b-a)*ln(I*exp(2*I*(f*x+e))*b-a*exp(2*I*(f*x+e))-I*b- \\ & a)+2*I/(I*a+b)^2/f/(b-I*a)*b*a*d^2/(a+I*b)*ln(1-(I*b-a)*exp(2*I*(f*x+e)))/(a \\ & +I*b))*x^2-2*I/(I*a+b)^2/f/(b-I*a)*b*a^2*c^2/(a+I*b)/(I*b-a)*ln(I*exp(2*I*(\\ & f*x+e))*b-a*exp(2*I*(f*x+e))-I*b-a)-4*I/(I*a+b)^2/f^3/(b-I*a)*b*a*d^2*e^2/(\\ & a+I*b)*ln(exp(I*(f*x+e)))-2*I/(I*a+b)^2/f^3/(b-I*a)*b*a*d^2/(a+I*b)*ln(1-(I \\ & *b-a)*exp(2*I*(f*x+e))/(a+I*b))*e^2-4*I/(I*a+b)^2/f^2/(b-I*a)*b^2*c*d/(a+I* \\ & b)*ln(exp(I*(f*x+e)))+2*I/(I*a+b)^2/f^2/(b-I*a)*b^2*d^2/(a+I*b)*ln(1-(I*b-a) \\ &)*exp(2*I*(f*x+e))/(a+I*b))*x+2*I/(I*a+b)^2/f^3/(b-I*a)*b^2*d^2/(a+I*b)*ln(\\ & 1-(I*b-a)*exp(2*I*(f*x+e))/(a+I*b))*e \end{aligned}$$

maxima [B] time = 4.43, size = 2558, normalized size = 3.91

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2/(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out]
$$-(2*c*d*e*(2*a*b*\log(b*\tan(f*x + e) + a)/((a^4 + 2*a^2*b^2 + b^4)*f) - a*b*\log(\tan(f*x + e)^2 + 1)/((a^4 + 2*a^2*b^2 + b^4)*f) - b/((a^2*b + b^3)*f*ta$$

```

n(f*x + e) + (a^3 + a*b^2)*f) + (a^2 - b^2)*(f*x + e)/((a^4 + 2*a^2*b^2 + b
^4)*f)) - (2*a*b*log(b*tan(f*x + e) + a)/(a^4 + 2*a^2*b^2 + b^4) - a*b*log(
tan(f*x + e)^2 + 1)/(a^4 + 2*a^2*b^2 + b^4) + (a^2 - b^2)*(f*x + e)/(a^4 +
2*a^2*b^2 + b^4) - b/(a^3 + a*b^2 + (a^2*b + b^3)*tan(f*x + e))) *c^2 - ((a^
3 - I*a^2*b + a*b^2 - I*b^3)*(f*x + e)^3*d^2 + (3*a^3 - 3*I*a^2*b + 3*a*b^2
- 3*I*b^3)*(f*x + e)*d^2*e^2 + (6*I*a*b^2 - 6*b^3)*d^2*e^2 - ((3*a^3 - 3*I
*a^2*b + 3*a*b^2 - 3*I*b^3)*d^2*e - (3*a^3 - 3*I*a^2*b + 3*a*b^2 - 3*I*b^3)
*c*d*f)*(f*x + e)^2 + ((6*I*a^2*b - 6*a*b^2)*d^2*e^2 + (-6*I*a*b^2 + 6*b^3)
*d^2*e + (6*I*a*b^2 - 6*b^3)*c*d*f + ((6*I*a^2*b + 6*a*b^2)*d^2*e^2 + (-6*I
*a*b^2 - 6*b^3)*d^2*e + (6*I*a*b^2 + 6*b^3)*c*d*f)*cos(2*f*x + 2*e) - 6*((a
^2*b - I*a*b^2)*d^2*e^2 - (a*b^2 - I*b^3)*d^2*e + (a*b^2 - I*b^3)*c*d*f)*si
n(2*f*x + 2*e))*arctan2(-b*cos(2*f*x + 2*e) + a*sin(2*f*x + 2*e) + b, a*cos
(2*f*x + 2*e) + b*sin(2*f*x + 2*e) + a) + ((-6*I*a^2*b + 6*a*b^2)*(f*x + e)
^2*d^2 + ((12*I*a^2*b - 12*a*b^2)*d^2*e + (-12*I*a^2*b + 12*a*b^2)*c*d*f +
(-6*I*a*b^2 + 6*b^3)*d^2)*(f*x + e) + ((-6*I*a^2*b - 6*a*b^2)*(f*x + e)^2*d
^2 + ((12*I*a^2*b + 12*a*b^2)*d^2*e + (-12*I*a^2*b - 12*a*b^2)*c*d*f + (-6*
I*a*b^2 - 6*b^3)*d^2)*(f*x + e))*cos(2*f*x + 2*e) + 6*((a^2*b - I*a*b^2)*(f
*x + e)^2*d^2 - (2*(a^2*b - I*a*b^2)*d^2*e - 2*(a^2*b - I*a*b^2)*c*d*f - (a
*b^2 - I*b^3)*d^2)*(f*x + e))*sin(2*f*x + 2*e))*arctan2((2*a*b*cos(2*f*x +
2*e) - (a^2 - b^2)*sin(2*f*x + 2*e))/(a^2 + b^2), (2*a*b*sin(2*f*x + 2*e) +
a^2 + b^2 + (a^2 - b^2)*cos(2*f*x + 2*e))/(a^2 + b^2)) + ((a^3 - 3*I*a^2*b
- 3*a*b^2 + I*b^3)*(f*x + e)^3*d^2 - ((3*a^3 - 9*I*a^2*b - 9*a*b^2 + 3*I*b
^3)*d^2*e - (3*a^3 - 9*I*a^2*b - 9*a*b^2 + 3*I*b^3)*c*d*f - (-6*I*a*b^2 - 6
*b^3)*d^2)*(f*x + e)^2 + ((3*a^3 - 9*I*a^2*b - 9*a*b^2 + 3*I*b^3)*d^2*e^2 +
(12*I*a*b^2 + 12*b^3)*d^2*e + (-12*I*a*b^2 - 12*b^3)*c*d*f)*(f*x + e))*cos
(2*f*x + 2*e) + ((-6*I*a^2*b + 6*a*b^2)*(f*x + e)*d^2 + (6*I*a^2*b - 6*a*b^
2)*d^2*e + (-6*I*a^2*b + 6*a*b^2)*c*d*f + (-3*I*a*b^2 + 3*b^3)*d^2 + ((-6*I
*a^2*b - 6*a*b^2)*(f*x + e)*d^2 + (6*I*a^2*b + 6*a*b^2)*d^2*e + (-6*I*a^2*b
- 6*a*b^2)*c*d*f + (-3*I*a*b^2 - 3*b^3)*d^2)*cos(2*f*x + 2*e) + 3*(2*(a^2*
b - I*a*b^2)*(f*x + e)*d^2 - 2*(a^2*b - I*a*b^2)*d^2*e + 2*(a^2*b - I*a*b^2
)*c*d*f + (a*b^2 - I*b^3)*d^2)*sin(2*f*x + 2*e))*dilog((I*a + b)*e^(2*I*f*x
+ 2*I*e)/(-I*a + b)) + (3*(a^2*b + I*a*b^2)*d^2*e^2 - 3*(a*b^2 + I*b^3)*d^
2*e + 3*(a*b^2 + I*b^3)*c*d*f + 3*((a^2*b - I*a*b^2)*d^2*e^2 - (a*b^2 - I*b
^3)*d^2*e + (a*b^2 - I*b^3)*c*d*f)*cos(2*f*x + 2*e) + ((3*I*a^2*b + 3*a*b^2
)*d^2*e^2 + (-3*I*a*b^2 - 3*b^3)*d^2*e + (3*I*a*b^2 + 3*b^3)*c*d*f)*sin(2*f
*x + 2*e))*log((a^2 + b^2)*cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) + (a
^2 + b^2)*sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e))
+ (3*(a^2*b + I*a*b^2)*(f*x + e)^2*d^2 - 3*(2*(a^2*b + I*a*b^2)*d^2*e - 2*(
a^2*b + I*a*b^2)*c*d*f - (a*b^2 + I*b^3)*d^2)*(f*x + e) + 3*((a^2*b - I*a*b
^2)*(f*x + e)^2*d^2 - (2*(a^2*b - I*a*b^2)*d^2*e - 2*(a^2*b - I*a*b^2)*c*d*
f - (a*b^2 - I*b^3)*d^2)*(f*x + e))*cos(2*f*x + 2*e) + ((3*I*a^2*b + 3*a*b^
2)*(f*x + e)^2*d^2 + ((-6*I*a^2*b - 6*a*b^2)*d^2*e + (6*I*a^2*b + 6*a*b^2)*
c*d*f + (3*I*a*b^2 + 3*b^3)*d^2)*(f*x + e))*sin(2*f*x + 2*e))*log(((a^2 + b
^2)*cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) + (a^2 + b^2)*sin(2*f*x + 2
*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e))/(a^2 + b^2)) + (3*(a^2*
b - I*a*b^2)*d^2*cos(2*f*x + 2*e) + (3*I*a^2*b + 3*a*b^2)*d^2*sin(2*f*x + 2
*e) + 3*(a^2*b + I*a*b^2)*d^2)*polylog(3, (I*a + b)*e^(2*I*f*x + 2*I*e)/(-I
*a + b)) + ((I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*(f*x + e)^3*d^2 + ((-3*I*a^
3 - 9*a^2*b + 9*I*a*b^2 + 3*b^3)*d^2*e + (3*I*a^3 + 9*a^2*b - 9*I*a*b^2 - 3
*b^3)*c*d*f + 6*(a*b^2 - I*b^3)*d^2)*(f*x + e)^2 + ((3*I*a^3 + 9*a^2*b - 9*
I*a*b^2 - 3*b^3)*d^2*e^2 - 12*(a*b^2 - I*b^3)*d^2*e + 12*(a*b^2 - I*b^3)*c*
d*f)*(f*x + e))*sin(2*f*x + 2*e))/((3*a^5 - 3*I*a^4*b + 6*a^3*b^2 - 6*I*a^2
*b^3 + 3*a*b^4 - 3*I*b^5)*f^2*cos(2*f*x + 2*e) + (3*I*a^5 + 3*a^4*b + 6*I*a
^3*b^2 + 6*a^2*b^3 + 3*I*a*b^4 + 3*b^5)*f^2*sin(2*f*x + 2*e) + (3*a^5 + 3*I
*a^4*b + 6*a^3*b^2 + 6*I*a^2*b^3 + 3*a*b^4 + 3*I*b^5)*f^2))/f

```

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(c + dx)^2}{(a + b \tan(e + fx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x)^2/(a + b*tan(e + f*x))^2,x)
```

```
[Out] int((c + d*x)^2/(a + b*tan(e + f*x))^2, x)
```

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(c + dx)^2}{(a + b \tan(e + fx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2/(a+b*tan(f*x+e))**2,x)
```

```
[Out] Integral((c + d*x)**2/(a + b*tan(e + f*x))**2, x)
```

3.61 $\int \frac{c+dx}{(a+b \tan(e+fx))^2} dx$

Optimal. Leaf size=214

$$\frac{b(2acf + 2adfx + bd) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f^2(a^2+b^2)^2} - \frac{b(c+dx)}{f(a^2+b^2)(a+b \tan(e+fx))} + \frac{(2acf + 2adfx + bd)^2}{4adf^2(a+ib)(a^2+b^2)} - \frac{(c+dx)}{2d(a^2+b^2)}$$

[Out] $-1/2*(d*x+c)^2/(a^2+b^2)/d+1/4*(2*a*d*f*x+2*a*c*f+b*d)^2/a/(a+I*b)/(a^2+b^2)/d/f^2+b*(2*a*d*f*x+2*a*c*f+b*d)*\ln(1+(a^2+b^2)*\exp(2*I*(f*x+e))/(a+I*b)^2)/(a^2+b^2)^2/f^2-I*a*b*d*\text{polylog}(2,-(a^2+b^2)*\exp(2*I*(f*x+e))/(a+I*b)^2)/(a^2+b^2)^2/f^2-b*(d*x+c)/(a^2+b^2)/f/(a+b*\tan(f*x+e))$

Rubi [A] time = 0.28, antiderivative size = 214, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.278$, Rules used = {3733, 3732, 2190, 2279, 2391}

$$\frac{b(2acf + 2adfx + bd) \log\left(1 + \frac{(a^2+b^2)e^{2i(e+fx)}}{(a+ib)^2}\right)}{f^2(a^2+b^2)^2} - \frac{b(c+dx)}{f(a^2+b^2)(a+b \tan(e+fx))} + \frac{(2acf + 2adfx + bd)^2}{4adf^2(a+ib)(a^2+b^2)} - \frac{(c+dx)}{2d(a^2+b^2)}$$

Antiderivative was successfully verified.

[In] Int[(c + d*x)/(a + b*Tan[e + f*x])^2, x]

[Out] $-(c + d*x)^2/(2*(a^2 + b^2)*d) + (b*d + 2*a*c*f + 2*a*d*f*x)^2/(4*a*(a + I*b)*(a^2 + b^2)*d*f^2) + (b*(b*d + 2*a*c*f + 2*a*d*f*x)*\text{Log}[1 + ((a^2 + b^2)*E^{(2*I)*(e + f*x)})/(a + I*b)^2])/((a^2 + b^2)^2*f^2) - (I*a*b*d*\text{PolyLog}[2, -((a^2 + b^2)*E^{(2*I)*(e + f*x)})/(a + I*b)^2])/((a^2 + b^2)^2*f^2) - (b*(c + d*x))/((a^2 + b^2)*f*(a + b*\tan[e + f*x]))$

Rule 2190

Int[(((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^(g_)*((e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x))))^n]/a)/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m-1)*Log[1 + (b*(F^(g*(e + f*x))))^n]/a], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_)*((F_)^(e_)*((c_) + (d_)*(x_)))^(n_)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 3732

Int[(((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*tan[(e_) + (f_)*(x_)]), x_Symbol] := Simp[(c + d*x)^(m+1)/(d*(m+1)*(a + I*b)), x] + Dist[2*I*b, Int[((c + d*x)^m*E^Simp[2*I*(e + f*x), x])/((a + I*b)^2 + (a^2 + b^2)*E^Simp[2*I*(e + f*x), x]), x] /; FreeQ[{a, b, c, d, e, f}, x] && NeQ[a^2 + b^2, 0] && IGtQ[m, 0]

Rule 3733

```
Int[((c_.) + (d_.)*(x_))/((a_.) + (b_.)*tan[(e_.) + (f_.)*(x_)])^2, x_Symbol]
:= -Simp[(c + d*x)^2/(2*d*(a^2 + b^2)), x] + (Dist[1/(f*(a^2 + b^2)), Int
[(b*d + 2*a*c*f + 2*a*d*f*x)/(a + b*Tan[e + f*x]), x], x] - Simp[(b*(c + d*
x))/(f*(a^2 + b^2)*(a + b*Tan[e + f*x])), x]) /; FreeQ[{a, b, c, d, e, f},
x] && NeQ[a^2 + b^2, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{c + dx}{(a + b \tan(e + fx))^2} dx &= -\frac{(c + dx)^2}{2(a^2 + b^2)d} - \frac{b(c + dx)}{(a^2 + b^2)f(a + b \tan(e + fx))} + \frac{\int \frac{bd + 2acf + 2adf x}{a + b \tan(e + fx)} dx}{(a^2 + b^2)f} \\ &= -\frac{(c + dx)^2}{2(a^2 + b^2)d} + \frac{(bd + 2acf + 2adf x)^2}{4a(a + ib)(a^2 + b^2)df^2} - \frac{b(c + dx)}{(a^2 + b^2)f(a + b \tan(e + fx))} + \frac{(2ib)}{\dots} \\ &= -\frac{(c + dx)^2}{2(a^2 + b^2)d} + \frac{(bd + 2acf + 2adf x)^2}{4a(a + ib)(a^2 + b^2)df^2} + \frac{b(bd + 2acf + 2adf x) \log\left(1 + \frac{(a^2 + b^2)}{a}\right)}{(a^2 + b^2)^2 f^2} \\ &= -\frac{(c + dx)^2}{2(a^2 + b^2)d} + \frac{(bd + 2acf + 2adf x)^2}{4a(a + ib)(a^2 + b^2)df^2} + \frac{b(bd + 2acf + 2adf x) \log\left(1 + \frac{(a^2 + b^2)}{a}\right)}{(a^2 + b^2)^2 f^2} \\ &= -\frac{(c + dx)^2}{2(a^2 + b^2)d} + \frac{(bd + 2acf + 2adf x)^2}{4a(a + ib)(a^2 + b^2)df^2} + \frac{b(bd + 2acf + 2adf x) \log\left(1 + \frac{(a^2 + b^2)}{a}\right)}{(a^2 + b^2)^2 f^2} \end{aligned}$$

Mathematica [B] time = 7.07, size = 745, normalized size = 3.48

$$\frac{2bc \sec^2(e + fx)(a \cos(e + fx) + b \sin(e + fx))^2(a \log(a \cos(e + fx) + b \sin(e + fx)) - b(e + fx))}{f(a - ib)(a + ib)(a^2 + b^2)(a + b \tan(e + fx))^2} d \sec^2(e + fx)$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[(c + d*x)/(a + b*Tan[e + f*x])^2,x]
```

```
[Out] ((e + f*x)*(-2*d*e + 2*c*f + d*(e + f*x))*Sec[e + f*x]^2*(a*Cos[e + f*x] +
b*Sin[e + f*x])^2)/(2*(a - I*b)*(a + I*b)*f^2*(a + b*Tan[e + f*x])^2) + (b^
2*d*(-(b*(e + f*x)) + a*Log[a*Cos[e + f*x] + b*Sin[e + f*x]])*Sec[e + f*x]^
2*(a*Cos[e + f*x] + b*Sin[e + f*x])^2)/(a*(a - I*b)*(a + I*b)*(a^2 + b^2)*f
^2*(a + b*Tan[e + f*x])^2) - (2*b*d*e*(-(b*(e + f*x)) + a*Log[a*Cos[e + f*x]
+ b*Sin[e + f*x]])*Sec[e + f*x]^2*(a*Cos[e + f*x] + b*Sin[e + f*x])^2)/((
a - I*b)*(a + I*b)*(a^2 + b^2)*f^2*(a + b*Tan[e + f*x])^2) + (2*b*c*(-(b*(e
+ f*x)) + a*Log[a*Cos[e + f*x] + b*Sin[e + f*x]])*Sec[e + f*x]^2*(a*Cos[e
+ f*x] + b*Sin[e + f*x])^2)/((a - I*b)*(a + I*b)*(a^2 + b^2)*f*(a + b*Tan[e
+ f*x])^2) - (d*(E^(I*ArcTan[a/b])*(e + f*x)^2 + (a*(I*(e + f*x)*(-Pi + 2*
ArcTan[a/b]) - Pi*Log[1 + E^((-2*I)*(e + f*x))]) - 2*(e + f*x + ArcTan[a/b])
*Log[1 - E^((2*I)*(e + f*x + ArcTan[a/b]))]) + Pi*Log[Cos[e + f*x]] + 2*ArcT
an[a/b]*Log[Sin[e + f*x + ArcTan[a/b]]]) + I*PolyLog[2, E^((2*I)*(e + f*x +
ArcTan[a/b]))]))/(Sqrt[1 + a^2/b^2]*b))*Sec[e + f*x]^2*(a*Cos[e + f*x] + b*
```

$\text{Sin}[e + f*x])^2)/((a - I*b)*(a + I*b)*\text{Sqrt}[(a^2 + b^2)/b^2]*f^2*(a + b*\text{Tan}[e + f*x])^2) + (\text{Sec}[e + f*x]^2*(a*\text{Cos}[e + f*x] + b*\text{Sin}[e + f*x])*(-(b^2*d*e*\text{Sin}[e + f*x]) + b^2*c*f*\text{Sin}[e + f*x] + b^2*d*(e + f*x)*\text{Sin}[e + f*x]))/(a*(a - I*b)*(a + I*b)*f^2*(a + b*\text{Tan}[e + f*x])^2)$

fricas [B] time = 0.59, size = 849, normalized size = 3.97

$$(a^3 - ab^2)df^2x^2 - 2b^3cf - 2(b^3df - (a^3 - ab^2)cf^2)x + (iab^2d \tan (fx + e) + ia^2bd)\text{Li}_2\left(\frac{2(iab-b^2)\tan (fx+e)^2-2a^2}{(a^2+b^2)\tan (fx+e)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+b*tan(f*x+e))^2,x, algorithm="fricas")

[Out] $\frac{1}{2}*((a^3 - a*b^2)*d*f^2*x^2 - 2*b^3*c*f - 2*(b^3*d*f - (a^3 - a*b^2)*c*f^2)*x + (I*a*b^2*d*\text{tan}(f*x + e) + I*a^2*b*d)*\text{dilog}((2*(I*a*b - b^2)*\text{tan}(f*x + e)^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*\text{tan}(f*x + e))/((a^2 + b^2)*\text{tan}(f*x + e)^2 + a^2 + b^2) + 1) + (-I*a*b^2*d*\text{tan}(f*x + e) - I*a^2*b*d)*\text{dilog}((2*(-I*a*b - b^2)*\text{tan}(f*x + e)^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*\text{tan}(f*x + e))/((a^2 + b^2)*\text{tan}(f*x + e)^2 + a^2 + b^2) + 1) + 2*(a^2*b*d*f*x + a^2*b*d*e + (a*b^2*d*f*x + a*b^2*d*e)*\text{tan}(f*x + e))*\text{log}(-2*(I*a*b - b^2)*\text{tan}(f*x + e)^2 - 2*a^2 - 2*I*a*b - (-2*I*a^2 + 4*a*b + 2*I*b^2)*\text{tan}(f*x + e))/((a^2 + b^2)*\text{tan}(f*x + e)^2 + a^2 + b^2) + 2*(a^2*b*d*f*x + a^2*b*d*e + (a*b^2*d*f*x + a*b^2*d*e)*\text{tan}(f*x + e))*\text{log}(-2*(-I*a*b - b^2)*\text{tan}(f*x + e)^2 - 2*a^2 + 2*I*a*b - (2*I*a^2 + 4*a*b - 2*I*b^2)*\text{tan}(f*x + e))/((a^2 + b^2)*\text{tan}(f*x + e)^2 + a^2 + b^2) - (2*a^2*b*d*e - 2*a^2*b*c*f - a*b^2*d + (2*a*b^2*d*e - 2*a*b^2*c*f - b^3*d)*\text{tan}(f*x + e))*\text{log}(((I*a*b + b^2)*\text{tan}(f*x + e)^2 - a^2 + I*a*b + (I*a^2 + I*b^2)*\text{tan}(f*x + e))/(\text{tan}(f*x + e)^2 + 1)) - (2*a^2*b*d*e - 2*a^2*b*c*f - a*b^2*d + (2*a*b^2*d*e - 2*a*b^2*c*f - b^3*d)*\text{tan}(f*x + e))*\text{log}(((I*a*b - b^2)*\text{tan}(f*x + e)^2 + a^2 + I*a*b + (I*a^2 + I*b^2)*\text{tan}(f*x + e))/(\text{tan}(f*x + e)^2 + 1)) + ((a^2*b - b^3)*d*f^2*x^2 + 2*a*b^2*c*f + 2*(a*b^2*d*f + (a^2*b - b^3)*c*f^2)*x)*\text{tan}(f*x + e))/((a^4*b + 2*a^2*b^3 + b^5)*f^2*\text{tan}(f*x + e) + (a^5 + 2*a^3*b^2 + a*b^4)*f^2)$

giac [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{dx + c}{(b \tan (fx + e) + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+b*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate((d*x + c)/(b*tan(f*x + e) + a)^2, x)

maple [B] time = 1.15, size = 999, normalized size = 4.67

$$\frac{dx^2}{2(2iab - a^2 + b^2)} - \frac{cx}{2iab - a^2 + b^2} + \frac{2ibad \ln\left(1 - \frac{(ib-a)e^{2i(fx+e)}}{ib+a}\right)e}{(ia + b)^2 f^2 (-ia + b)(ib + a)} - \frac{2ib^2(dx + c)}{(-ia + b)f(ia + b)^2 \left(e^{2i(fx+e)}b + ia e^{2i(fx+e)}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x+c)/(a+b*tan(f*x+e))^2,x)

[Out] $-1/2/(2*I*a*b - a^2 + b^2)*d*x^2 - 1/(2*I*a*b - a^2 + b^2)*c*x + 2*I/(I*a + b)^2/f^2/(b - I*a)*b*a*d/(a + I*b)*\text{ln}(1 - (I*b - a)*\text{exp}(2*I*(f*x + e))/(a + I*b))*e - 2*I*b^2*(d*x + c)/(b - I*a)/f/(I*a + b)^2/(\text{exp}(2*I*(f*x + e))*b + I*a*\text{exp}(2*I*(f*x + e))) - b + I*a - 1/(I*a + b)$

$$b^2/f^2/(b-I*a)*b^3*d/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+2*I/(I*a+b)^2/f^2/(b-I*a)*b*a^2*d*e/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)+2*I/(I*a+b)^2/f/(b-I*a)*b*a*d/(a+I*b)*\ln(1-(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))*x-2/(I*a+b)^2/f/(b-I*a)*b^2*a*c/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)-2*I/(I*a+b)^2/f^2/(b-I*a)*b^2*d/(a+I*b)*\ln(\exp(I*(f*x+e)))-4*I/(I*a+b)^2/f/(b-I*a)*b*a*c/(a+I*b)*\ln(\exp(I*(f*x+e)))+2/(I*a+b)^2/f^2/(b-I*a)*b^2*a*d*e/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)-2*I/(I*a+b)^2/f/(b-I*a)*b*a^2*c/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)-I/(I*a+b)^2/f^2/(b-I*a)*b^2*d/(a+I*b)/(I*b-a)*\ln(I*\exp(2*I*(f*x+e))*b-a*\exp(2*I*(f*x+e))-I*b-a)*a+4*I/(I*a+b)^2/f^2/(b-I*a)*b*a*d*e/(a+I*b)*\ln(\exp(I*(f*x+e)))+2/(I*a+b)^2/(b-I*a)*b*a*d/(a+I*b)*x^2+4/(I*a+b)^2/f/(b-I*a)*b*a*d/(a+I*b)*e*x+2/(I*a+b)^2/f^2/(b-I*a)*b*a*d/(a+I*b)*e^2+1/(I*a+b)^2/f^2/(b-I*a)*b*a*d/(a+I*b)*\operatorname{polylog}(2,(I*b-a)*\exp(2*I*(f*x+e))/(a+I*b))$$

maxima [B] time = 1.49, size = 1164, normalized size = 5.44

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out] ((a^3 - I*a^2*b + a*b^2 - I*b^3)*d*f^2*x^2 + (2*a^3 - 2*I*a^2*b + 2*a*b^2 - 2*I*b^3)*c*f^2*x + (4*I*a*b^2 - 4*b^3)*c*f + ((4*I*a^2*b - 4*a*b^2)*c*f + (2*I*a*b^2 - 2*b^3)*d + ((4*I*a^2*b + 4*a*b^2)*c*f + (2*I*a*b^2 + 2*b^3)*d)*cos(2*f*x + 2*e) - 2*(2*(a^2*b - I*a*b^2)*c*f + (a*b^2 - I*b^3)*d)*sin(2*f*x + 2*e))*arctan2(-b*cos(2*f*x + 2*e) + a*sin(2*f*x + 2*e) + b, a*cos(2*f*x + 2*e) + b*sin(2*f*x + 2*e) + a) + ((-4*I*a^2*b - 4*a*b^2)*d*f*x*cos(2*f*x + 2*e) + 4*(a^2*b - I*a*b^2)*d*f*x*sin(2*f*x + 2*e) + (-4*I*a^2*b + 4*a*b^2)*d*f*x)*arctan2((2*a*b*cos(2*f*x + 2*e) - (a^2 - b^2)*sin(2*f*x + 2*e))/(a^2 + b^2), (2*a*b*sin(2*f*x + 2*e) + a^2 + b^2 + (a^2 - b^2)*cos(2*f*x + 2*e))/(a^2 + b^2)) + ((a^3 - 3*I*a^2*b - 3*a*b^2 + I*b^3)*d*f^2*x^2 + ((2*a^3 - 6*I*a^2*b - 6*a*b^2 + 2*I*b^3)*c*f^2 + (-4*I*a*b^2 - 4*b^3)*d*f)*x)*cos(2*f*x + 2*e) + ((-2*I*a^2*b - 2*a*b^2)*d*cos(2*f*x + 2*e) + 2*(a^2*b - I*a*b^2)*d*sin(2*f*x + 2*e) + (-2*I*a^2*b + 2*a*b^2)*d)*dilog((I*a + b)*e^(2*I*f*x + 2*I*e)/(-I*a + b)) + (2*(a^2*b + I*a*b^2)*c*f + (a*b^2 + I*b^3)*d + (2*(a^2*b - I*a*b^2)*c*f + (a*b^2 - I*b^3)*d)*cos(2*f*x + 2*e) + ((2*I*a^2*b + 2*a*b^2)*c*f + (I*a*b^2 + b^3)*d)*sin(2*f*x + 2*e))*log((a^2 + b^2)*cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) + (a^2 + b^2)*sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e)) + (2*(a^2*b - I*a*b^2)*d*f*x*cos(2*f*x + 2*e) + (2*I*a^2*b + 2*a*b^2)*d*f*x*sin(2*f*x + 2*e) + 2*(a^2*b + I*a*b^2)*d*f*x)*log(((a^2 + b^2)*cos(2*f*x + 2*e)^2 + 4*a*b*sin(2*f*x + 2*e) + (a^2 + b^2)*sin(2*f*x + 2*e)^2 + a^2 + b^2 + 2*(a^2 - b^2)*cos(2*f*x + 2*e))/(a^2 + b^2)) + ((I*a^3 + 3*a^2*b - 3*I*a*b^2 - b^3)*d*f^2*x^2 + ((2*I*a^3 + 6*a^2*b - 6*I*a*b^2 - 2*b^3)*c*f^2 + 4*(a*b^2 - I*b^3)*d*f)*x)*sin(2*f*x + 2*e))/((2*a^5 - 2*I*a^4*b + 4*a^3*b^2 - 4*I*a^2*b^3 + 2*a*b^4 - 2*I*b^5)*f^2*cos(2*f*x + 2*e) + (2*I*a^5 + 2*a^4*b + 4*I*a^3*b^2 + 4*a^2*b^3 + 2*I*a*b^4 + 2*b^5)*f^2*sin(2*f*x + 2*e) + (2*a^5 + 2*I*a^4*b + 4*a^3*b^2 + 4*I*a^2*b^3 + 2*a*b^4 + 2*I*b^5)*f^2)

mupad [F] time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{c + dx}{(a + b \tan(e + fx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((c + d*x)/(a + b*tan(e + f*x))^2,x)

[Out] int((c + d*x)/(a + b*tan(e + f*x))^2, x)

sympy [F] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{c + dx}{(a + b \tan(e + fx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)/(a+b*tan(f*x+e))**2,x)

[Out] Integral((c + d*x)/(a + b*tan(e + f*x))**2, x)

$$3.62 \quad \int \frac{1}{(c+dx)(a+b \tan(e+fx))^2} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{1}{(c+dx)(a+b \tan(e+fx))^2}, x\right)$$

[Out] Unintegrable(1/(d*x+c)/(a+b*tan(f*x+e))^2, x)

Rubi [A] time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{(c+dx)(a+b \tan(e+fx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/((c + d*x)*(a + b*Tan[e + f*x])^2), x]

[Out] Defer[Int][1/((c + d*x)*(a + b*Tan[e + f*x])^2), x]

Rubi steps

$$\int \frac{1}{(c+dx)(a+b \tan(e+fx))^2} dx = \int \frac{1}{(c+dx)(a+b \tan(e+fx))^2} dx$$

Mathematica [A] time = 19.52, size = 0, normalized size = 0.00

$$\int \frac{1}{(c+dx)(a+b \tan(e+fx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/((c + d*x)*(a + b*Tan[e + f*x])^2), x]

[Out] Integrate[1/((c + d*x)*(a + b*Tan[e + f*x])^2), x]

fricas [A] time = 0.45, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{1}{a^2dx + a^2c + (b^2dx + b^2c) \tan(fx + e)^2 + 2(abdx + abc) \tan(fx + e)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e))^2,x, algorithm="fricas")

[Out] integral(1/(a^2*d*x + a^2*c + (b^2*d*x + b^2*c)*tan(f*x + e)^2 + 2*(a*b*d*x + a*b*c)*tan(f*x + e)), x)

giac [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(dx+c)(b \tan(fx+e)+a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e))^2,x, algorithm="giac")

[Out] integrate(1/((d*x + c)*(b*tan(f*x + e) + a)^2), x)

maple [A] time = 10.73, size = 0, normalized size = 0.00

$$\int \frac{1}{(dx + c)(a + b \tan(fx + e))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)/(a+b*tan(f*x+e))^2,x)

[Out] int(1/(d*x+c)/(a+b*tan(f*x+e))^2,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out] Timed out

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{1}{(a + b \tan(e + fx))^2 (c + dx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*tan(e + f*x))^2*(c + d*x)),x)

[Out] int(1/((a + b*tan(e + f*x))^2*(c + d*x)), x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a + b \tan(e + fx))^2 (c + dx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)/(a+b*tan(f*x+e))**2,x)

[Out] Integral(1/((a + b*tan(e + f*x))**2*(c + d*x)), x)

$$3.63 \quad \int \frac{1}{(c+dx)^2(a+b \tan(e+fx))^2} dx$$

Optimal. Leaf size=23

$$\text{Int}\left(\frac{1}{(c+dx)^2(a+b \tan(e+fx))^2}, x\right)$$

[Out] Unintegrable(1/(d*x+c)^2/(a+b*tan(f*x+e))^2, x)

Rubi [A] time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/((c + d*x)^2*(a + b*Tan[e + f*x])^2), x]

[Out] Defer[Int][1/((c + d*x)^2*(a + b*Tan[e + f*x])^2), x]

Rubi steps

$$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))^2} dx = \int \frac{1}{(c+dx)^2(a+b \tan(e+fx))^2} dx$$

Mathematica [A] time = 19.41, size = 0, normalized size = 0.00

$$\int \frac{1}{(c+dx)^2(a+b \tan(e+fx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/((c + d*x)^2*(a + b*Tan[e + f*x])^2), x]

[Out] Integrate[1/((c + d*x)^2*(a + b*Tan[e + f*x])^2), x]

fricas [A] time = 0.46, size = 0, normalized size = 0.00

$$\text{integral}\left(\frac{1}{a^2d^2x^2 + 2a^2cdx + a^2c^2 + (b^2d^2x^2 + 2b^2cdx + b^2c^2)\tan(fx + e)^2 + 2(abd^2x^2 + 2abcdx + abc^2)\tan(fx + e)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+b*tan(f*x+e))^2, x, algorithm="fricas")

[Out] integral(1/(a^2*d^2*x^2 + 2*a^2*c*d*x + a^2*c^2 + (b^2*d^2*x^2 + 2*b^2*c*d*x + b^2*c^2)*tan(f*x + e)^2 + 2*(a*b*d^2*x^2 + 2*a*b*c*d*x + a*b*c^2)*tan(f*x + e)), x)

giac [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+b*tan(f*x+e))^2, x, algorithm="giac")

[Out] Timed out

maple [A] time = 18.37, size = 0, normalized size = 0.00

$$\int \frac{1}{(dx+c)^2 (a+b \tan (fx+e))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x+c)^2/(a+b*tan(f*x+e))^2,x)

[Out] int(1/(d*x+c)^2/(a+b*tan(f*x+e))^2,x)

maxima [F(-1)] time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)^2/(a+b*tan(f*x+e))^2,x, algorithm="maxima")

[Out] Timed out

mupad [A] time = 0.00, size = -1, normalized size = -0.04

$$\int \frac{1}{(a+b \tan (e+f x))^2 (c+d x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/((a + b*tan(e + f*x))^2*(c + d*x)^2),x)

[Out] int(1/((a + b*tan(e + f*x))^2*(c + d*x)^2), x)

sympy [A] time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{1}{(a+b \tan (e+f x))^2 (c+d x)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x+c)**2/(a+b*tan(f*x+e))**2,x)

[Out] Integral(1/((a + b*tan(e + f*x))**2*(c + d*x)**2), x)

Chapter 4

Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

4.0.1 Mathematica and Rubi grading function

```
(* Original version thanks to Albert Rich emailed on 03/21/2017 *)
(* ::Package:: *)

(* ::Subsection:: *)
(*GradeAntiderivative[result,optimal]*)

(* ::Text:: *)
(*If result and optimal are mathematical expressions, *)
(*      GradeAntiderivative[result,optimal] returns*)
(* "F" if the result fails to integrate an expression that*)
(*   is integrable*)
(* "C" if result involves higher level functions than necessary*)
(* "B" if result is more than twice the size of the optimal*)
(*   antiderivative*)
(* "A" if result can be considered optimal*)

GradeAntiderivative[result_,optimal_] :=
  If[ExpnType[result]<=ExpnType[optimal],
    If[FreeQ[result,Complex] || Not[FreeQ[optimal,Complex]],
      If[LeafCount[result]<=2*LeafCount[optimal],
        "A",
        "B"],
      "C"],
    If[FreeQ[result,Integrate] && FreeQ[result,Int],
      "C",
      "F"]]

(* ::Text:: *)
(*The following summarizes the type number assigned an *)
(*expression based on the functions it involves*)
(*1 = rational function*)
(*2 = algebraic function*)
```

```

(*3 = elementary function*)
(*4 = special function*)
(*5 = hyperpergeometric function*)
(*6 = appell function*)
(*7 = rootsum function*)
(*8 = integrate function*)
(*9 = unknown function*)

ExpnType[expn_] :=
  If[AtomQ[expn],
    1,
  If[ListQ[expn],
    Max[Map[ExpnType,expn]],
  If[Head[expn]===Power,
    If[IntegerQ[expn[[2]]],
      ExpnType[expn[[1]]],
    If[Head[expn[[2]]]===Rational,
      If[IntegerQ[expn[[1]]] || Head[expn[[1]]]===Rational,
        1,
        Max[ExpnType[expn[[1]],2]],
      Max[ExpnType[expn[[1]],ExpnType[expn[[2]],3]]],
  If[Head[expn]===Plus || Head[expn]===Times,
    Max[ExpnType[First[expn]],ExpnType[Rest[expn]]],
  If[ElementaryFunctionQ[Head[expn]],
    Max[3,ExpnType[expn[[1]]]],
  If[SpecialFunctionQ[Head[expn]],
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],4]],
  If[HypergeometricFunctionQ[Head[expn]],
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],5]],
  If[AppellFunctionQ[Head[expn]],
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],6]],
  If[Head[expn]===RootSum,
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],7]],
  If[Head[expn]===Integrate || Head[expn]===Int,
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],8]],
  9]]]]]]]]]]

ElementaryFunctionQ[func_] :=
  MemberQ[{
    Exp,Log,
    Sin,Cos,Tan,Cot,Sec,Csc,
    ArcSin,ArcCos,ArcTan,ArcCot,ArcSec,ArcCsc,
    Sinh,Cosh,Tanh,Coth,Sech,Csch,
    ArcSinh,ArcCosh,ArcTanh,ArcCoth,ArcSech,ArcCsch
  },func]

SpecialFunctionQ[func_] :=
  MemberQ[{
    Erf, Erfc, Erfi,
    FresnelS, FresnelC,
    ExpIntegralE, ExpIntegralEi, LogIntegral,
    SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
    Gamma, LogGamma, PolyGamma,
    Zeta, PolyLog, ProductLog,
    EllipticF, EllipticE, EllipticPi
  },func]

HypergeometricFunctionQ[func_] :=
  MemberQ[{Hypergeometric1F1,Hypergeometric2F1,HypergeometricPFQ},func]

```

```
AppellFunctionQ[func_] :=
  MemberQ[{AppellF1},func]
```

4.0.2 Maple grading function

```
# File: GradeAntiderivative.mpl
# Original version thanks to Albert Rich emailed on 03/21/2017

#Nasser 03/22/2017 Use Maple leaf count instead since buildin
#Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
#Nasser 03/24/2017 corrected the check for complex result
#Nasser 10/27/2017 check for leafsize and do not call ExpnType()
#
# if leaf size is "too large". Set at 500,000
#Nasser 12/22/2019 Added debug flag, added 'dilog' to special functions
#
# see problem 156, file Apostol_Problems

GradeAntiderivative := proc(result,optimal)
local leaf_count_result, leaf_count_optimal,ExpnType_result,ExpnType_optimal,
  debug:=false;

  leaf_count_result:=leafcount(result);
  #do NOT call ExpnType() if leaf size is too large. Recursion problem
  if leaf_count_result > 500000 then
    return "B";
  fi;

  leaf_count_optimal:=leafcount(optimal);

  ExpnType_result:=ExpnType(result);
  ExpnType_optimal:=ExpnType(optimal);

  if debug then
    print("ExpnType_result",ExpnType_result," ExpnType_optimal=",
ExpnType_optimal);
  fi;

# If result and optimal are mathematical expressions,
# GradeAntiderivative[result,optimal] returns
# "F" if the result fails to integrate an expression that
# is integrable
# "C" if result involves higher level functions than necessary
# "B" if result is more than twice the size of the optimal
# antiderivative
# "A" if result can be considered optimal

#This check below actually is not needed, since I only
#call this grading only for passed integrals. i.e. I check
#for "F" before calling this. But no harm of keeping it here.
#just in case.

if not type(result,freeof('int')) then
  return "F";
end if;

if ExpnType_result<=ExpnType_optimal then
  if debug then
    print("ExpnType_result<=ExpnType_optimal");
  fi;

```

```

if is_contains_complex(result) then
  if is_contains_complex(optimal) then
    if debug then
      print("both result and optimal complex");
    fi;
    #both result and optimal complex
    if leaf_count_result<=2*leaf_count_optimal then
      return "A";
    else
      return "B";
    end if
  else #result contains complex but optimal is not
    if debug then
      print("result contains complex but optimal is not");
    fi;
    return "C";
  end if
else # result do not contain complex
  # this assumes optimal do not as well
  if debug then
    print("result do not contain complex, this assumes optimal do
not as well");
  fi;
  if leaf_count_result<=2*leaf_count_optimal then
    if debug then
      print("leaf_count_result<=2*leaf_count_optimal");
    fi;
    return "A";
  else
    if debug then
      print("leaf_count_result>2*leaf_count_optimal");
    fi;
    return "B";
  end if
end if
else #ExpnType(result) > ExpnType(optimal)
  if debug then
    print("ExpnType(result) > ExpnType(optimal)");
  fi;
  return "C";
end if

end proc:

#
# is_contains_complex(result)
# takes expressions and returns true if it contains "I" else false
#
#Nasser 032417
is_contains_complex:= proc(expression)
  return (has(expression,I));
end proc:

# The following summarizes the type number assigned an expression
# based on the functions it involves
# 1 = rational function
# 2 = algebraic function
# 3 = elementary function
# 4 = special function
# 5 = hyperpergeometric function
# 6 = appell function
# 7 = rootsum function
# 8 = integrate function

```

```

# 9 = unknown function

ExpnType := proc(expn)
  if type(expn,'atomic') then
    1
  elif type(expn,'list') then
    apply(max,map(ExpnType,expn))
  elif type(expn,'sqrt') then
    if type(op(1,expn),'rational') then
      1
    else
      max(2,ExpnType(op(1,expn)))
    end if
  elif type(expn,'^^') then
    if type(op(2,expn),'integer') then
      ExpnType(op(1,expn))
    elif type(op(2,expn),'rational') then
      if type(op(1,expn),'rational') then
        1
      else
        max(2,ExpnType(op(1,expn)))
      end if
    else
      max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    end if
  elif type(expn,'+' or type(expn,'*') then
    max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
  elif ElementaryFunctionQ(op(0,expn)) then
    max(3,ExpnType(op(1,expn)))
  elif SpecialFunctionQ(op(0,expn)) then
    max(4,apply(max,map(ExpnType,[op(expn)])))
  elif HypergeometricFunctionQ(op(0,expn)) then
    max(5,apply(max,map(ExpnType,[op(expn)])))
  elif AppellFunctionQ(op(0,expn)) then
    max(6,apply(max,map(ExpnType,[op(expn)])))
  elif op(0,expn)='int' then
    max(8,apply(max,map(ExpnType,[op(expn)]))) else
    9
  end if
end proc:

ElementaryFunctionQ := proc(func)
  member(func,[
    exp,log,ln,
    sin,cos,tan,cot,sec,csc,
    arcsin,arccos,arctan,arccot,arcsec,arccsc,
    sinh,cosh,tanh,coth,sech,csch,
    arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
end proc:

SpecialFunctionQ := proc(func)
  member(func,[
    erf,erfc,erfi,
    FresnelS,FresnelC,
    Ei,Ei,Li,Si,Ci,Shi,Chi,
    GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
    EllipticF,EllipticE,EllipticPi])
end proc:

HypergeometricFunctionQ := proc(func)
  member(func,[Hypergeometric1F1,hypergeom,HypergeometricPFQ])
end proc:

```

```

AppellFunctionQ := proc(func)
  member(func,[AppellF1])
end proc:

# u is a sum or product. rest(u) returns all but the
# first term or factor of u.
rest := proc(u) local v;
  if nops(u)=2 then
    op(2,u)
  else
    apply(op(0,u),op(2..nops(u),u))
  end if
end proc:

#leafcount(u) returns the number of nodes in u.
#Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
leafcount := proc(u)
  MmaTranslator[Mma][LeafCount](u);
end proc:

```

4.0.3 Sympy grading function

```

#Dec 24, 2019. Nasser M. Abbasi:
#           Port of original Maple grading function by
#           Albert Rich to use with Sympy/Python
#Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
#           added 'exp_polar'
from sympy import *

def leaf_count(expr):
  #sympy do not have leaf count function. This is approximation
  return round(1.7*count_ops(expr))

def is_sqrt(expr):
  if isinstance(expr,Pow):
    if expr.args[1] == Rational(1,2):
      return True
    else:
      return False
  else:
    return False

def is_elementary_function(func):
  return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
    asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
    asinh,acosh,atanh,acoth,asech,acsch
  ]

def is_special_function(func):
  return func in [ erf,erfc,erfi,
    fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
    gamma,loggamma,digamma,zeta,polylog,LambertW,
    elliptic_f,elliptic_e,elliptic_pi,exp_polar
  ]

def is_hypergeometric_function(func):
  return func in [hyper]

def is_appell_function(func):
  return func in [appellf1]

```



```

def is_atom(expn):
    try:
        if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
            return True
        else:
            return False

    except AttributeError as error:
        return False

def expnType(expn):
    debug=False
    if debug:
        print("expn=",expn,"type(expn)=",type(expn))

    if is_atom(expn):
        return 1
    elif isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
            return 1
        else:
            return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Pow): #type(expn,'^^')
        if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
            return expnType(expn.args[0]) #ExpnType(op(1,expn))
        elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
            if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
                return 1
            else:
                return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,'+`' or
    type(expn,'*`)
        m1 = expnType(expn.args[0])
        m2 = expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
    elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
        return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
    elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))
    elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,
    expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif is_appell_function(expn.func):
        m1 = max(map(expnType, list(expn.args)))
        return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif isinstance(expn,RootSum):
        m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType
    ,Apply[List,expn]],7]],
        return max(7,m1)
    elif str(expn).find("Integral") != -1:
        m1 = max(map(expnType, list(expn.args)))
        return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    else:
        return 9

```

```

#main function
def grade_antiderivative(result,optimal):

    leaf_count_result = leaf_count(result)
    leaf_count_optimal = leaf_count(optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if str(result).find("Integral") != -1:
        return "F"

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex
                if leaf_count_result <= 2*leaf_count_optimal:
                    return "A"
                else:
                    return "B"
            else: #result contains complex but optimal is not
                return "C"
        else: # result do not contain complex, this assumes optimal do not as
well
            if leaf_count_result <= 2*leaf_count_optimal:
                return "A"
            else:
                return "B"
    else:
        return "C"

```

4.0.4 SageMath grading function

```

#Dec 24, 2019. Nasser: Ported original Maple grading function by
#           Albert Rich to use with Sagemath. This is used to
#           grade Fricas, Giac and Maxima results.
#Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
#           'arctan2','floor','abs','log_integral'

from sage.all import *
from sage.symbolic.operators import add_vararg, mul_vararg

debug=False;

def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)

def is_sqrt(expr):
    if expr.operator() == operator.pow: #isinstance(expr,Pow):
        if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
            if debug: print ("expr is sqrt")
            return True

```

```

        else:
            return False
    else:
        return False

def is_elementary_function(func):
    debug=False
    m = func.name() in ['exp','log','ln',
        'sin','cos','tan','cot','sec','csc',
        'arcsin','arccos','arctan','arccot','arcsec','arccsc',
        'sinh','cosh','tanh','coth','sech','csch',
        'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
        'arctan2','floor','abs'
    ]
    if debug:
        if m:
            print ("func ", func , " is elementary_function")
        else:
            print ("func ", func , " is NOT elementary_function")

    return m

def is_special_function(func):
    debug=False
    if debug: print ("type(func)=", type(func))

    m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
        'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','
sinh_integral'
        'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
        'polylog','lambert_w','elliptic_f','elliptic_e',
        'elliptic_pi','exp_integral_e','log_integral']

    if debug:
        print ("m=",m)
        if m:
            print ("func ", func ," is special_function")
        else:
            print ("func ", func ," is NOT special_function")

    return m

def is_hypergeometric_function(func):
    return func.name() in ['hypergeometric','hypergeometric_M',
hypergeometric_U']

def is_appell_function(func):
    return func.name() in ['hypergeometric']    #[appellf1] can't find this in
sagemath

def is_atom(expn):

    debug=False
    if debug: print ("Enter is_atom")

    #thanks to answer at https://ask.sagemath.org/question/49179/what-is-sagemath-equivalent-to-atomic-type-in-maple/
    try:
        if expn.parent() is SR:

```

```

        return expn.operator() is None
    if expn.parent() in (ZZ, QQ, AA, QQbar):
        return expn in expn.parent() # Should always return True
    if hasattr(expn.parent(),"base_ring") and hasattr(expn.parent(),"gens")
:
        return expn in expn.parent().base_ring() or expn in expn.parent().
gens()
    return False

except AttributeError as error:
    return False

def expnType(expn):

    if debug:
        print(">>>>Enter expnType, expn=", expn)
        print(">>>>is_atom(expn)=", is_atom(expn))

    if is_atom(expn):
        return 1
    elif type(expn)==list: #isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if type(expn.operands()[0])==Rational: #type(isinstance(expn.args[0],
Rational):
            return 1
        else:
            return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.
args[0]))
    elif expn.operator() == operator.pow: #isinstance(expn,Pow)
        if type(expn.operands()[1])==Integer: #isinstance(expn.args[1],Integer
)
            return expnType(expn.operands()[0]) #expnType(expn.args[0])
        elif type(expn.operands()[1])==Rational: #isinstance(expn.args[1],
Rational)
            if type(expn.operands()[0])==Rational: #isinstance(expn.args[0],
Rational)
                return 1
            else:
                return max(2,expnType(expn.operands()[0])) #max(2,expnType(
expn.args[0]))
        else:
            return max(3,expnType(expn.operands()[0]),expnType(expn.operands()
[1])) #max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1]))
    elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #
isinstance(expn,Add) or isinstance(expn,Mul)
        m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
        m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn)))
    elif is_elementary_function(expn.operator()): #is_elementary_function(expn
.func)
        return max(3,expnType(expn.operands()[0]))
    elif is_special_function(expn.operator()): #is_special_function(expn.func)
        m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
        return max(4,m1) #max(4,m1)
    elif is_hypergeometric_function(expn.operator()): #
is_hypergeometric_function(expn.func)
        m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))
        return max(5,m1) #max(5,m1)
    elif is_appell_function(expn.operator()):

```

```

        m1 = max(map(expnType, expn.operands()))      #max(map(expnType, list(
expn.args)))
        return max(6,m1)      #max(6,m1)
    elif str(expn).find("Integral") != -1: #this will never happen, since it
        #is checked before calling the grading function that is passed.
        #but kept it here.
        m1 = max(map(expnType, expn.operands()))      #max(map(expnType, list(
expn.args)))
        return max(8,m1)      #max(5,apply(max,map(ExpnType,[op(expn)])))
    else:
        return 9

#main function
def grade_antiderivative(result,optimal):

    if debug: print ("Enter grade_antiderivative for sagemath")

    leaf_count_result = tree_size(result) #leaf_count(result)
    leaf_count_optimal = tree_size(optimal) #leaf_count(optimal)

    if debug: print ("leaf_count_result=", leaf_count_result, "
leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",
expnType_optimal)

    if expnType_result <= expnType_optimal:
        if result.has(I):
            if optimal.has(I): #both result and optimal complex
                if leaf_count_result <= 2*leaf_count_optimal:
                    return "A"
                else:
                    return "B"
            else: #result contains complex but optimal is not
                return "C"
        else: # result do not contain complex, this assumes optimal do not as
well
            if leaf_count_result <= 2*leaf_count_optimal:
                return "A"
            else:
                return "B"
    else:
        return "C"

```